

Tutorial IV

Multi-material, self-consistent subduction with a free surface¹

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¹Schmeling et al., PEPI, 2008

Succeeded in:

- Setting up a model with one compositional heterogeneity
- Using ASPECT's function parser
- Setting up mesh-independent initial conditions
- Tackling benchmark problems

By the end of this tutorial, you should be able to

- Write and install new material **plugins**
- Modify the input parameter file for a **subduction** model with multiple materials
- Understand issues regarding **averaging**
- Understand the concept of “**sticky-air**” and its effect on the solver

Simple subduction

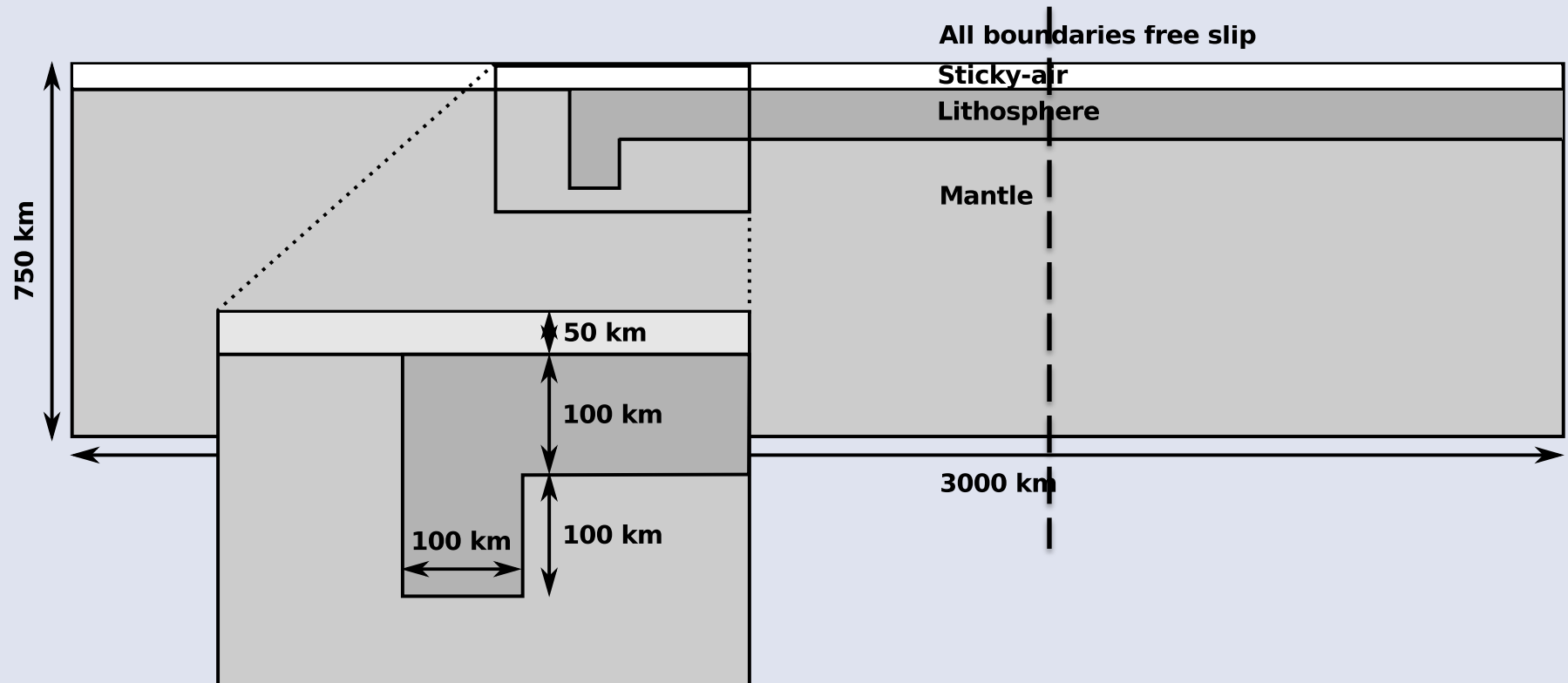
Start simple:

Subduction model of

Schmeling et al. 2008 (PEPI 171)

- 2D
- No temperature effects
- Constant viscosities
- Benchmark →
results of other codes to compare

Schmeling et al. 2008 subduction



Although a relatively simple setup,
it discusses very important points:

- Effect of different **averaging** methods on viscosities near rheological boundaries
- **Decoupling** subducting plate from the surface
- Approximation of **free surface** through sticky-air

Sticky-air

- Thin layer of relatively low viscosity (10^{19} Pas) and density (0 kg/m^3) to allow for surface deformation
- No need to deform grid, but
- High viscosity contrasts and
- High resolution needed

Changes compared to Tutorial III:

- Prescribe parameters of multiple (>2) materials
- Implement 4 different types of averaging of materials



1. Modify [schmelting_empty.prm](#)
2. Write a new Material Model based on assigned averaging method
3. Run simulation and visualize results
4. Report slap tip depth after 1 and 2 My

Editing the input file

We will begin by editing the input file

1. Change to the appropriate directory

```
> cd ~/ASPECT_TUTORIAL/models
```

2. Open the parameter file for editing

```
> gedit schmelting_empty.prm
```

Editing the input file

Now read through the following sections in the input file and edit the **red** sections:

1. Global parameters
2. Geometry model
3. **Compositional fields**
4. **Material model**
5. Compositional initial conditions

Editing the input file

Global parameters

```
set Dimension = 2
set Start time = 0
set End time = 0
set Use years in output instead of seconds = true
set Number of cheap solver steps = 0
set Output directory = schmeling
```

Geometry model

```
subsection Geometry model
  set Model name = box
  subsection Box
    set X extent = 2000000
    set Y extent = 750000
    set X repetitions = 3
  end
end
```

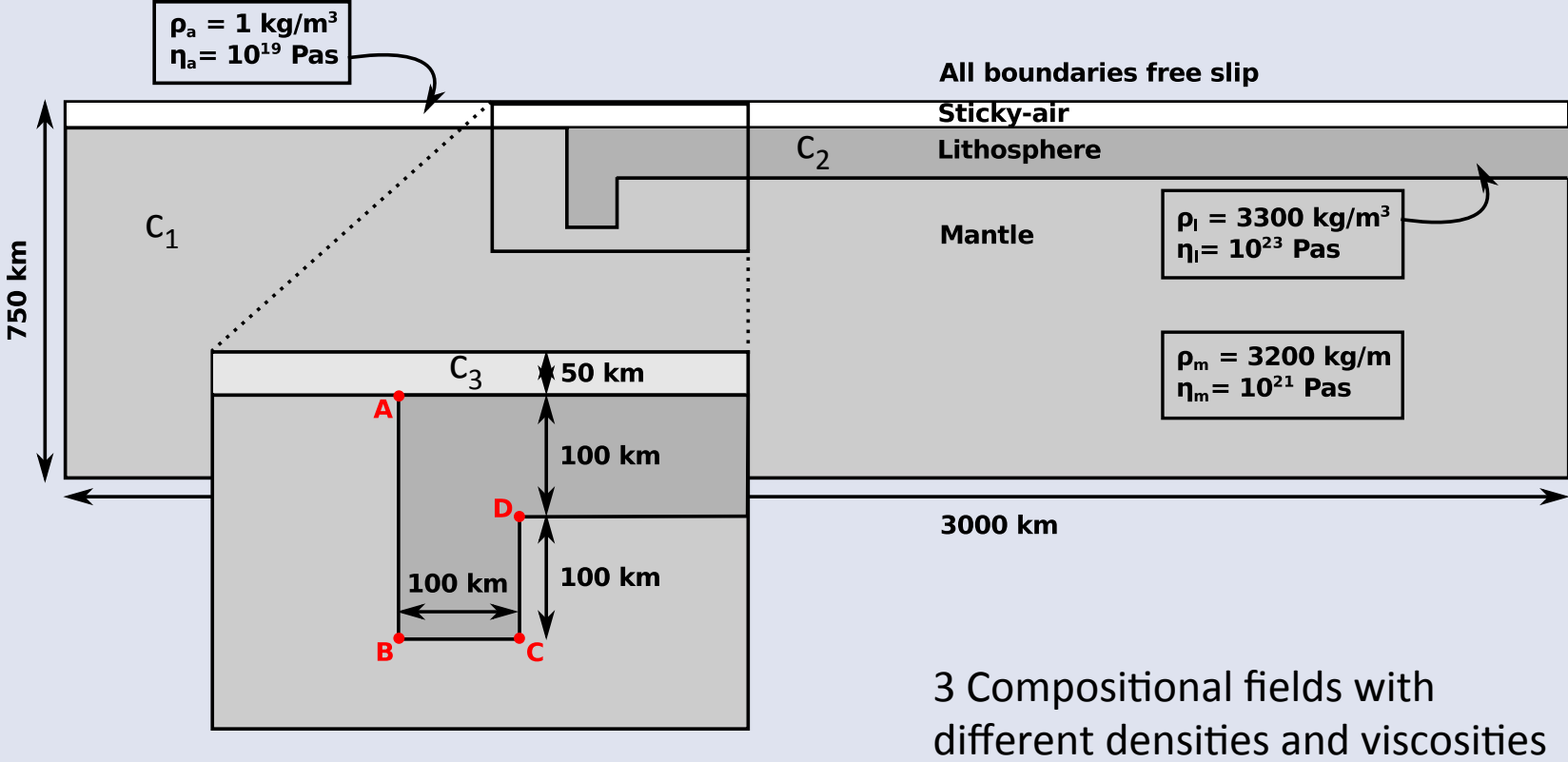
Compositional fields

```
subsection Compositional fields
  set Number of fields      =
end
subsection Compositional initial conditions
  set Model name           = function
  subsection Function
    set Variable names      = x, z
    set Function constants  = Ax = 1000000.0, Az=700000.0, Bz=500000.0,
                             Cx=1100000.0, Dz=600000.0
    set Function expression = \
      if((z<Bz)|(x<Ax&z<Az)|(x>Cx&z<Dz),1,0); \ #mantle
      if((x>=Ax&z>=Dz&z<Az)|(x>=Ax&x<=Cx&z>=Bz&z<Dz),1,0); \ #lithosphere
      if(z>=Az,1,0) # air
  end
end
```

How many compositional fields? For simplicity, we describe all materials as fields

You already know how to use the function parser!

Editing the input file



Editing the input file

Material model

Normally, here you provide a functional name for your new Material Model plugin

```
subsection Material model
set Model name = XXX
subsection XXX model
set Thermal conductivity = 0.0
set Thermal expansion coefficient = 0.0
set Reference specific heat = 1.0
set List of densities of fields =
set List of viscosities of fields =
end
end
```

No temperature effects

Here we provide the densities and viscosities of the compositions to the Material Model plugin. Use the same order as in the definition of the compositional fields.

Material Model plugins

1. Change to the appropriate directory


```
> cd ~/ASPECT_TUTORIAL/aspect/source/material_model
```

2. What files are there?

interface.cc

simple.cc
simpler.cc
steinberger.cc
table.cc ...

Material Model plugins



Plugins:

- for Geometry, Material, Gravity etc. in `~/source`
- derive from interface.cc
- can be selected from the input file

A Material Model plugin should at least provide

1. Viscosity
2. Density
3. Specific heat
4. Thermal conduct.
5. Thermal expansion
6. Compressibility

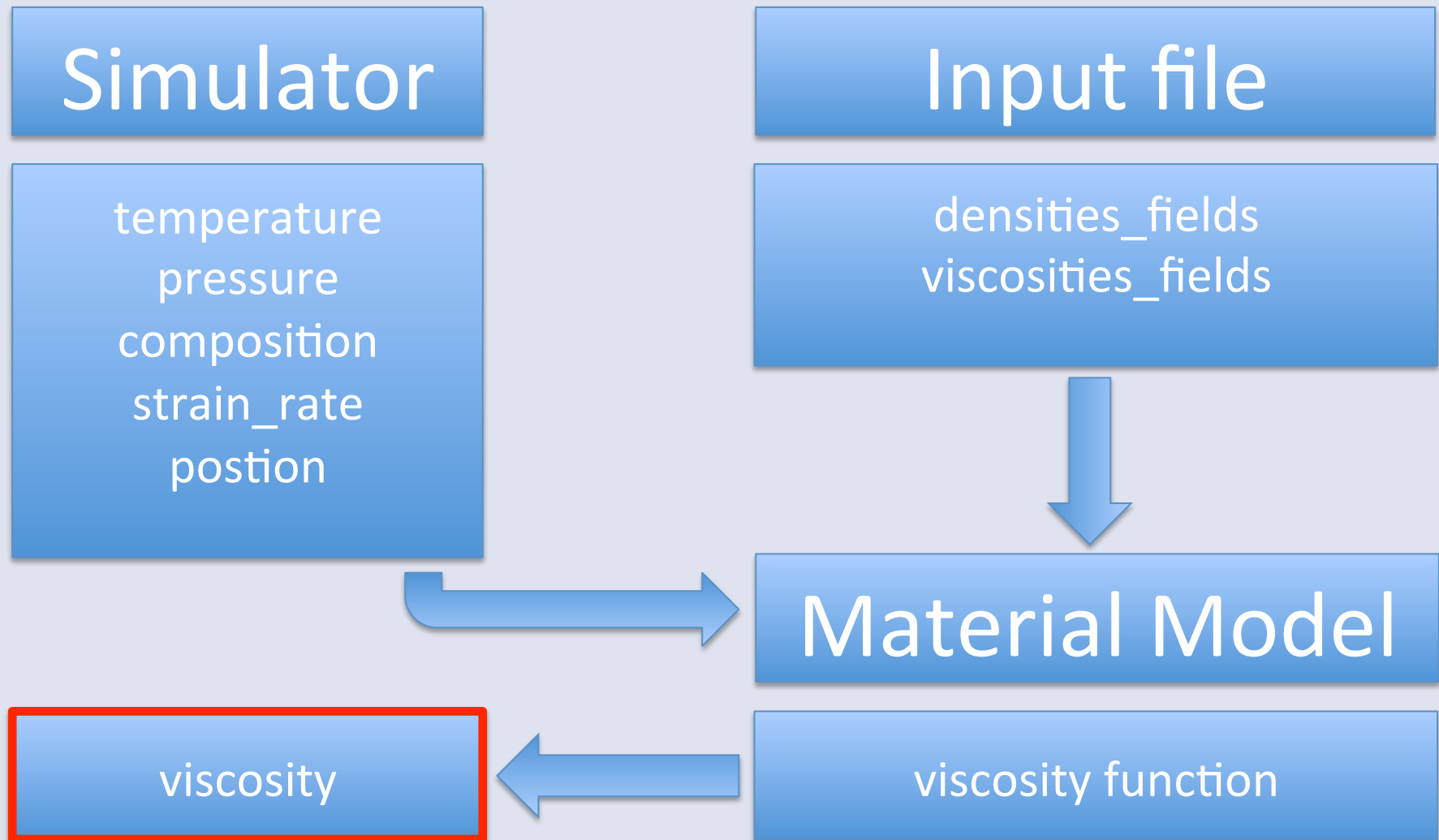
The Material Model plugin – viscosity function

So far, we used Material Model simple.cc

```
> gedit simple.cc
```

```
template <int dim>  
double  
Simple<dim>::  
viscosity (const double temperature,  
           const double pressure,  
           const std::vector<double> &composition,  
           const SymmetricTensor<2,dim> &strain_rate,  
           const Point<dim> &position) const
```

The Material Model plugin – viscosity function



The Material Model plugin – viscosity function

So far, we used Material Model simple.cc

> `gedit simple.cc`

```
const double delta_temp = temperature-reference_T;  
const double temperature_dependence = (reference_T > 0  
    ? std::max(std::min(std::exp(-thermal_viscosity_exponent*delta_temp/  
reference_T),1e2),1e-2)  
    : 1.0);  
double composition_dependence = 1.0;  
if ((composition_viscosity_prefactor != 1.0) && (composition.size() > 0))  
{ return (pow(10, ((1-composition[0]) * log10(eta*temperature_dependence)  
    + composition[0] * log10(eta*composition_viscosity_prefactor  
    *temperature_dependence))));  
}  
return composition_dependence * temperature_dependence * eta;
```

The Material Model plugin – viscosity function

So far, we used Material Model simple.cc

```
> gedit simple.cc
```

```
if (composition.size() > 0)
{ return (pow(10, ((1-composition[0]) * log10(eta)
+ composition[0] * log10(eta*composition_viscosity_prefactor)));
}
```

What kind of averaging?

Writing a viscosity function

ASPECT: build on others!



- [XXX.cc](#) is a slightly adapted copy of simple.cc
- Implement a viscosity function (line 35) that averages the contribution of the fields as follows:

- Group 1: Harmonic averaging
- Group 2: Geometric averaging
- Group 3: Arithmetic averaging
- Group 4: Infinite norm

Writing a viscosity function

Group 1 - Harmonic

$$\eta_{harm} = \frac{c_1 + c_2 + c_3}{\frac{c_1}{\eta_1} + \frac{c_2}{\eta_2} + \frac{c_3}{\eta_3}}$$

Group 2 - Geometric

$$\log \eta_{geom} = \frac{c_1 \log \eta_1 + c_2 \log \eta_2 + c_3 \log \eta_3}{c_1 + c_2 + c_3}$$

Group 3 - Arithmetic

$$\eta_{arith} = \frac{c_1 \eta_1 + c_2 \eta_2 + c_3 \eta_3}{c_1 + c_2 + c_3}$$

Group 4 - Infinite norm

$$\eta_{inf} = \eta_{\max(c_i)}$$

Where c_i represent the values of the 3 compositional fields, and η_i are the viscosities of each corresponding field.

~/ASPECT_TUTORIAL/aspect/source/material_model/schmelting.cc is a working material model with each averaging method implemented in case you need it

Advection of a field

The advection of compositional fields can result in under- and overshooting of the c_i values near steep gradients →

1. Prevent oscillations

Stabilization (Guermond et al., J. Comput. Phys., 2011):

$$\frac{\partial c_i}{\partial t} + u \cdot \nabla c_i - \nabla \cdot \nu_h \nabla c_i = 0$$



2. Deal with oscillations

Cut off c_i between 0 and 1

ADVECTION OF A STEP FUNCTION

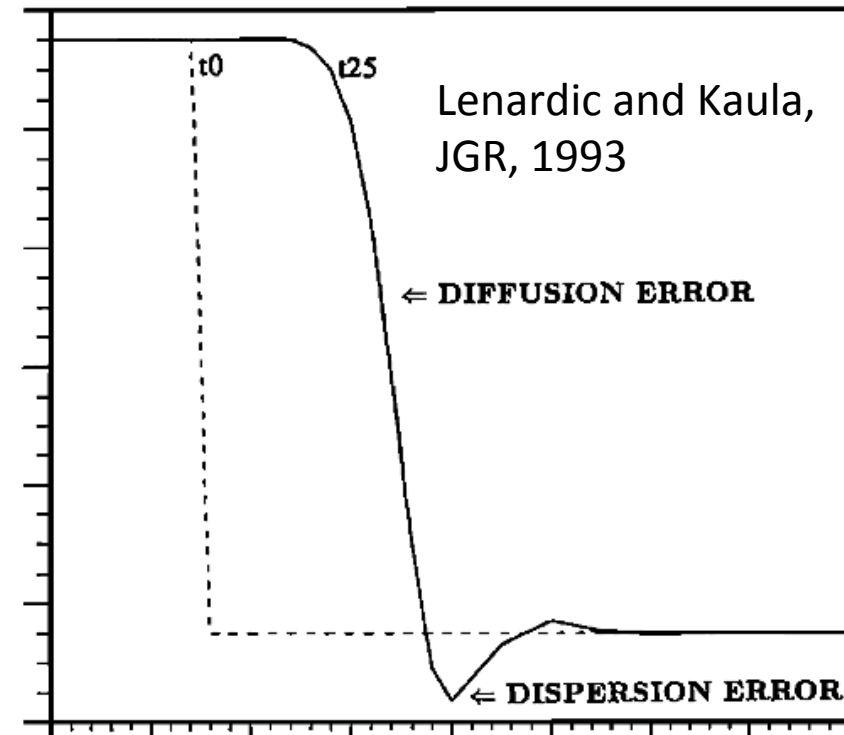


Fig. 1. Numerical advection of a step function over 25 Courant-Friedrichs-Lewy time steps. T_0 is the initial step function and T_{25} is the advected step function. Two types of numerical errors are present: (1) numerical diffusion reflected in the tilting of the step; and (2) numerical dispersion resulting in the leading edge ripples. The numerical scheme employed was second-order accurate for smooth flow problems.

C++ syntax

- Always end declarations and assignments with
“.”
;
- The first entry of a vector is accessed with “0”:
e.g. `composition[0]`
- Calculating a minimum of two numbers with:
e.g. `std::min(composition[0],1.0)`

Plugin installation

```
> cd ~/ASPECT_TUTORIAL/aspect/include/ \
    aspect/material_model/
```

Here the corresponding header file `XXX.h` is located

```
> cd ~/ASPECT_TUTORIAL/aspect/debug
```

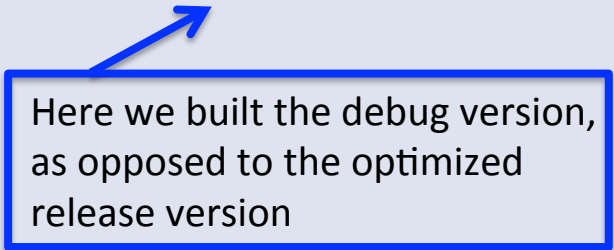
Normally, you would call

```
> cmake .
```

```
> make
```

to compile and install your new plugin. Build system *cmake* will automatically detect it. Now you only need to call

```
> make -j2
```



Here we built the debug version, as opposed to the optimized release version

Using ASPECT

Now run ASPECT in the terminal

1. Change to the appropriate directory

```
> cd ~/ASPECT_TUTORIAL/models/
```

2. Run ASPECT with the tutorial parameter file

```
> mpirun -np 2 aspect-debug schmelting_empty.prm
```

3. If correct,

```
> cd ~/ASPECT_TUTORIAL/aspect/release
```

```
> make -j2
```

4. Change model time to 2.5 My and rerun (this will take about 15 minutes, have a coffee)

5. Use ParaView to visualize slab evolution

```
> paraview schmelting/solution.pvd
```

Subduction evolution

Report slab tip depth after 1 and 2 My and model time

	Harmonic	Geometric	Arithmetic	Infinite
1 My Slab tip depth	(???)	(???)	(???)	(???)
2 My Slab tip depth	(???)	(???)	(???)	(???)
Model time after 15 min wall time	(???)	(???)	(???)	(???)

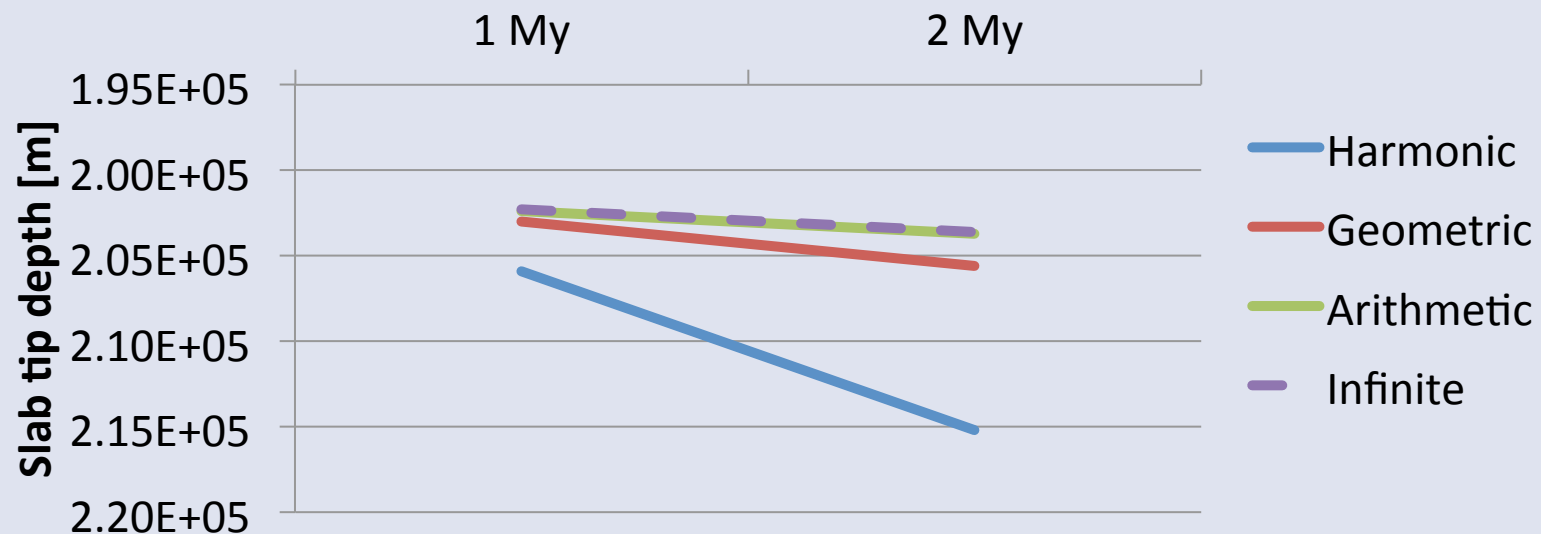
Subduction evolution

Finding slab tip depth in ParaView:

- Plot isocontour $C_2 = 0.5$
1. Use grid lines to estimate, or
 2. Use Spreadsheet view of isocontour with *Show only selected elements* and 3D view *Select Points On*, or
 3. Use Spreadsheet view and Python calculator, or
 4. Next time, write an ASPECT postprocessor 😊

Subduction evolution answer key

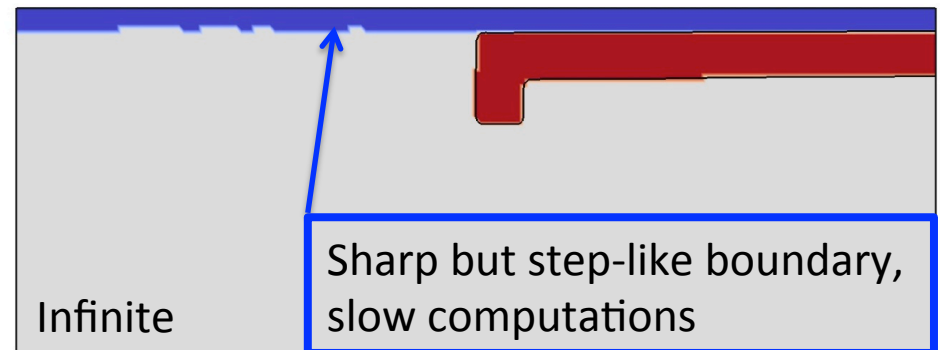
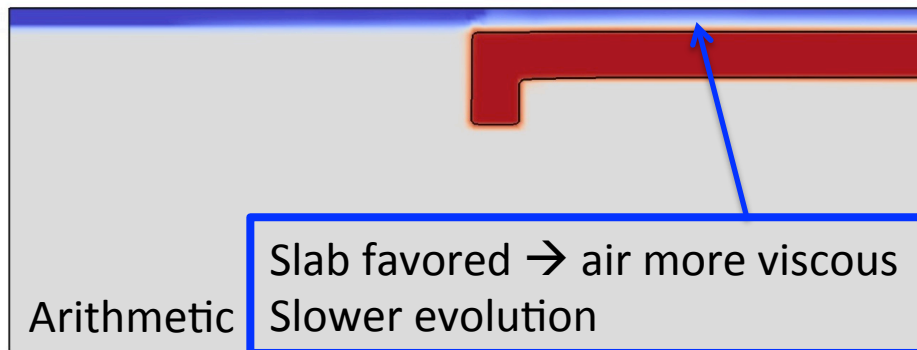
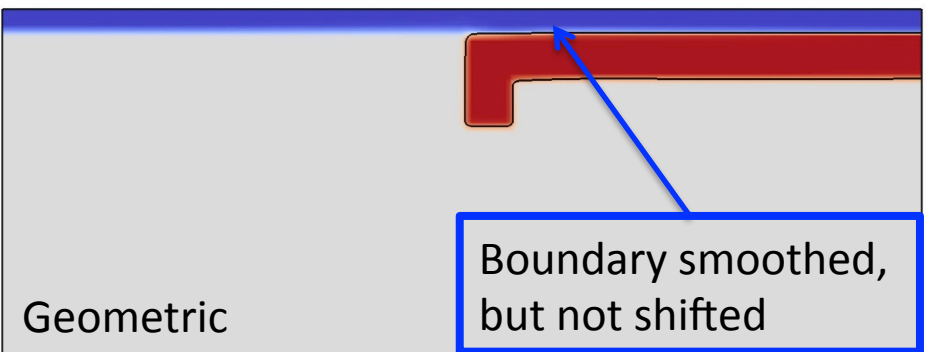
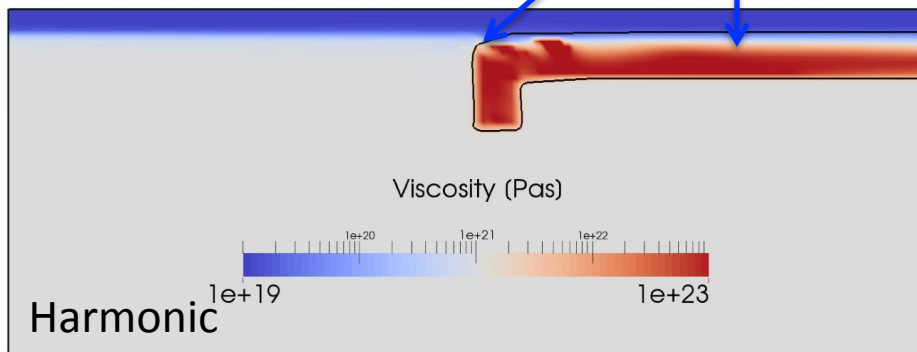
	Harmonic	Geometric	Arithmetic	Infinite
1 My Slab tip depth	205,892 m	202,983	202,387	202,291
2 My Slab tip depth	215,181 m	205,587	203,725	203,629
Model time after 15 min wall time	2.11903e6 yr	2.14136e6	2.20938e6	329,512



Results after 2 My

Slab detaching from surface

Air favored \rightarrow slab thinned

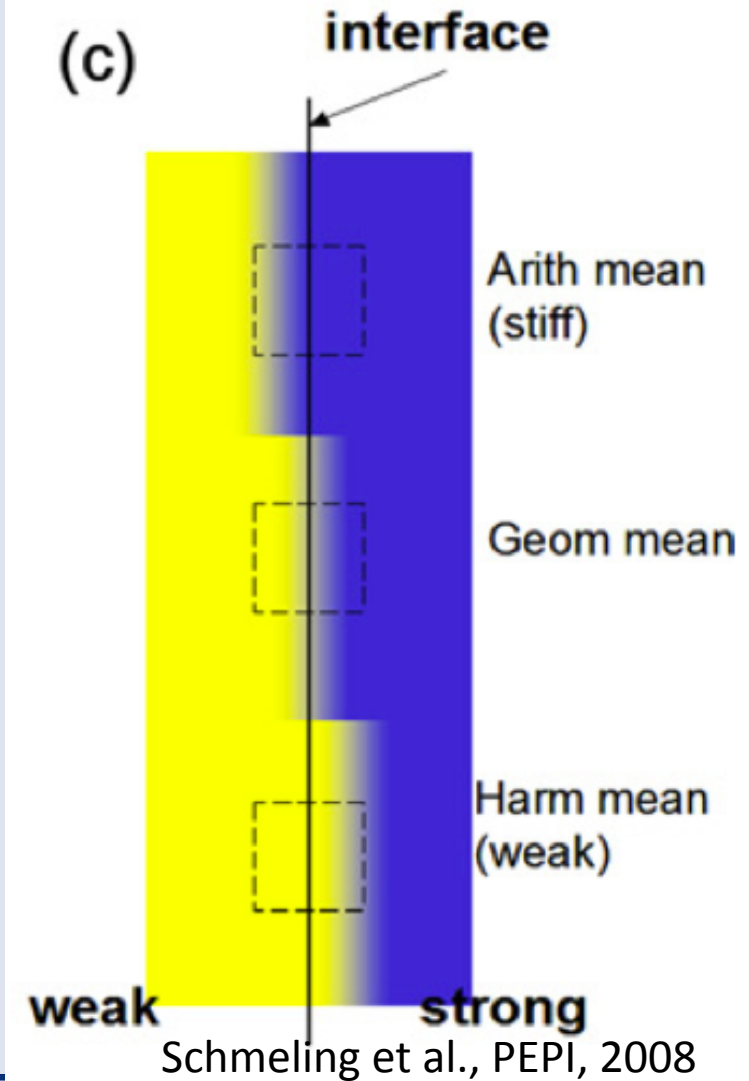


So what averaging do we use?

- Averaging affects rheological boundaries

Schmeling et al. (2008):

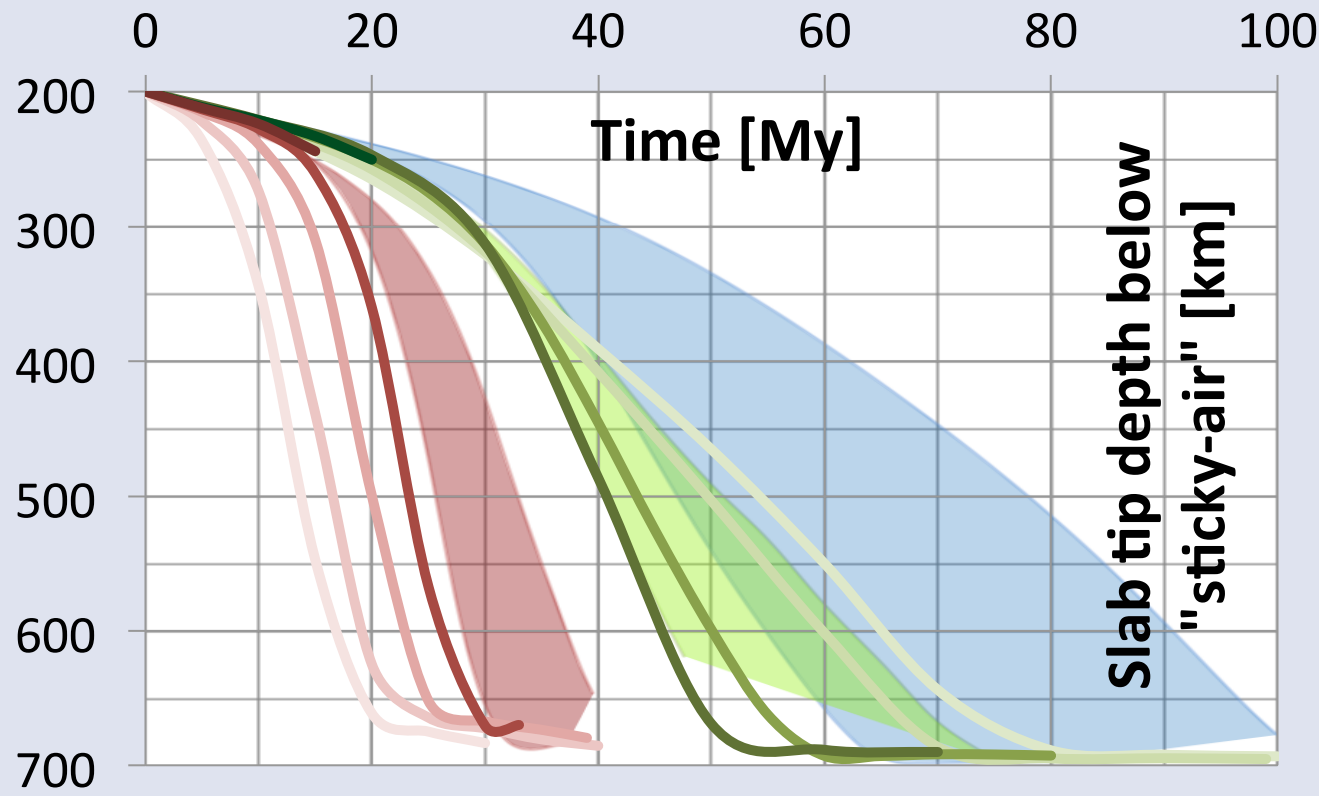
- Harmonic \rightarrow equivalent to effective viscosity of 2 viscous elements acting in series, like channel flow with flow-parallel compositional boundary, i.e. simple shear. Results in weak effective viscosity.
 - Arithmetic \rightarrow 2 viscous elements in parallel, interface-parallel pure shear. Results in stiff effective viscosity.
 - Geometric norm has no physical model, intermediate viscosity.
- \rightarrow Harmonic mean more appropriate for high viscosity contrasts ($1e4$) and flows dominated by cusp-like overriding wedges



Subduction evolution

Harmonic: higher resolution, slower subduction

Geometric: higher resolution, faster subduction



Shaded areas from
Schmeling et al., PEPI,
2008, lines obtained
with ASPECT

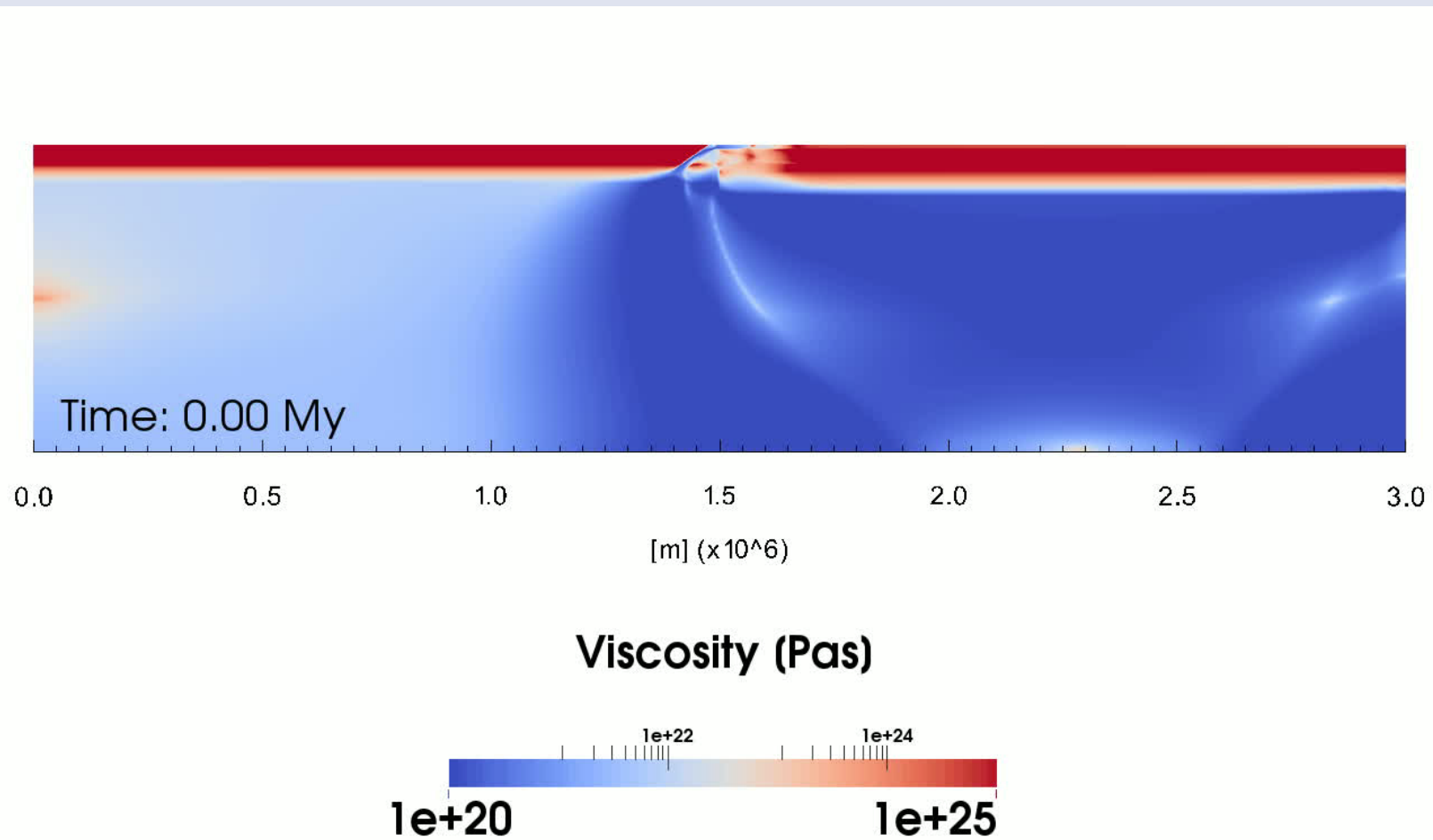
Results harmonic averaging



Red colors indicate composition 2

- More materials with different characteristics, i.e. overriding plate and crust
- Realistic deformation mechanisms, i.e. elasto-visco-plasticity
- Complex boundary conditions, i.e. plate velocities, free surfaces, open boundaries
- 4D modeling

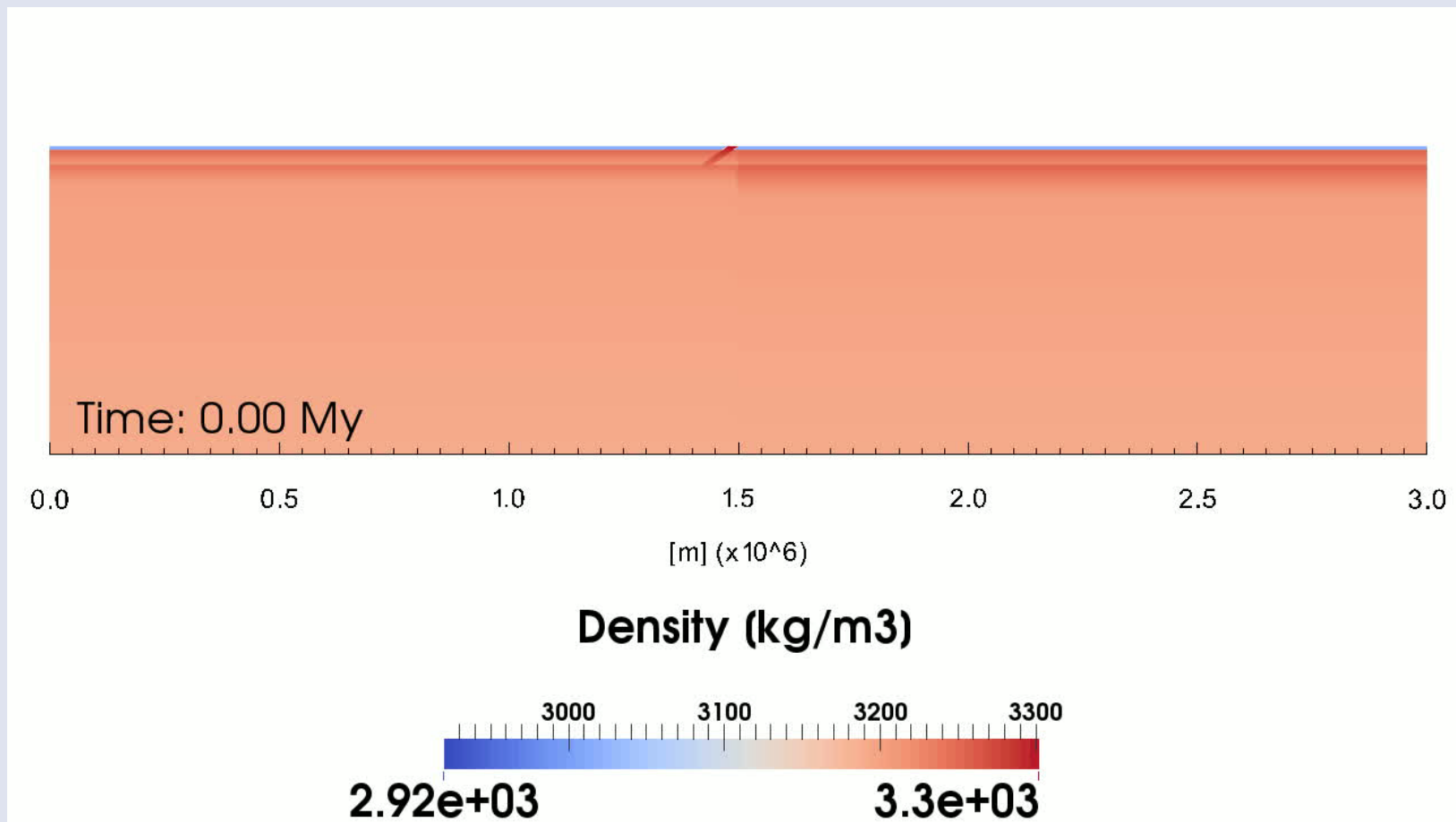
Example – Quinquis et al. (in prep)



ASPECT 2014 – visco-plastic, thermo-mechanically coupled subduction, 8 materials



Example – Quinquis et al. (in prep)



ASPECT 2014 – visco-plastic, thermo-mechanically coupled subduction, 8 materials

