

A tomography map of the Mojavian lithosphere viscosity. The map uses a color scale from blue (low viscosity) to red (high viscosity). A prominent dark grey fault line runs from the top center towards the bottom right. Other fault lines are shown in brown and grey. The background is a mix of yellow, orange, and red, indicating high viscosity regions, with some blue and purple patches indicating lower viscosity. The title text is overlaid on the upper left portion of the map.

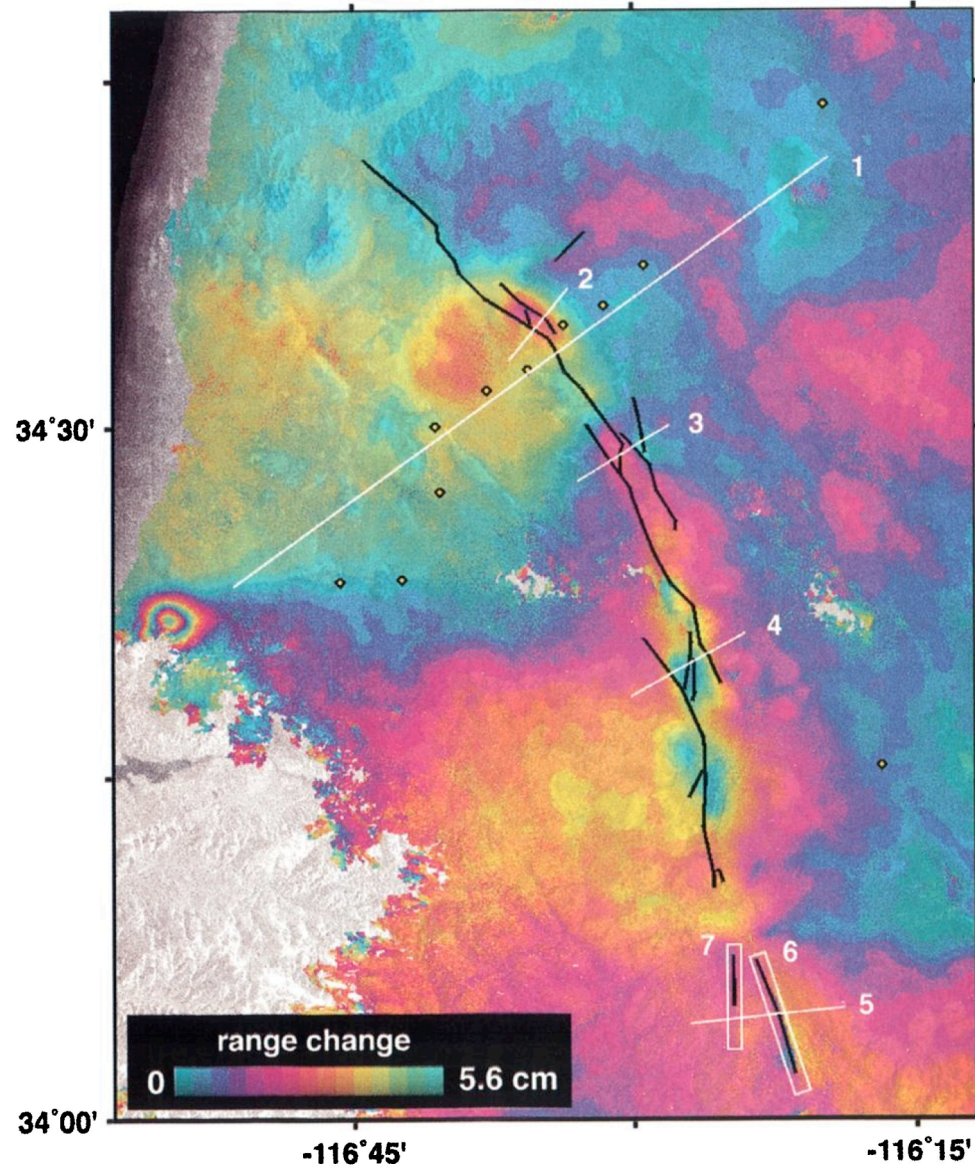
Tomography of the Mojavian Lithosphere Viscosity
from Space Geodetic data of the Landers and
Hector Mine Earthquakes

Sylvain Barbot, Yuri Fialko
CIG 2010

Poroelastic rebound along the Landers 1992 earthquake surface rupture

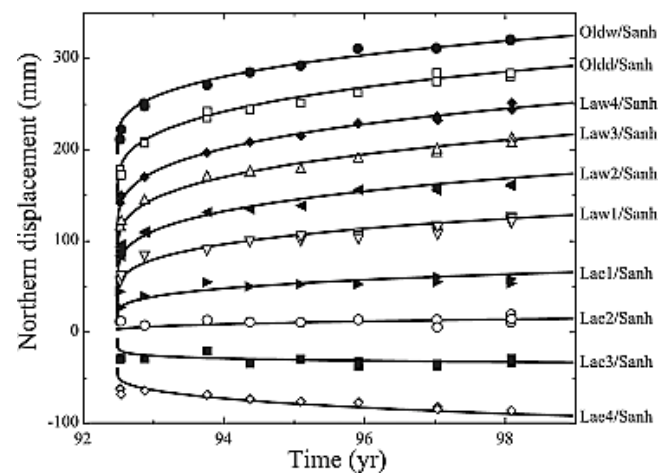
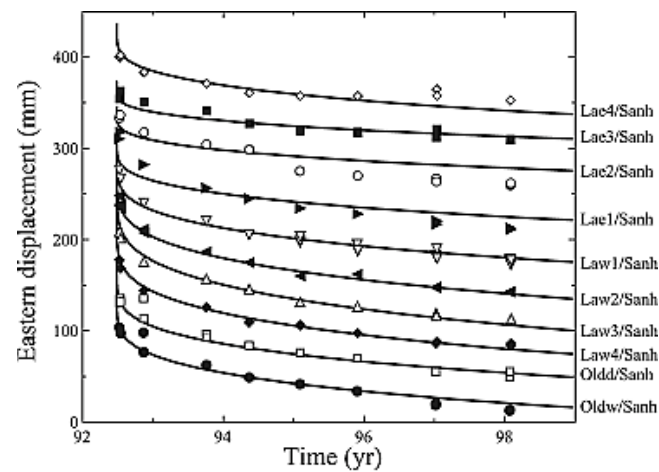
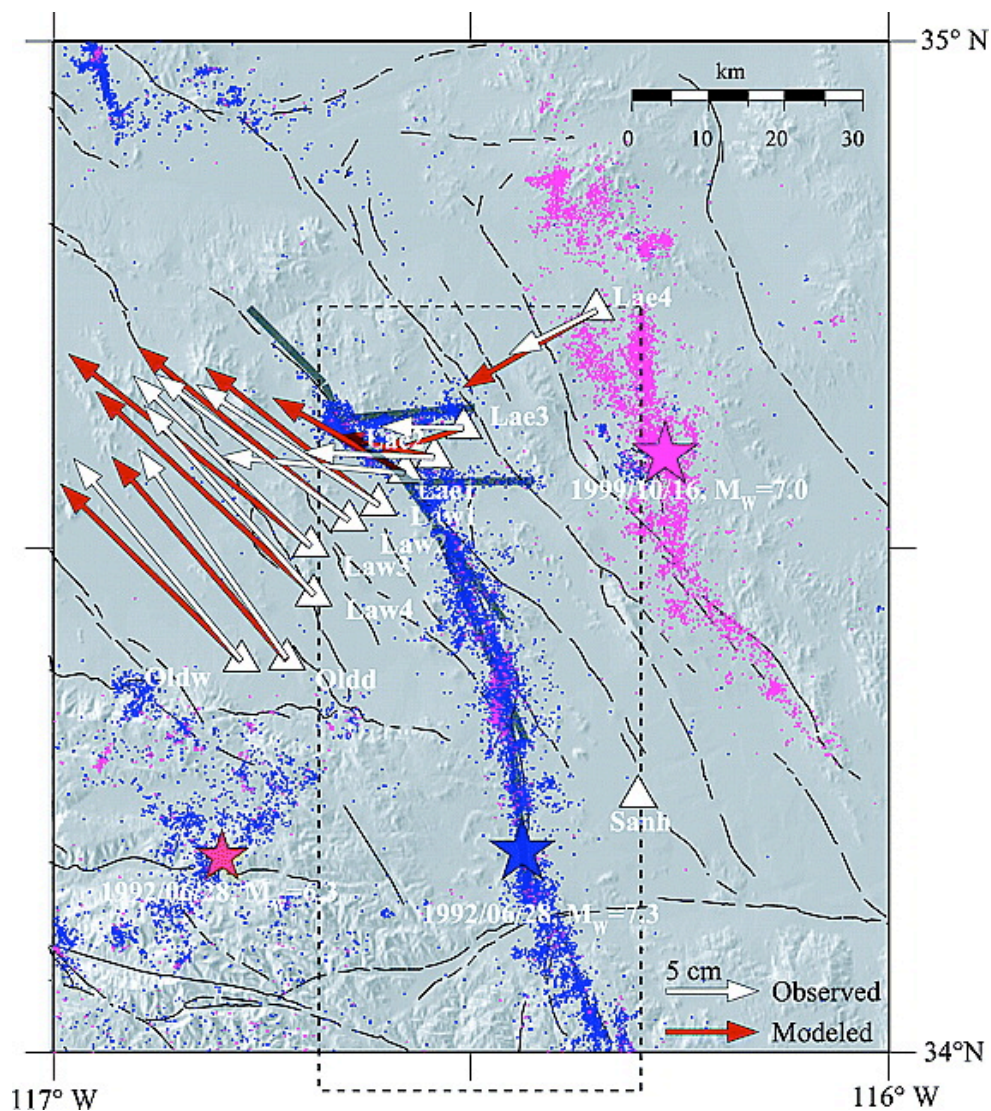
Gilles Peltzer, Paul Rosen, and Francois Rogez
Jet Propulsion Laboratory, California Institute of Technology, Pasadena

K. Hudnut
U.S. Geological Survey, Pasadena, California



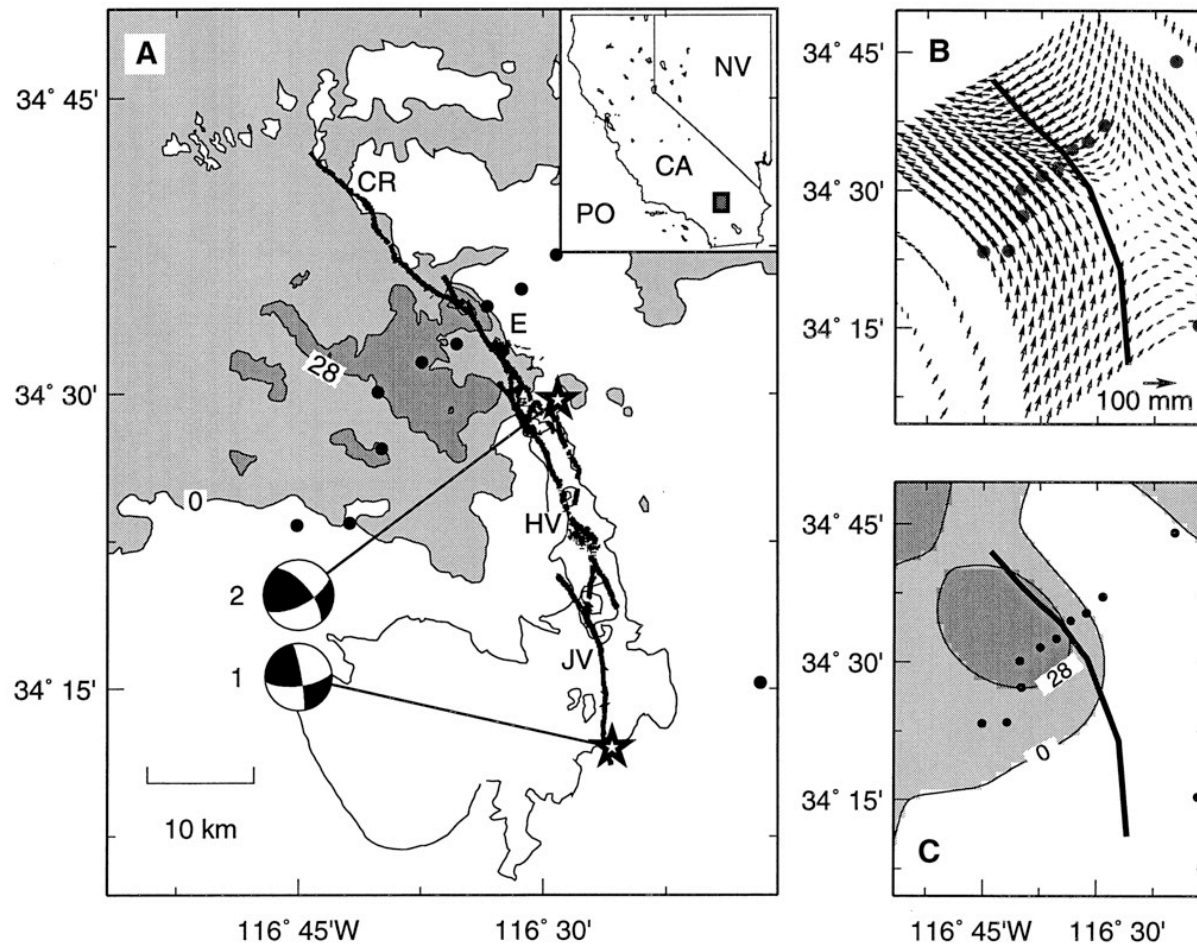
Modeling afterslip and aftershocks following the 1992 Landers earthquake

H. Perfettini¹ and J.-P. Avouac²



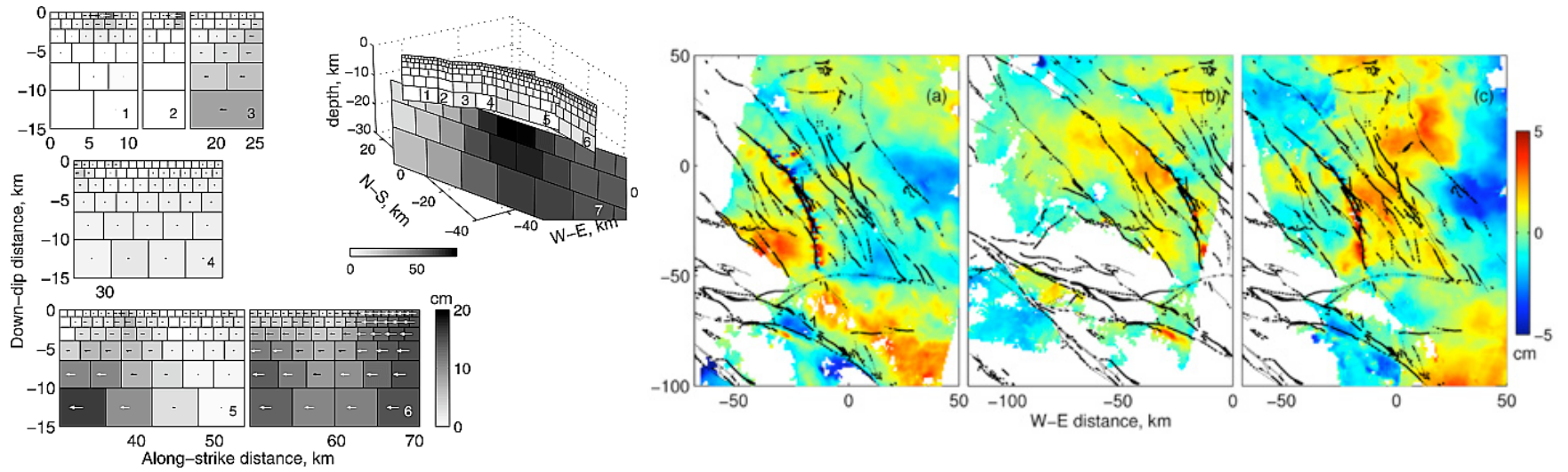
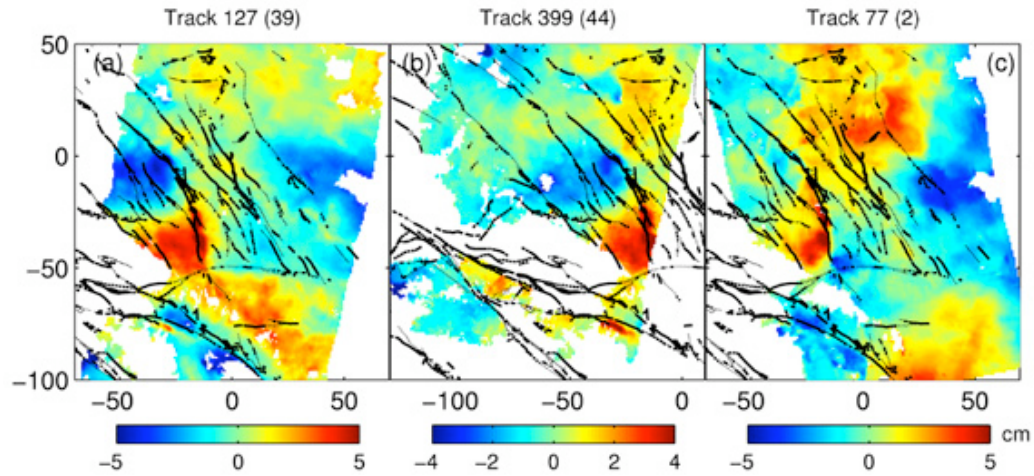
Viscoelastic Flow in the Lower Crust after the 1992 Landers, California, Earthquake

Jishu Deng,* Michael Gurnis, Hiroo Kanamori, Egill Hauksson



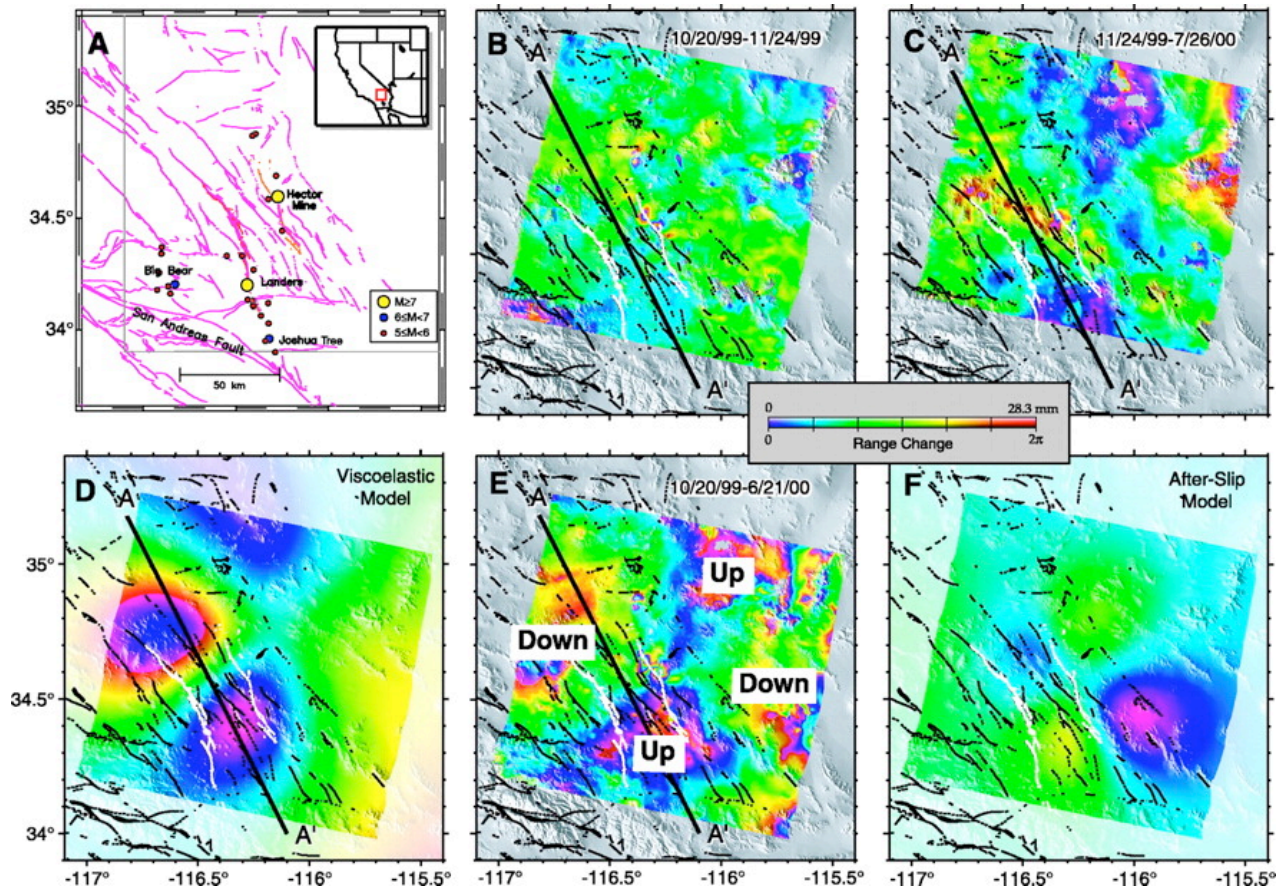
Evidence of fluid-filled upper crust from observations of postseismic deformation due to the 1992 M_w 7.3 Landers earthquake

Yuri Fialko



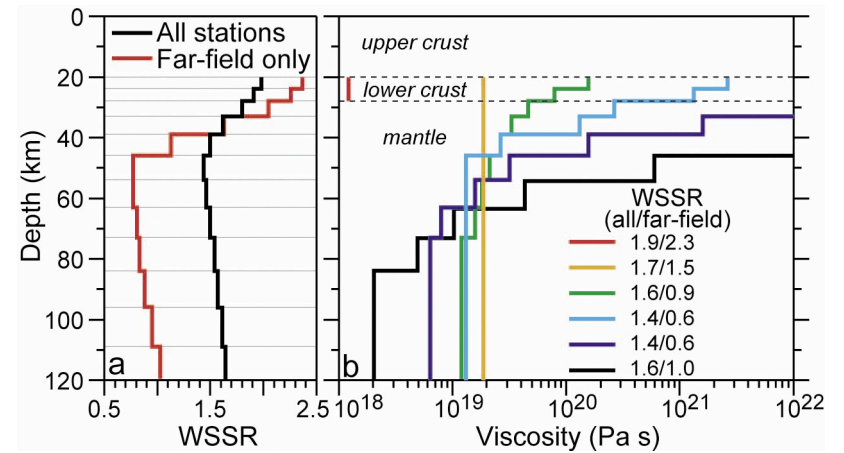
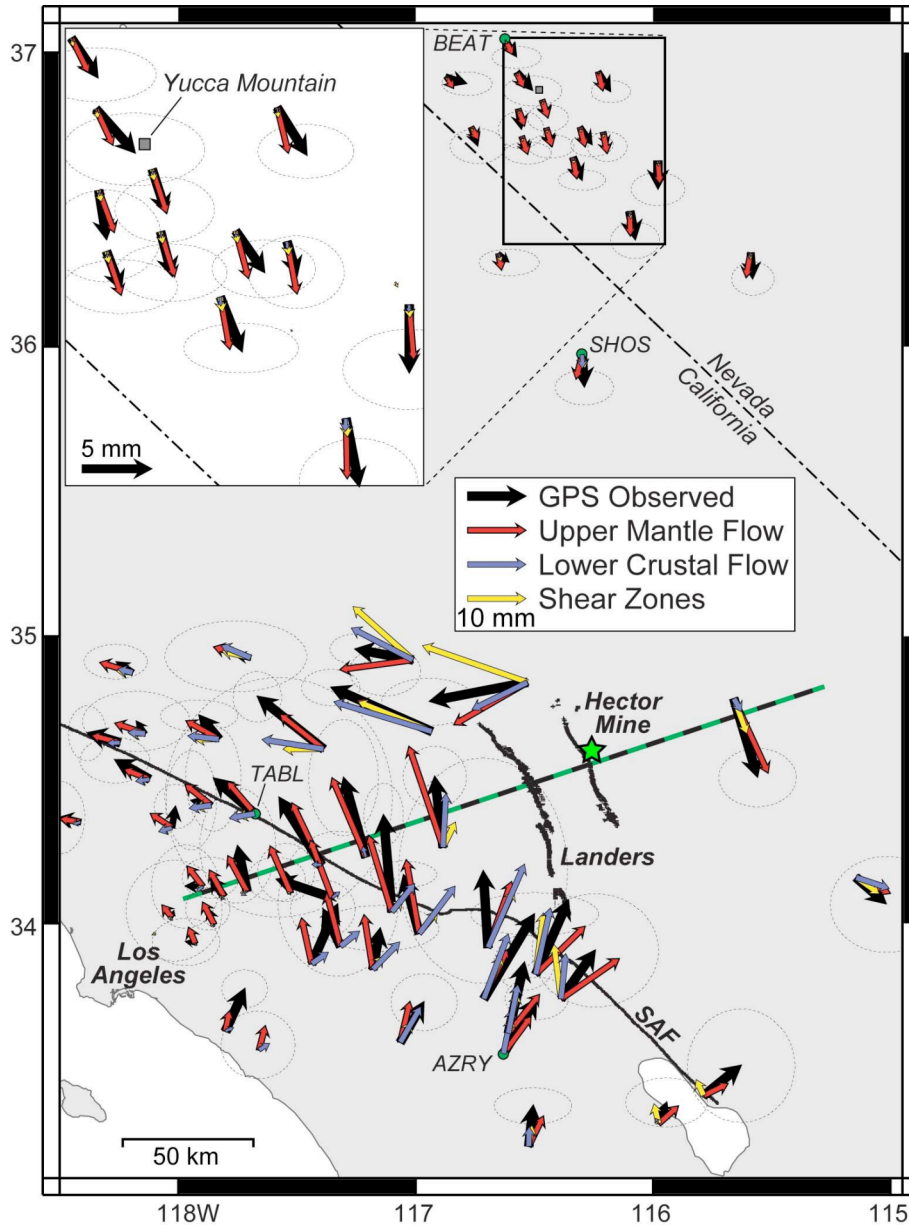
Mantle Flow Beneath a Continental Strike-Slip Fault: Postseismic Deformation After the 1999 Hector Mine Earthquake

Fred F. Pollitz,* Chuck Wicks, Wayne Thatcher



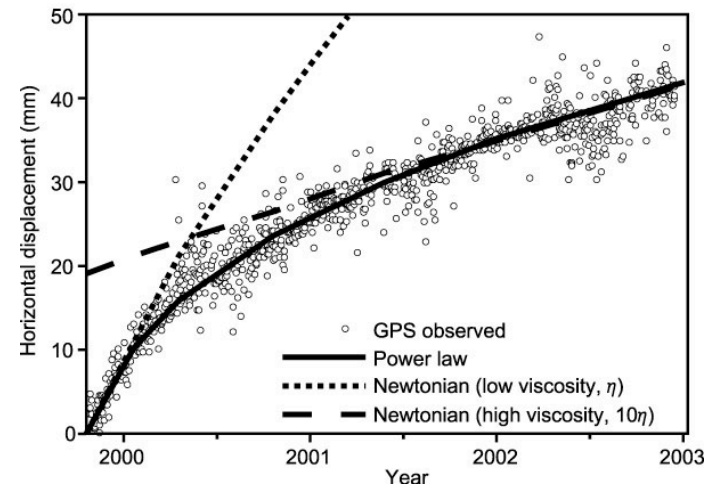
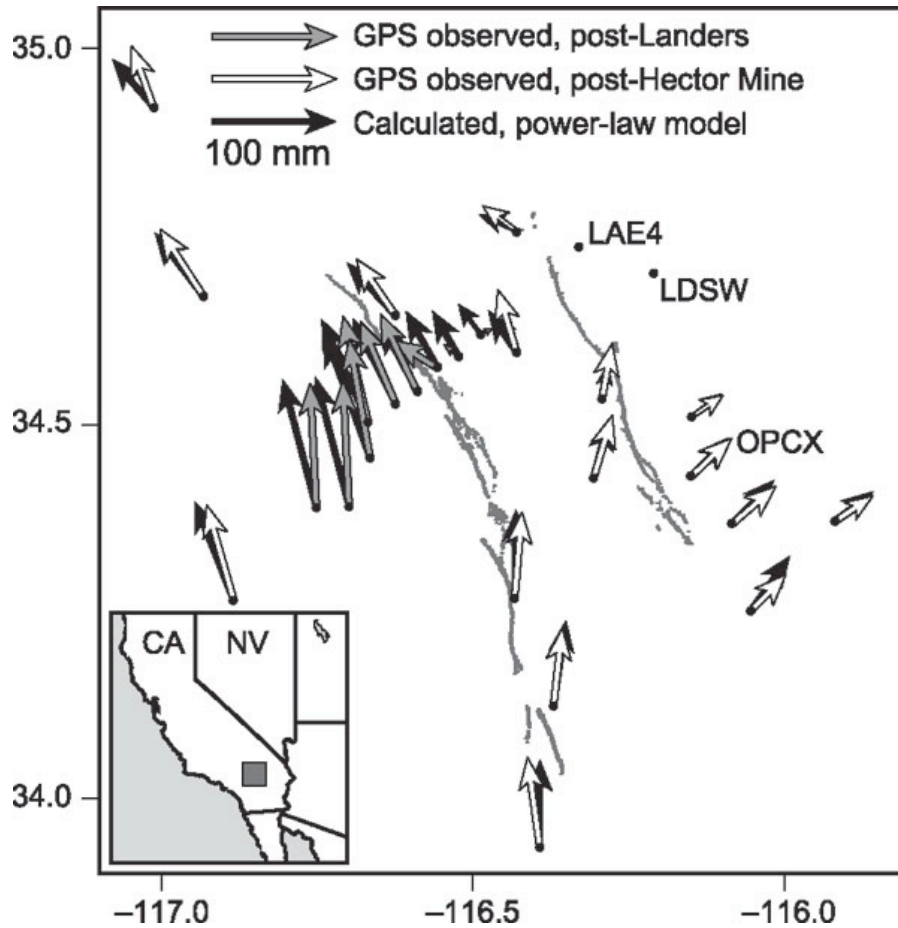
Far-reaching transient motions after Mojave earthquakes require broad mantle flow beneath a strong crust

Andrew M. Freed,¹ Roland Bürgmann,² and Thomas Herring³



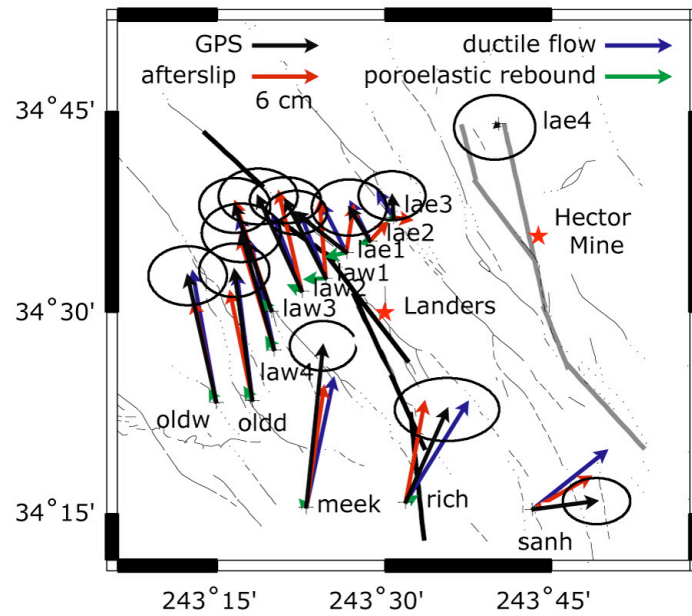
Evidence of power-law flow in the Mojave desert mantle

Andrew M. Freed¹ & Roland Bürgmann²

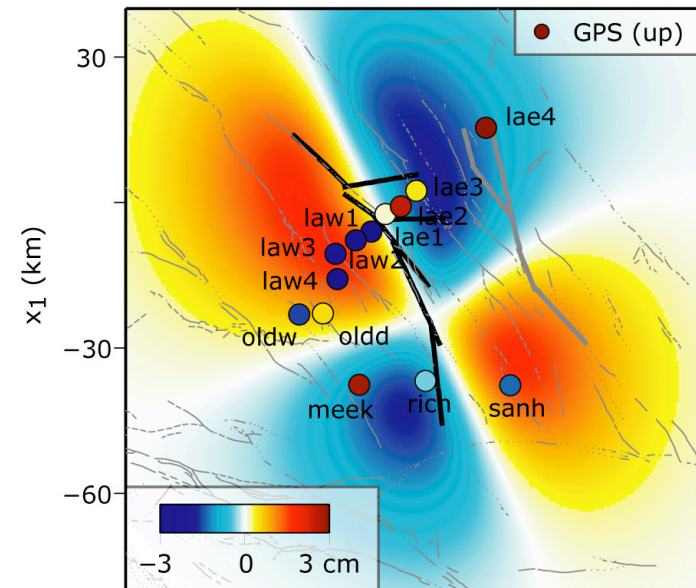


Time dependence of post Hector Mine GPS displacements favors a **nonlinear** ductile rheology.

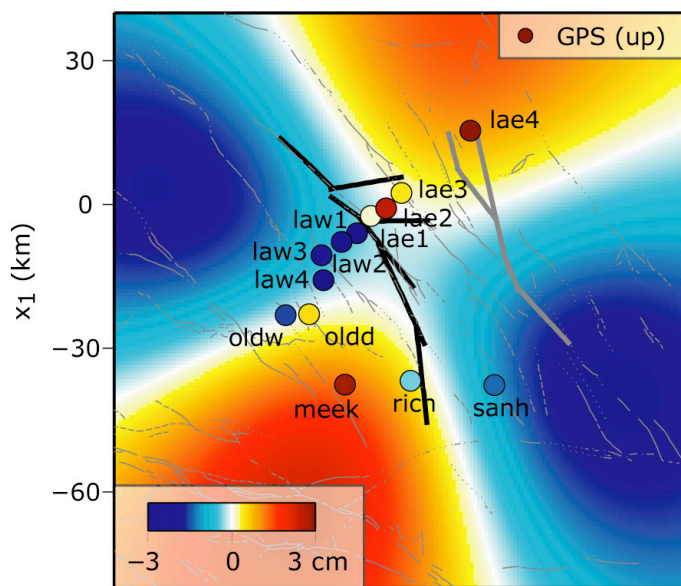
A. GPS and modeled horizontal displacements



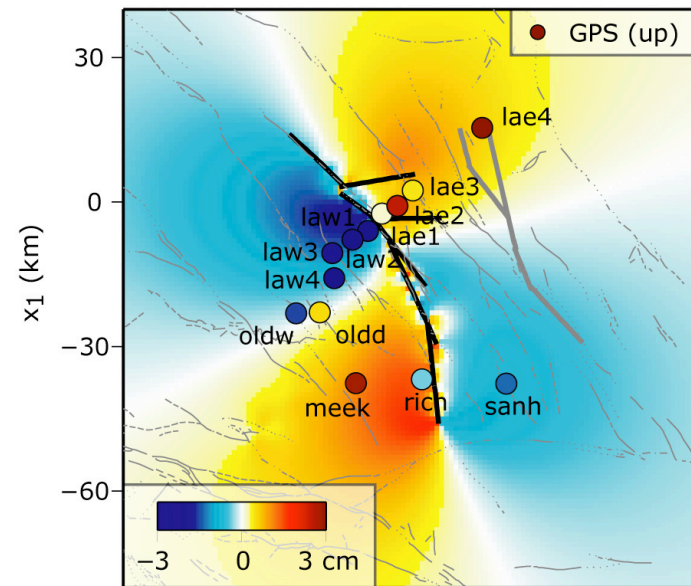
B. Afterslip model $h = 15$ km



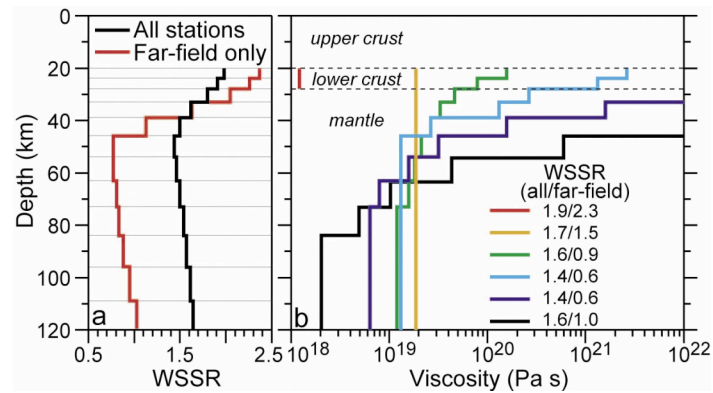
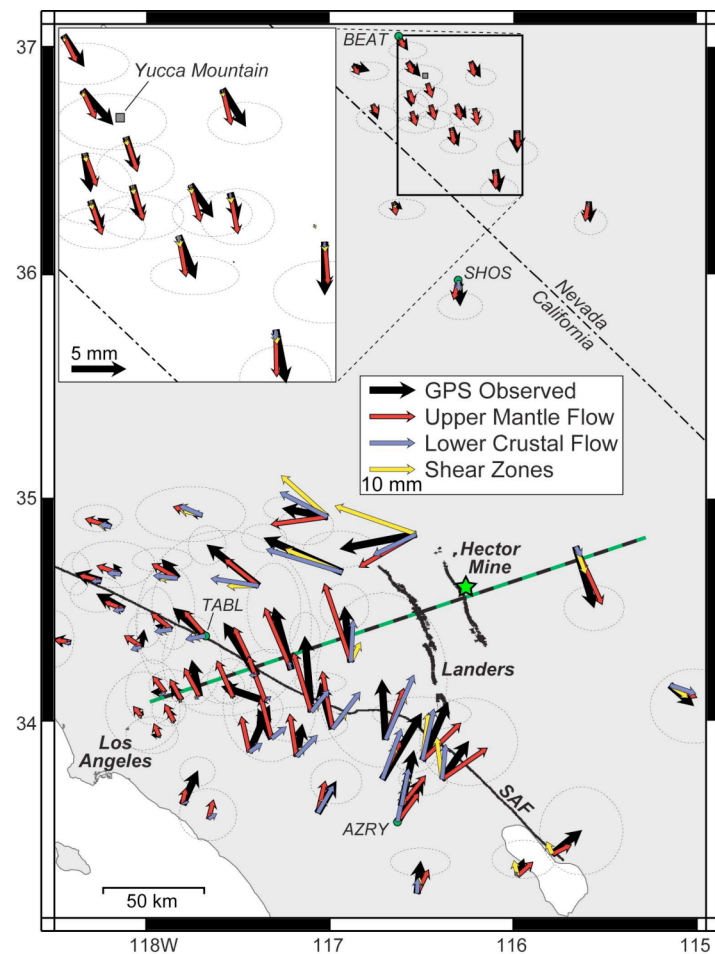
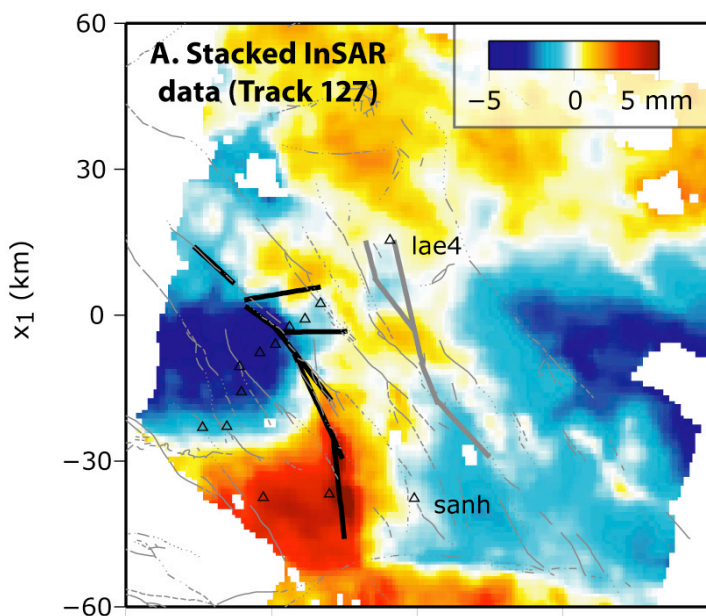
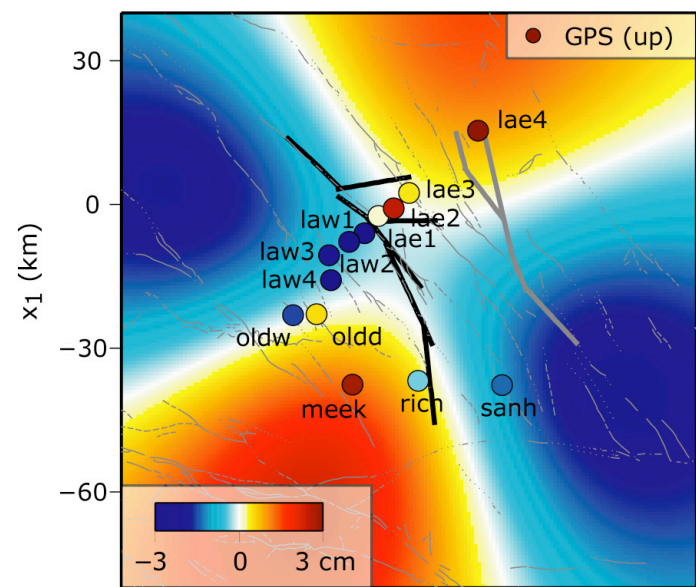
C. Crème brûlée linear model $H = 40$ km



D. Poroelastic rebound model



C. Crème brûlée linear model H = 40 km



Outlines

- Design of the linear inverse problem
- Models of post-Landers deformation with InSAR data
 - afterslip transitioning to viscous flow
 - poroelastic rebound & viscous flow
 - viscoelastic flow alone
- Resolution of geodetic data
- Models of post-Hector Mine deformation with InSAR and GPS data
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- Lateral variations in viscosity
- Conclusions

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Design of inverse problem: the rheology

- Aseismic creep rheology: rate-strengthening friction

$$\dot{s} = 2\dot{s}_0 \sinh \frac{\tau}{a\sigma}$$

$$t_c = \frac{a\sigma}{\dot{s}_0} \frac{L}{G}$$

- Viscoelastic flow: power-law rheology

$$\dot{\varepsilon} = A \left(\frac{\tau}{G} \right)^n$$

$$t_m = \frac{1}{A} \quad \text{for } n = 1$$

- Poroelastic rebound: full relaxation

$$K_d = (1 - \beta)K_u$$

no time scale

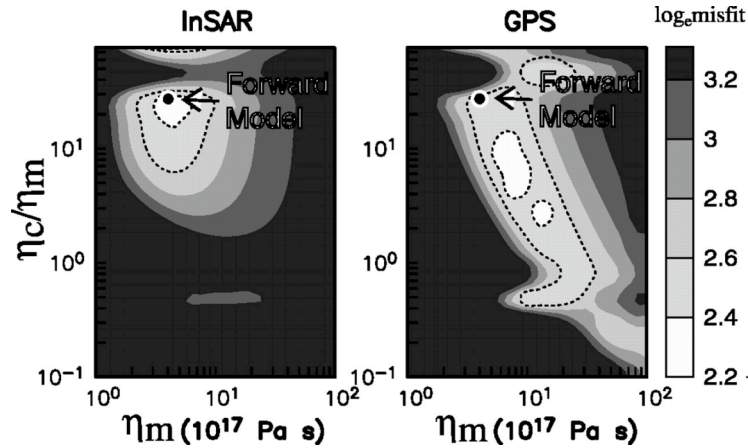
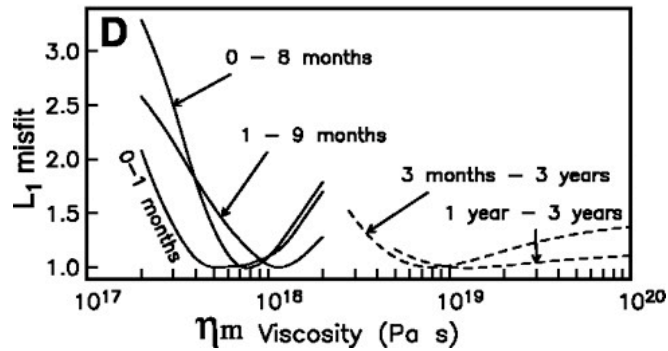
A Unified Continuum Representation of Postseismic Relaxation Mechanisms: Semi-Analytic Models of Afterslip, Poroelastic Rebound and Viscoelastic Flow

Sylvain Barbot*, Yuri Fialko www.its.caltech.edu/~sbarbot/crust/

Design of inverse problem: misfit reduction by exploration of parameter

Mantle Flow Beneath a Continental Strike-Slip Fault: Postseismic Deformation After the 1999 Hector Mine Earthquake

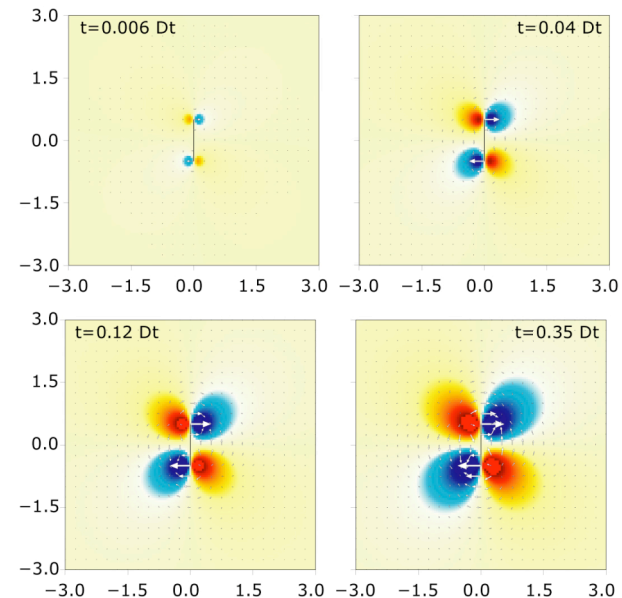
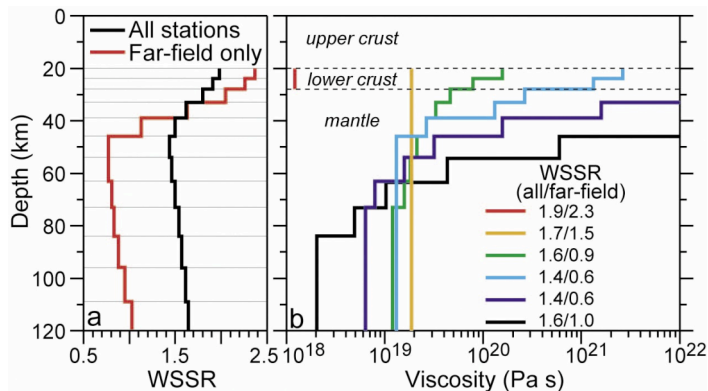
Fred F. Pollitz,* Chuck Wicks, Wayne Thatcher



Pore fluid diffusion:
not time-space separable

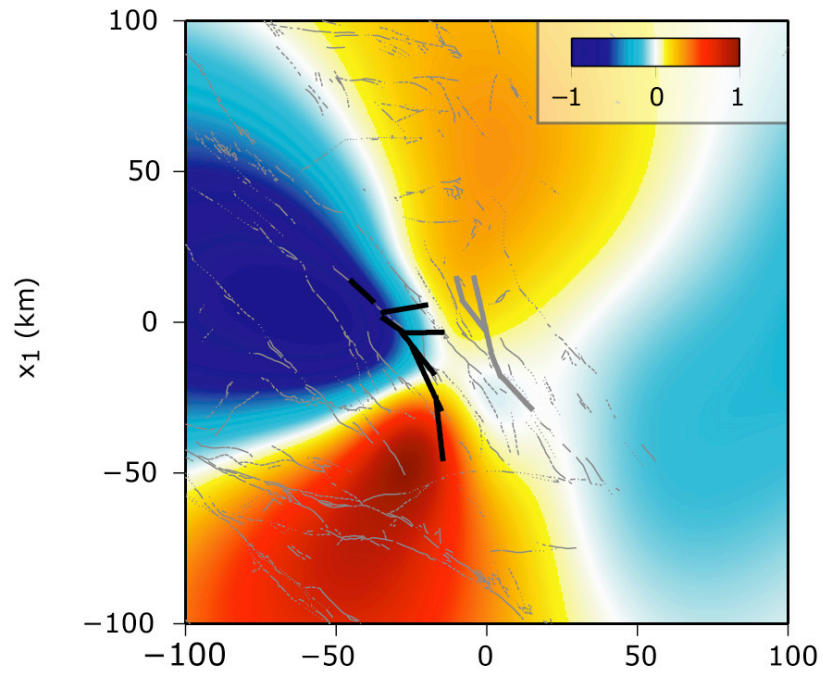
Far-reaching transient motions after Mojave earthquakes require broad mantle flow beneath a strong crust

Andrew M. Freed,¹ Roland Bürgmann,² and Thomas Herring³

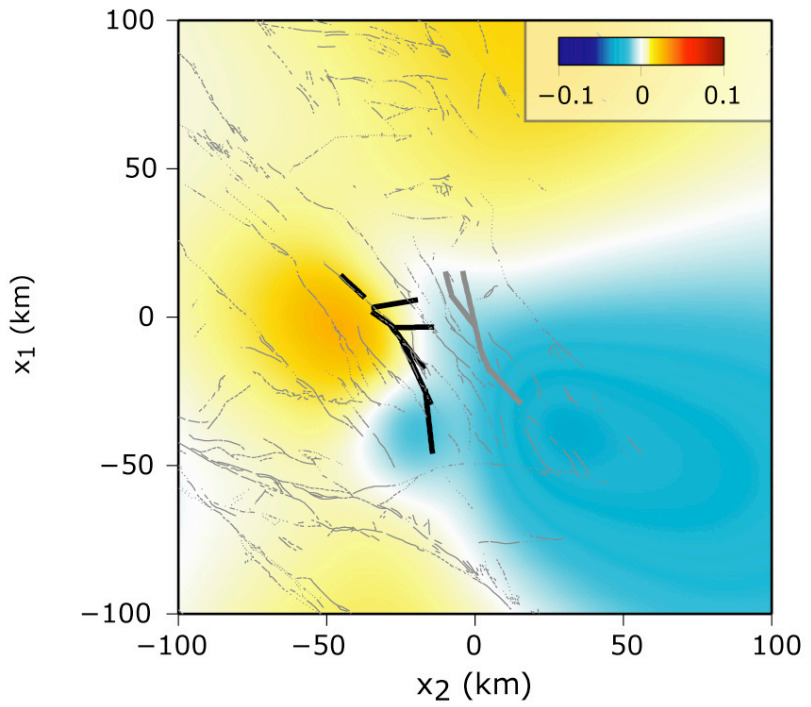


Design of inverse problem: a linear solution?

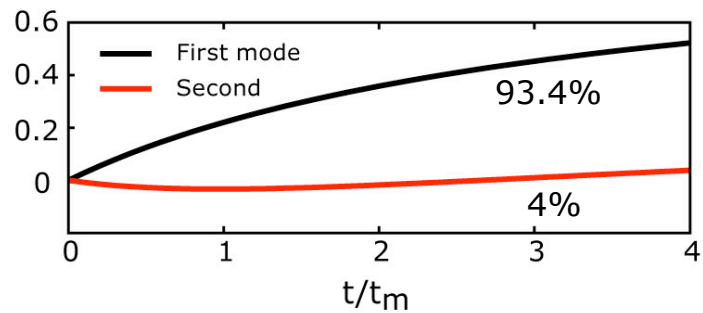
A. Dominant mode of post-Landers LOS deformation



B. Second dominant mode of post-Landers LOS deformation



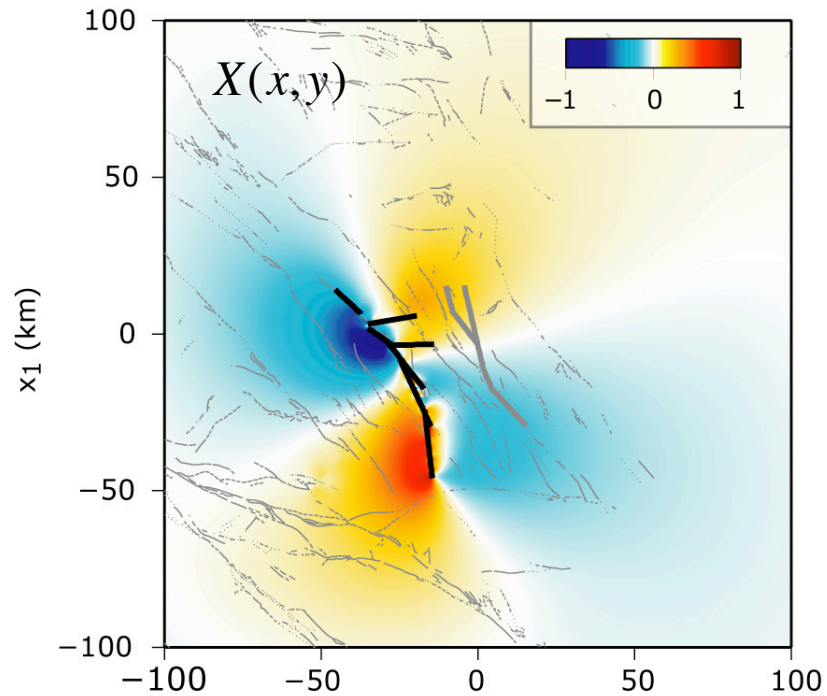
C. Time dependence of post-Landers deformation modes



Post-Landers viscoelastic relaxation in the radar line of sight (LOS) is dominated by a time-space separable signal.

Design of inverse problem: a linear solution?

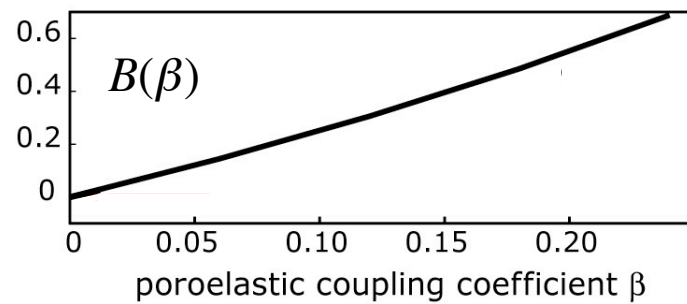
D. Dominant mode of poroelastic LOS deformation



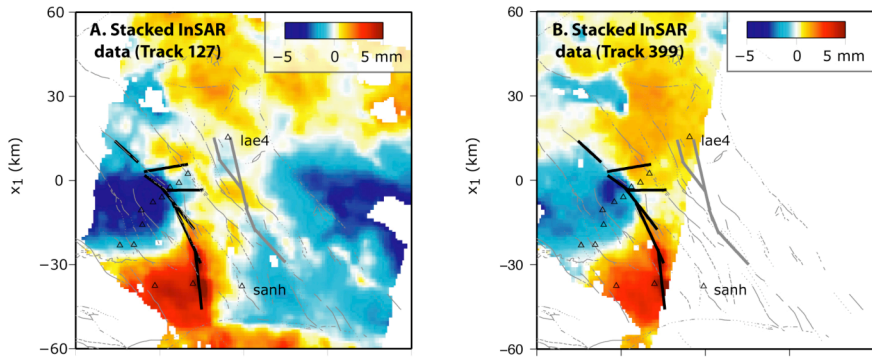
Full poroelastic rebound is separable in amplitude and spatial distribution.

$$LOS(x, y; \beta) = B(\beta)X(x, y)$$

F. Fluid/solid coupling dependence of modes



Design of inverse problem: a linear inverse problem



data vector

$$\mathbf{d} = \begin{bmatrix} d_1 \\ \vdots \\ d_N \end{bmatrix}$$

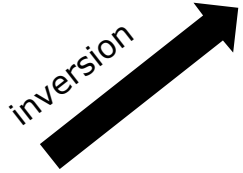
$$\mathbf{G} = \begin{bmatrix} G_{11} & \dots & \dots & \dots & \dots & G_{1M} \\ \vdots & & & & & \vdots \\ \vdots & & & & & \vdots \\ \vdots & & & & & \vdots \\ \vdots & & & & & \vdots \\ \vdots & & & & & \vdots \\ \vdots & & & & & \vdots \\ \vdots & & & & & \vdots \\ \vdots & & & & & \vdots \\ \vdots & & & & & \vdots \\ \vdots & & & & & \vdots \\ G_{N1} & \dots & \dots & \dots & \dots & G_{NM} \end{bmatrix}$$

response of a nominal flow in horizon i



$$\mathbf{m} = \begin{bmatrix} m_1 \\ \vdots \\ m_M \end{bmatrix}$$

amplitude of deformation for horizon i



minimize the misfit

$$\chi = \|\mathbf{d} - \mathbf{G}\mathbf{m}\|$$

with non-negativity constraint

$$\mathbf{A}\mathbf{m} \geq 0$$

and regularization

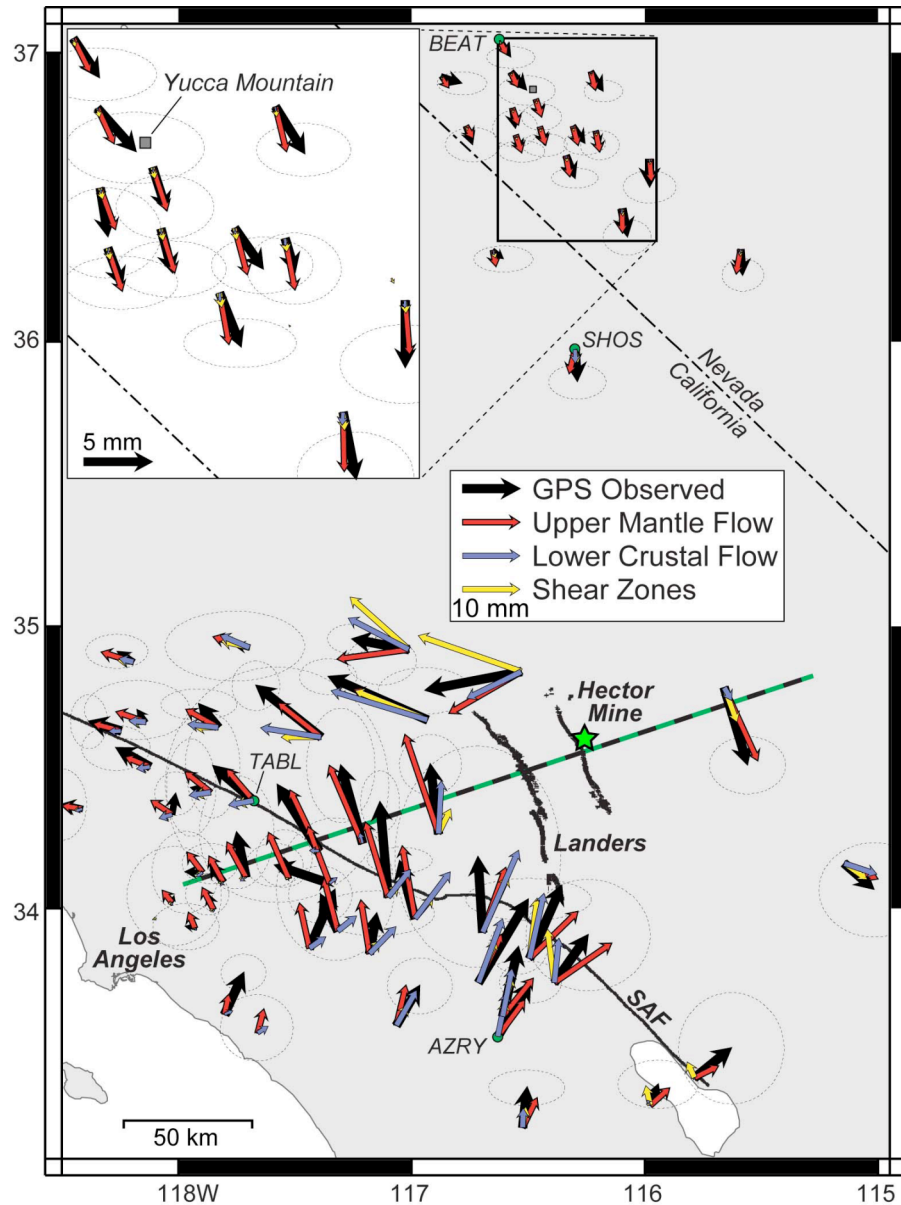
$$\lambda^2 \mathbf{D}\mathbf{m} = 0$$

include a bilinear function to compensate for imprecise knowledge of orbits.

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Schizosphere model

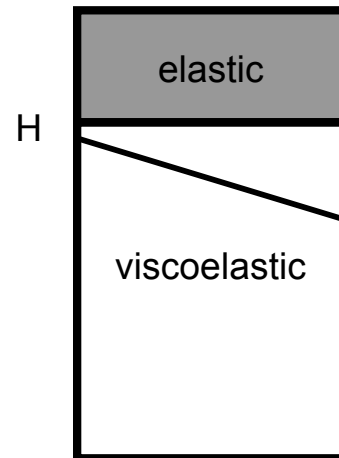


Freed et al., 2007

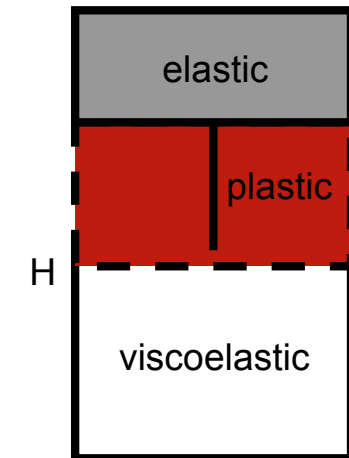
Displacement on far-field Nevada GPS stations requires **deep sources** of deformation.

How deep is the viscous substrate if deformation is accommodated by **mylonitic shear** in the **schizosphere**?

Crème-brûlée model



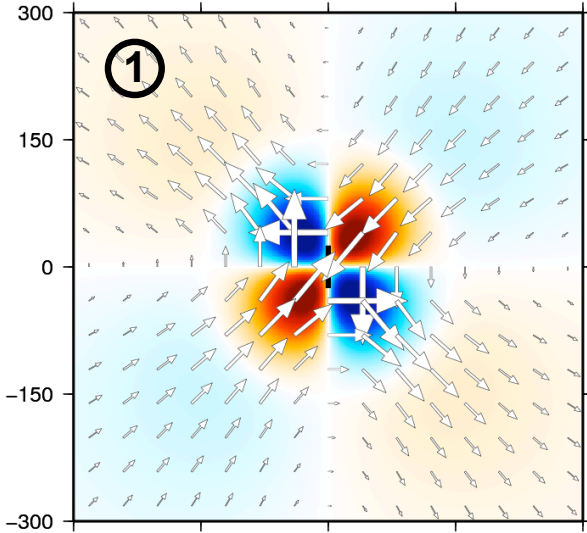
schizosphere model



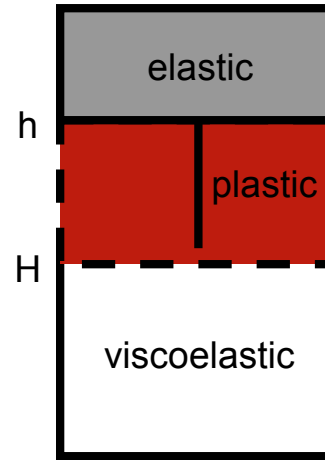
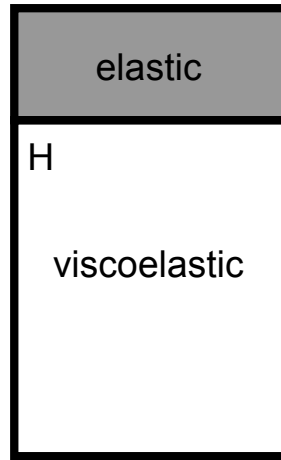
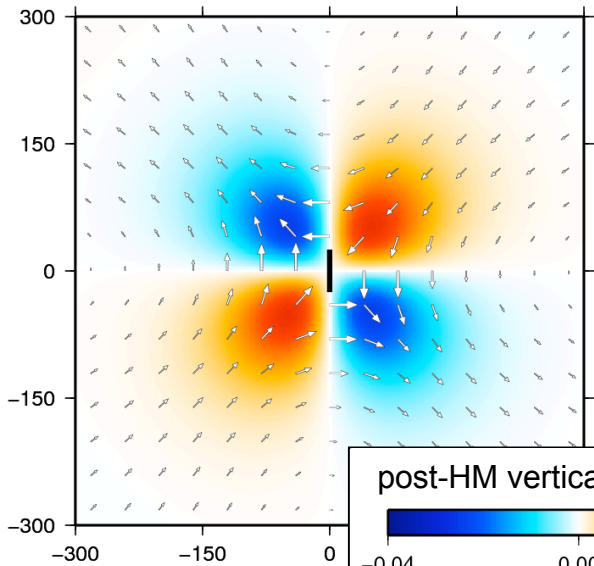
Schizosphere model

crème-brûlée models

H = 30 km

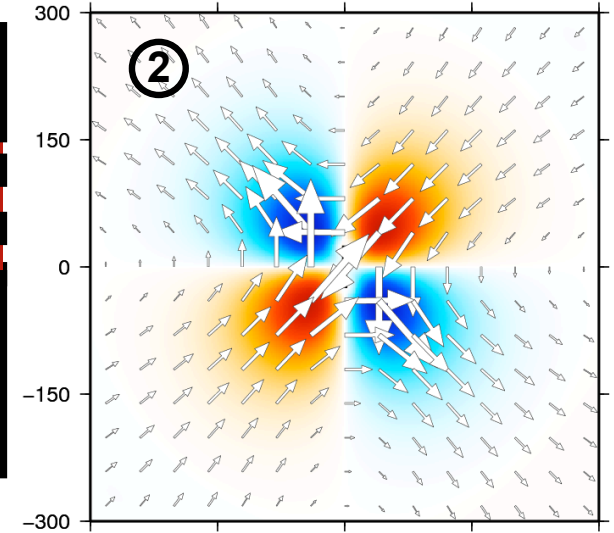


H = 50 km

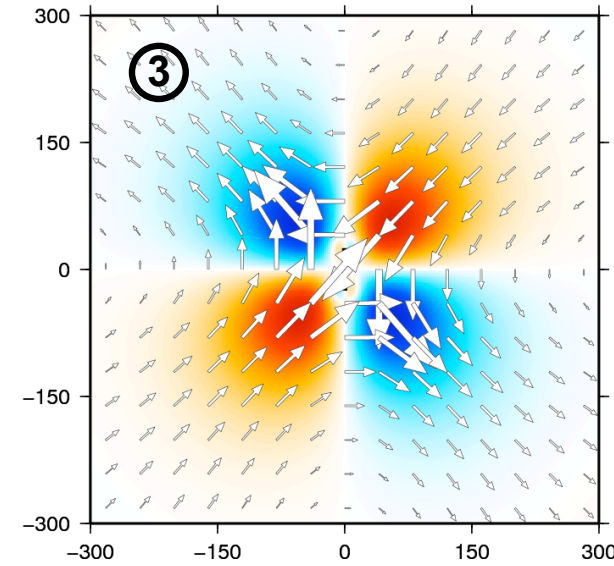


schizosphere models

h = 15 km; H = 40 km

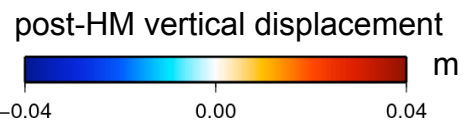


h = 15 km; H = 50 km

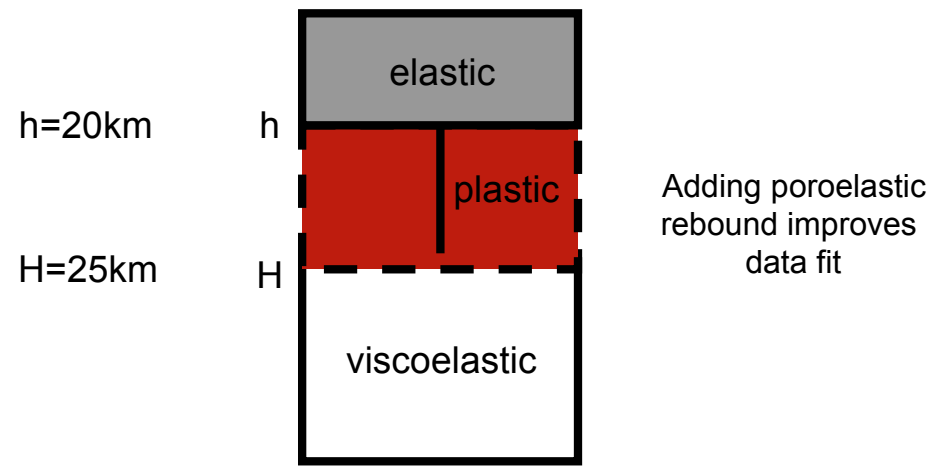
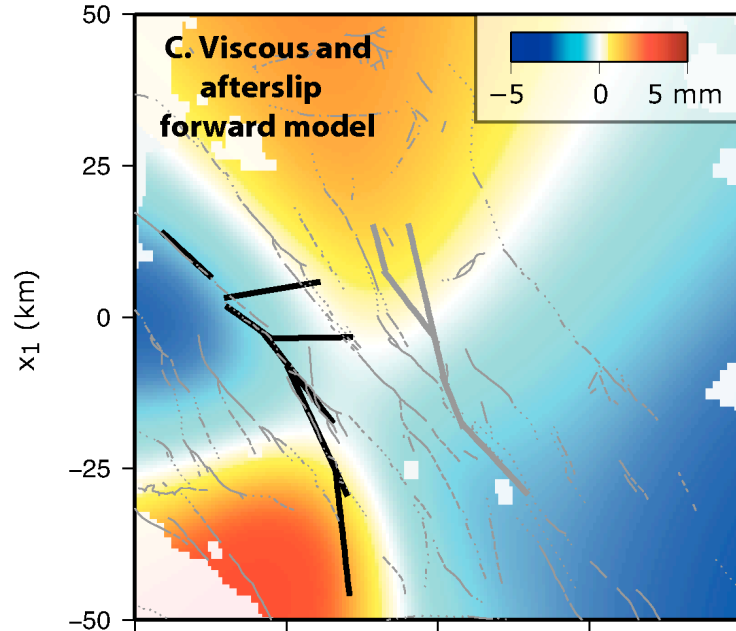
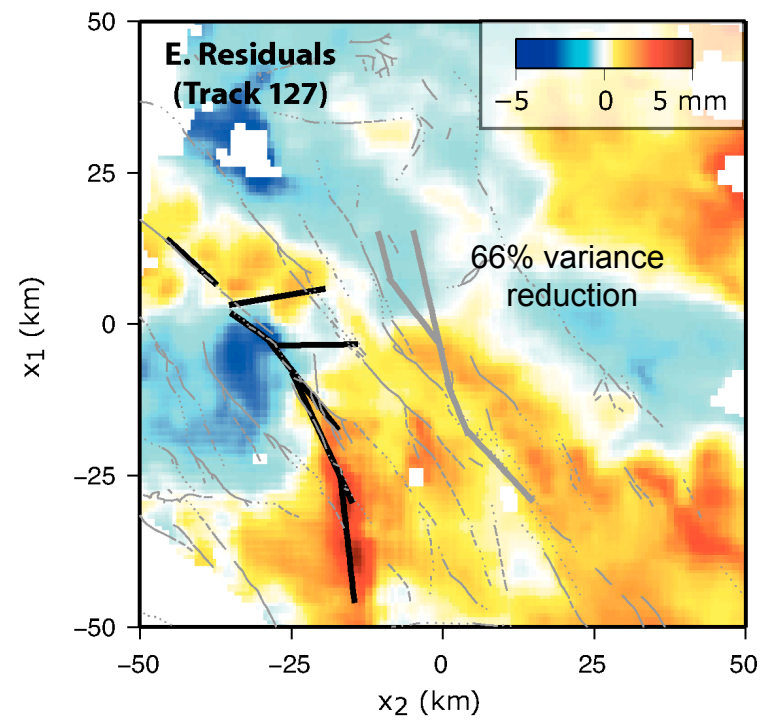
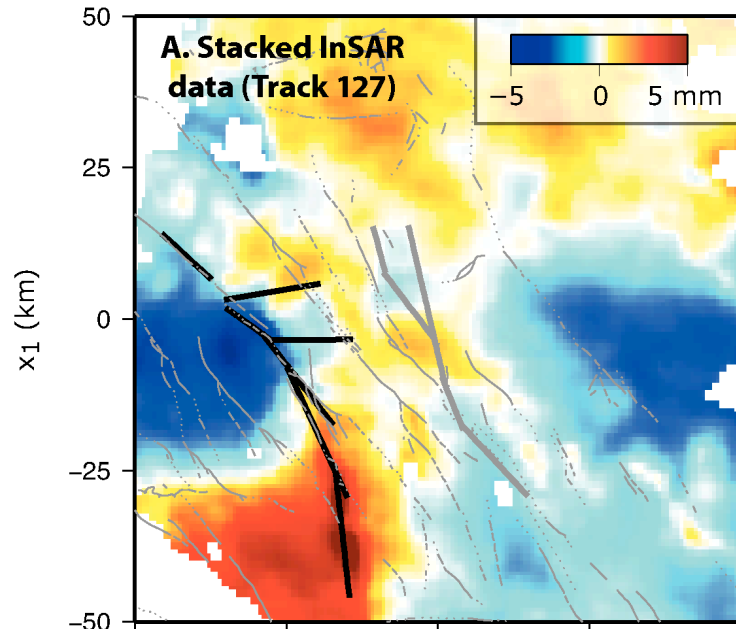


The **brittle-ductile transition** depth may be located 20 km deeper than in crème-brûlée models if shear stress is guided along **weak fault roots**.

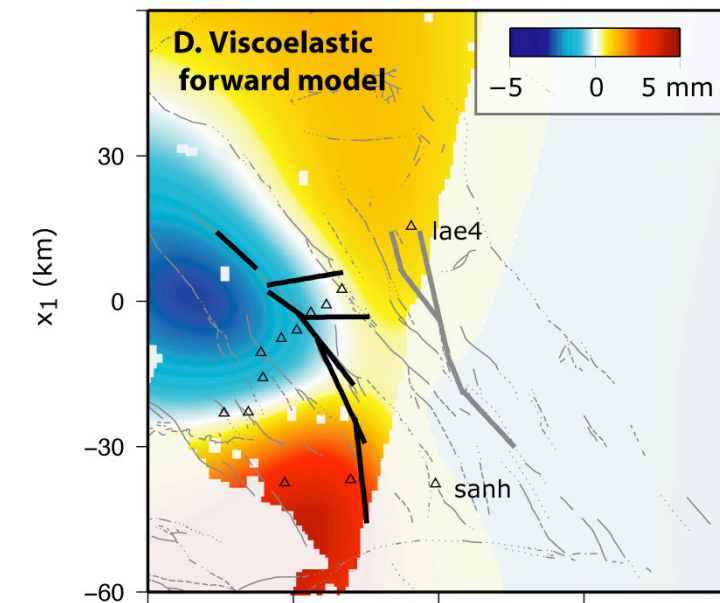
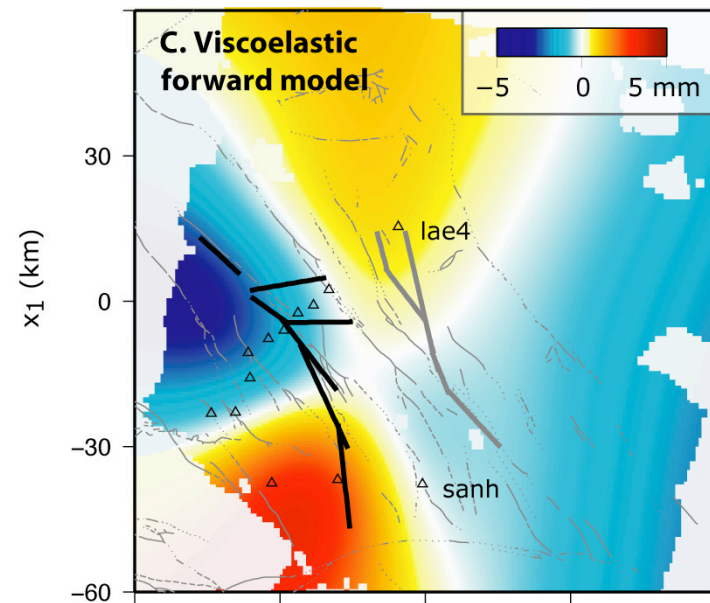
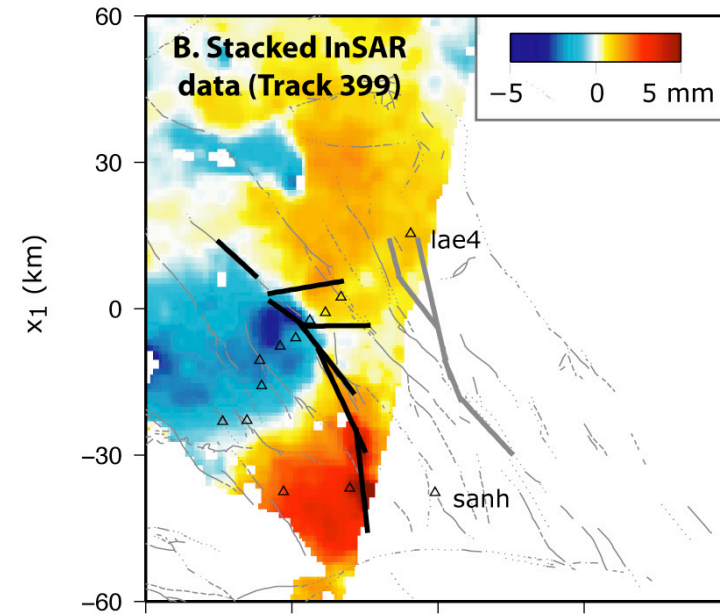
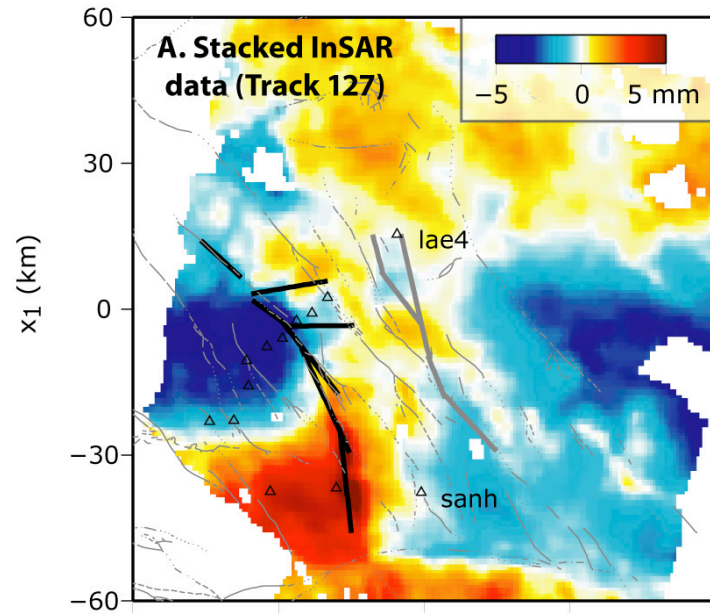
Thin **crème-brûlée** and **thick-schizosphere** models produce similar far-field horizontal displacements.



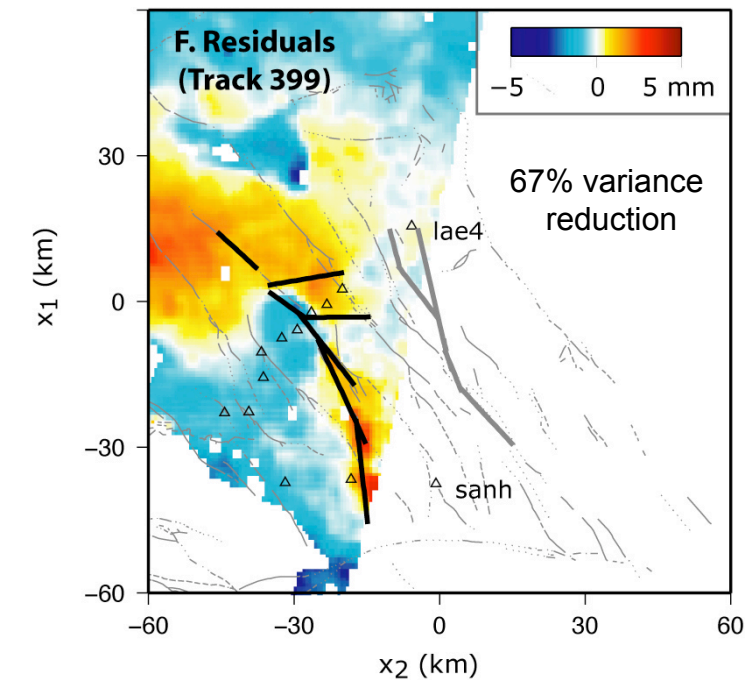
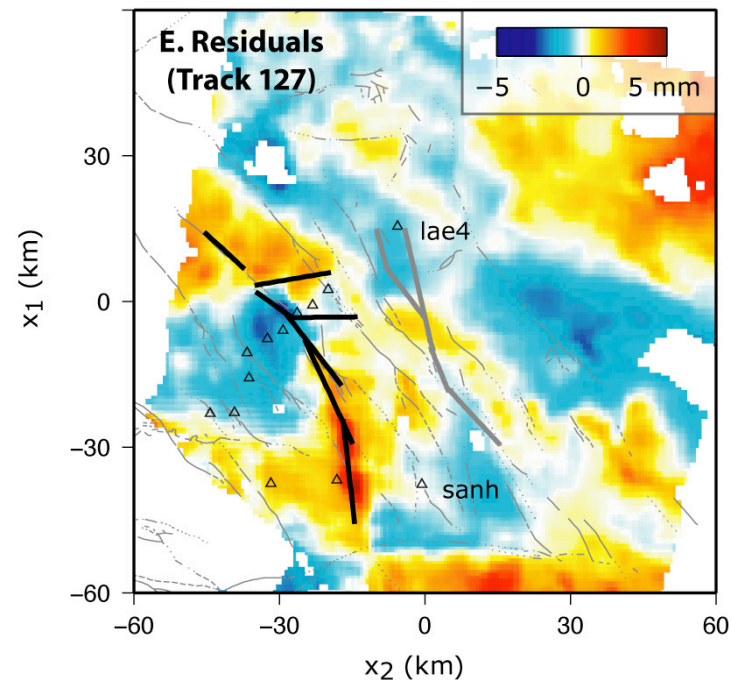
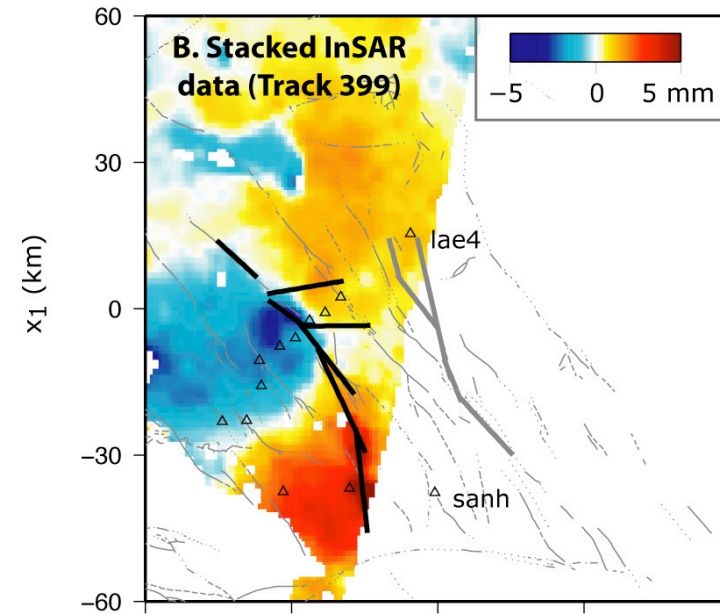
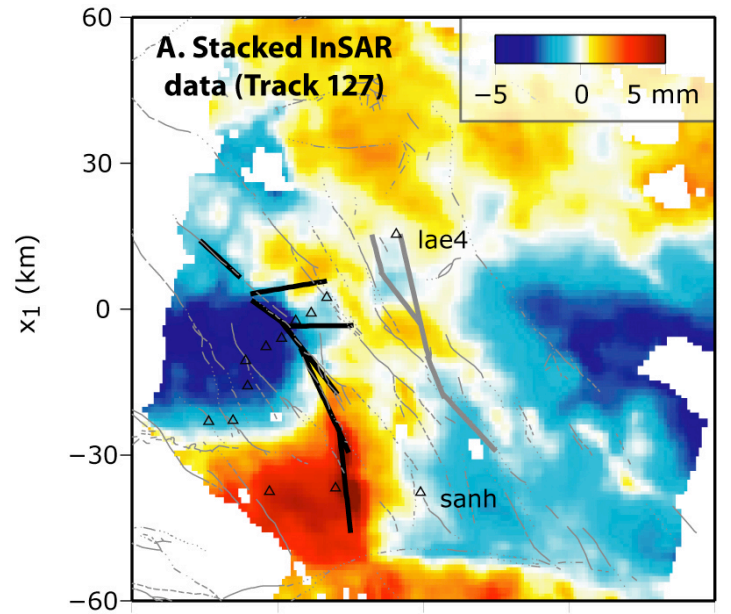
Afterslip + viscous flow model



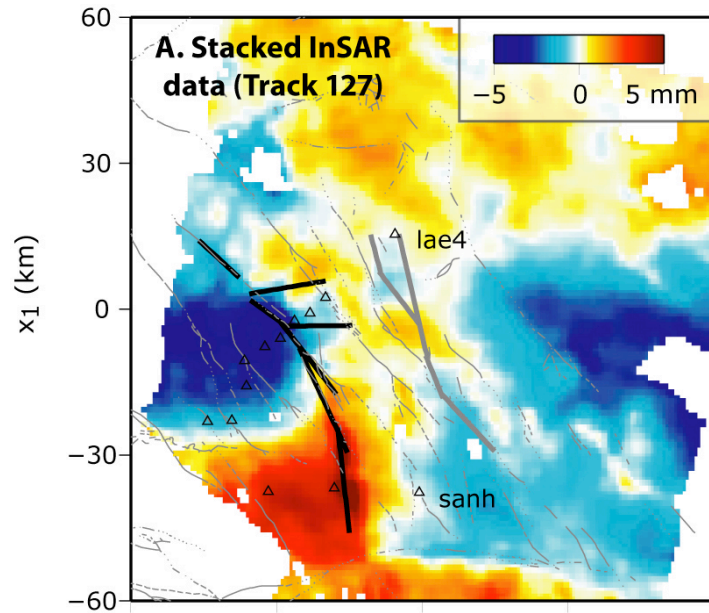
Viscous model



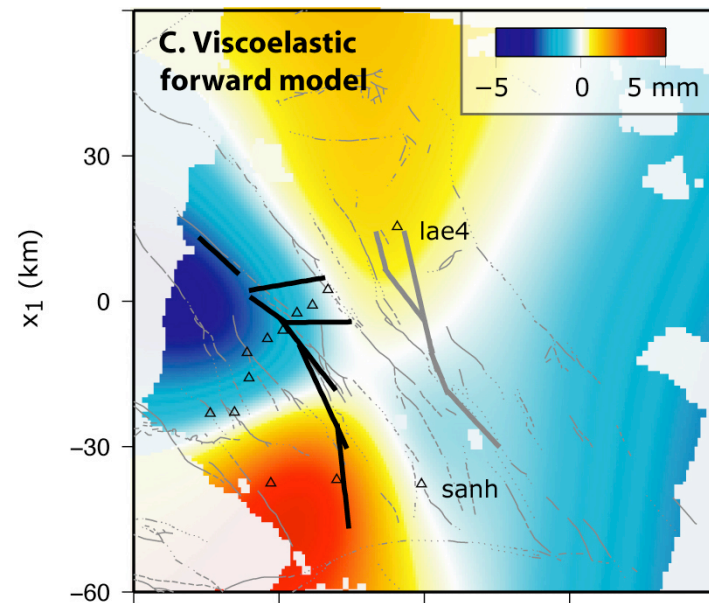
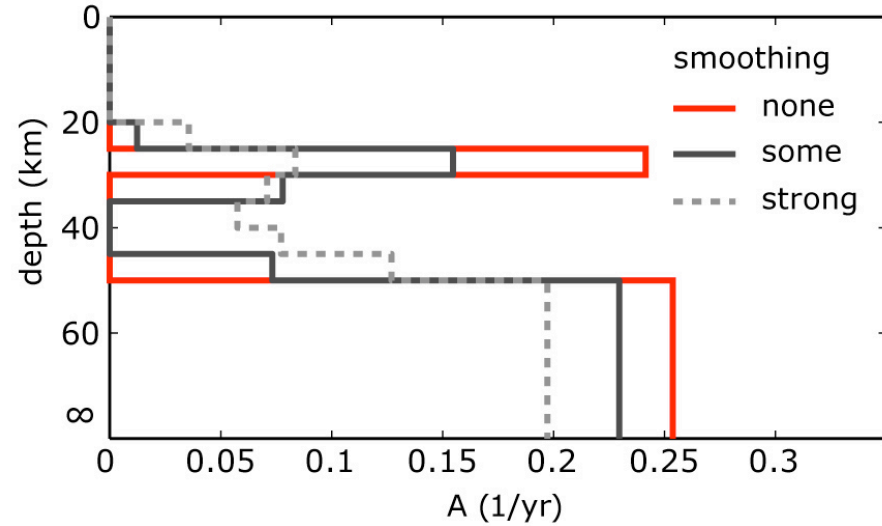
Viscous model



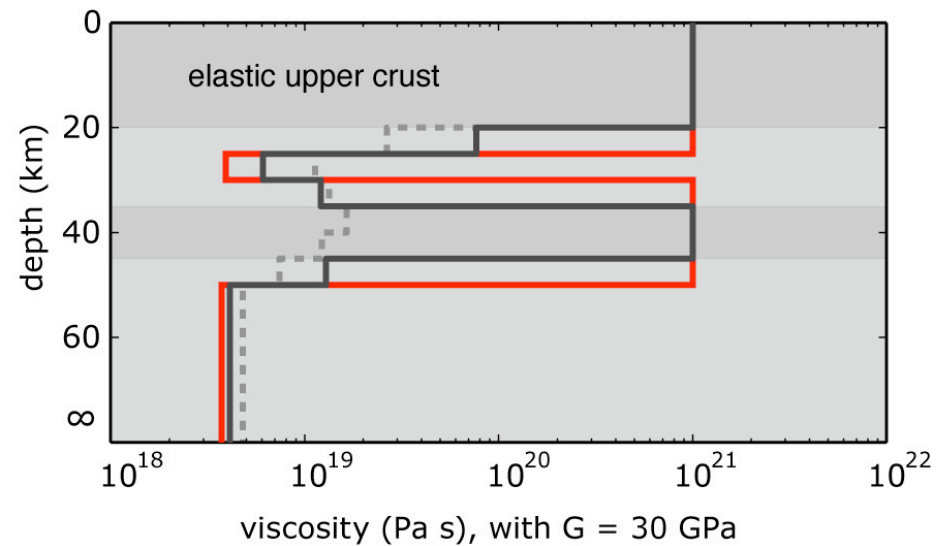
Lithosphere strength



A. Models of lithosphere fluidity from post Landers InSAR data

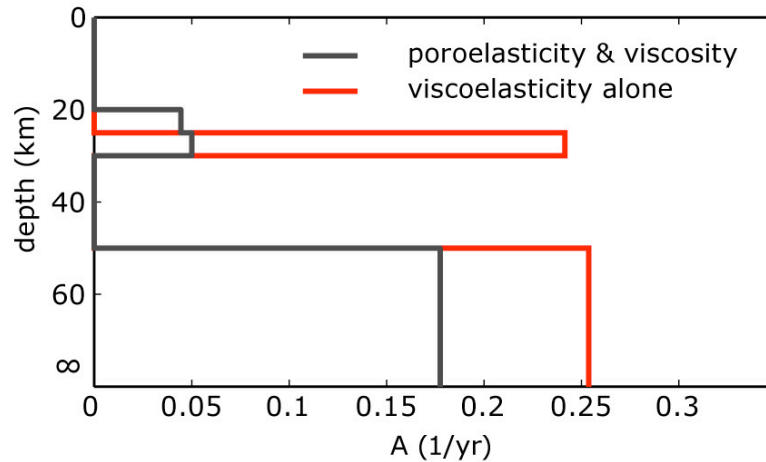


B. Inferred viscosity profile



Lithosphere strength, effect of poroelasticity

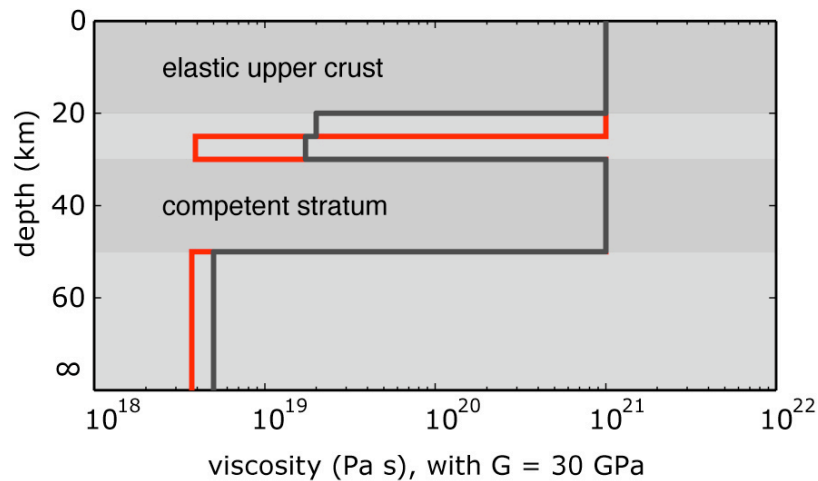
A. Influence of poroelasticity on inferred fluidity



Joint poro- and viscoelastic model explains 71% of data

viscoelastic model explains 67% of data

B. Inferred viscosity profile (post-Landers InSAR data)



stratification of ductile layers is unaffected

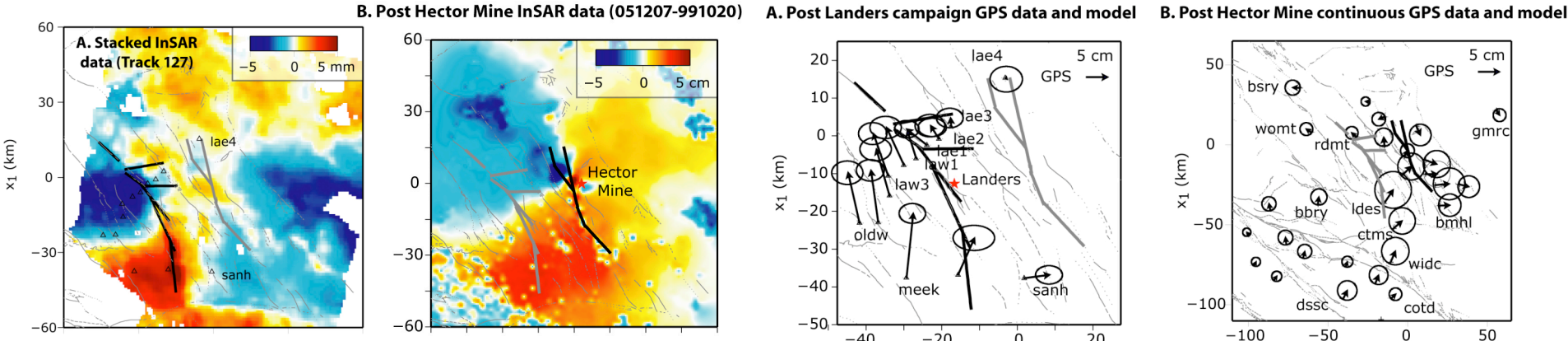
Conclusions on Post-Landers modeling

- Preferred model is a combination of poroelastic rebound and viscoelastic flow with 71% variance reduction (VR)
- Second best model is viscoelastic flow alone (67% VR)
- A combination of afterslip and viscoelastic flow is a viable explanation of InSAR data (66% VR)
- Poroelastic rebound always improve quality of fit.
- Viscous flow likely takes place in two separate horizons, one between 25 and 30km depth another below 50km depth. Location of top layer may be biased up by the presence of afterslip.

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- **Resolution of geodetic data**
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Design of inverse problem: Landers & Hector Mine data set



data vector

response of a nominal flow in horizon i

$$\mathbf{d} = \begin{bmatrix} d_1 \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ d_N \end{bmatrix}$$

$$\mathbf{G} = \begin{bmatrix} G_{11} & \dots & \dots & \dots & \dots & G_{1M} \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ G_{N1} & \dots & \dots & \dots & \dots & G_{NM} \end{bmatrix}$$

$$\mathbf{m} = \begin{bmatrix} m_1 \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ m_M \end{bmatrix}$$

horizon i

Fit GPS time series

$$d(t) = m_1 + m_2(t - t_0) + m_3(1 - e^{-t/t_m})H(t - t_0) + m_4 \cos(2\pi t) + m_5 \sin(2\pi t) + m_6 \cos(4\pi t) + m_7 \sin(2\pi t)$$

Resolution of inverse problem: InSAR vs. GPS

spectral decomposition of the design matrix

$$\mathbf{G} = \mathbf{U}\mathbf{\Lambda}\mathbf{V}'$$

the misfit function can be written

$$\chi = \|\mathbf{U}'\mathbf{d} - \mathbf{\Lambda}\mathbf{V}'\mathbf{m}\|$$

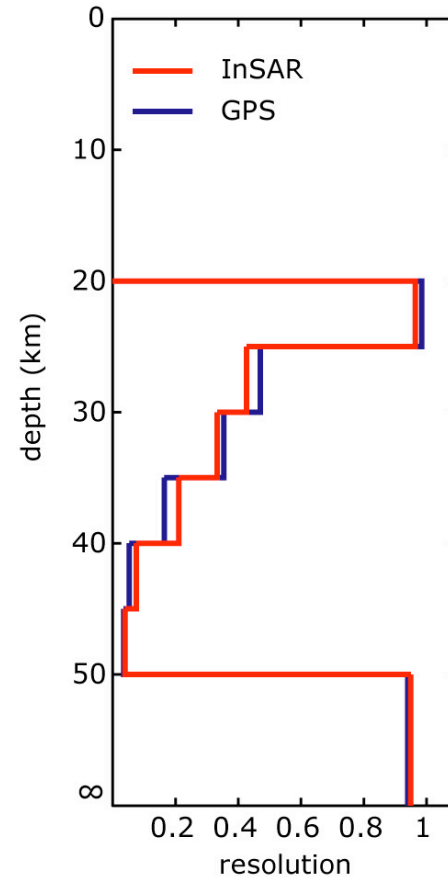
keep only large eigenvalues and define new design matrix

$$\tilde{\mathbf{G}} = \tilde{\mathbf{\Lambda}}\mathbf{V}'$$

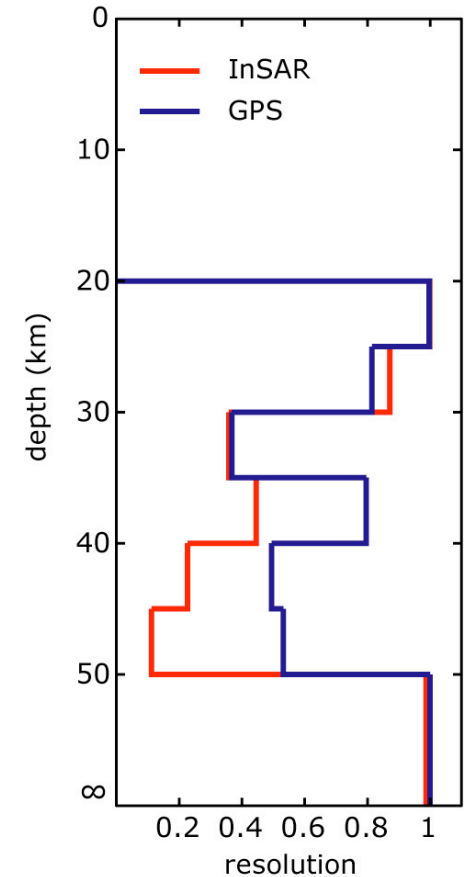
infer the resolution on model parameters

$$\mathbf{R} = \tilde{\mathbf{G}}'(\tilde{\mathbf{G}}\tilde{\mathbf{G}}')^{-1}\tilde{\mathbf{G}}$$

A. Resolution of post Landers data



B. Resolution of post HM data



N=1600 data points
M=7 parameters

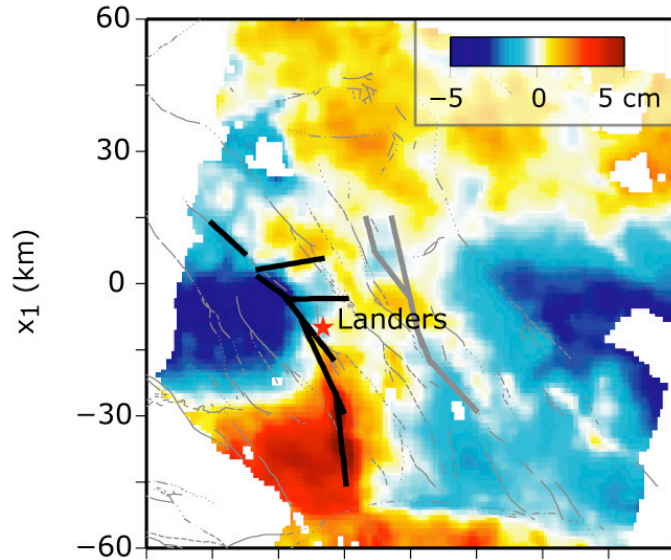


under-constrained
inverse problem

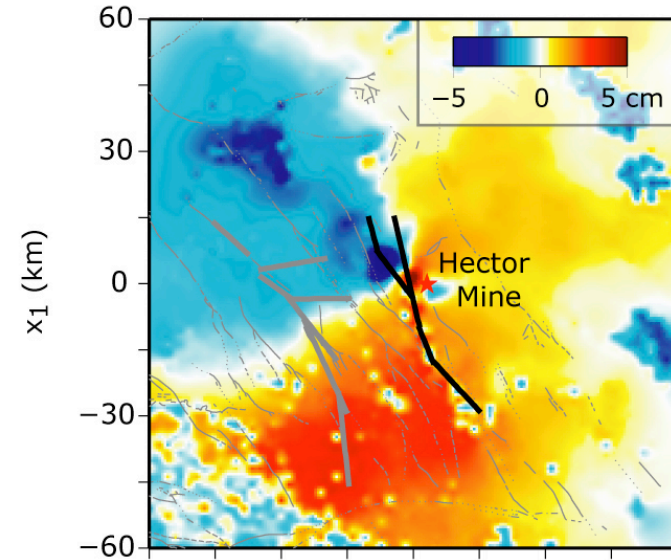
Outlines

- Design of the linear inverse problem
- Models of post-Landers deformation with InSAR data
 - afterslip transitioning to viscous flow
 - poroelastic rebound & viscous flow
 - viscoelastic flow alone
- Resolution of geodetic data
- **Models of post-Hector Mine deformation with InSAR and GPS data**
 - poroelastic rebound & viscous flow
 - viscoelastic flow alone
- Lateral variations in viscosity
- Conclusions

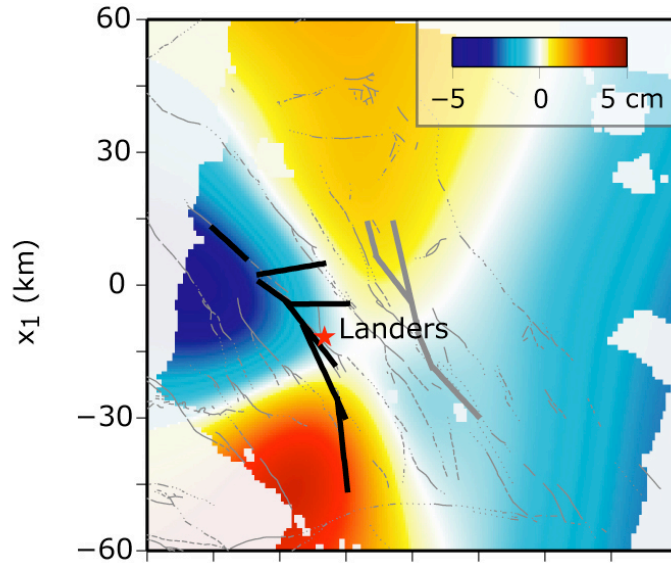
A. Stack of post Landers InSAR data (track 127)



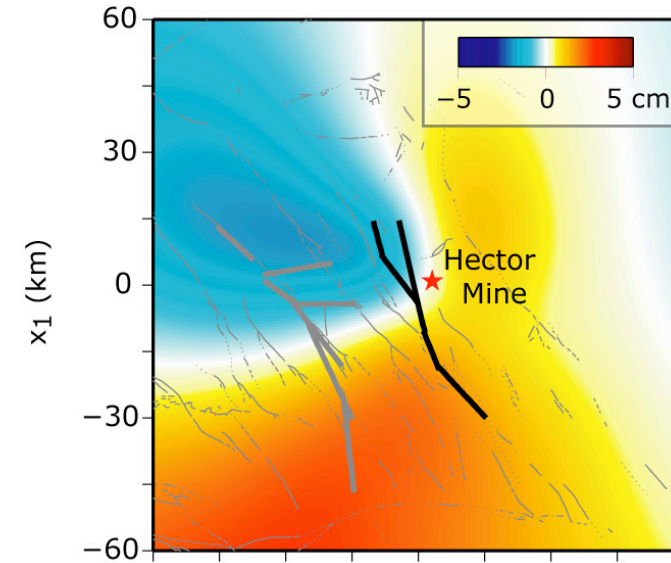
B. Post Hector Mine InSAR data (051207-991020)



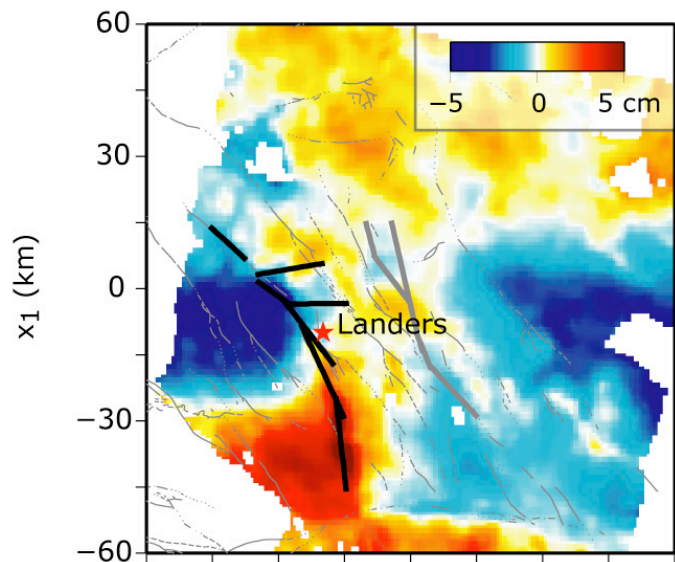
C. Viscoelastic forward model (cumulative, 7 years)



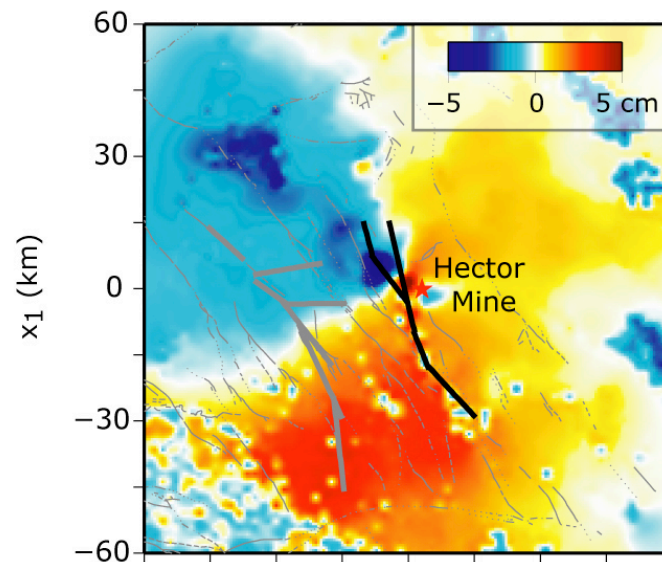
D. Viscoelastic forward model



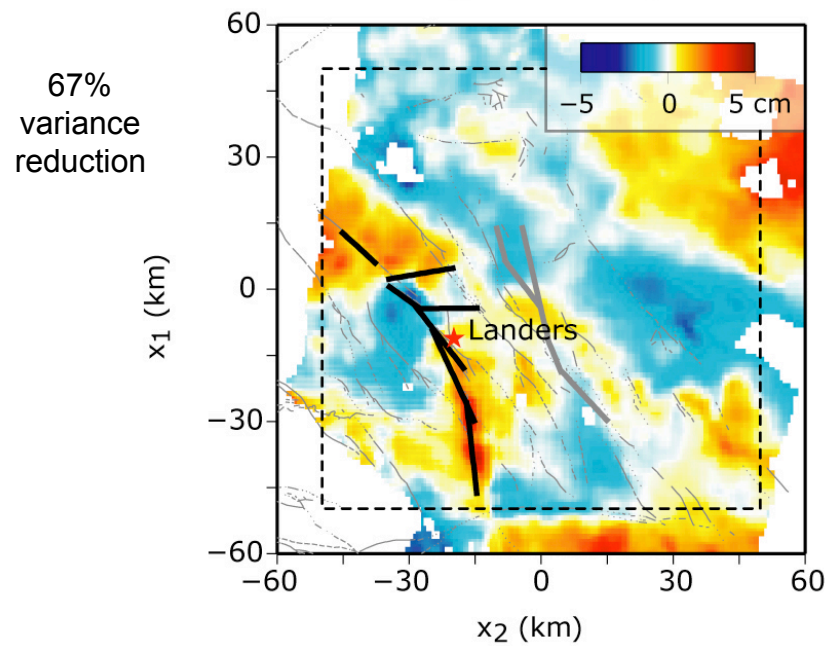
A. Stack of post Landers InSAR data (track 127)



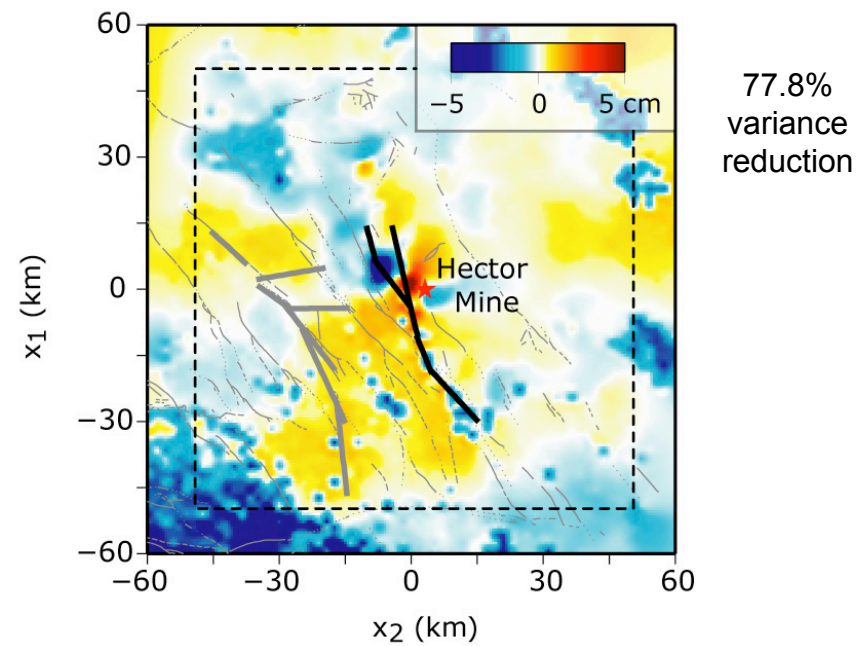
B. Post Hector Mine InSAR data (051207-991020)



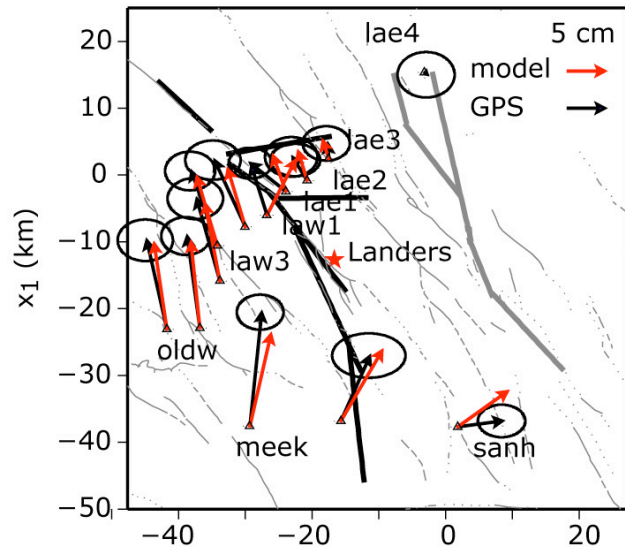
E. InSAR LOS residuals (post Landers)



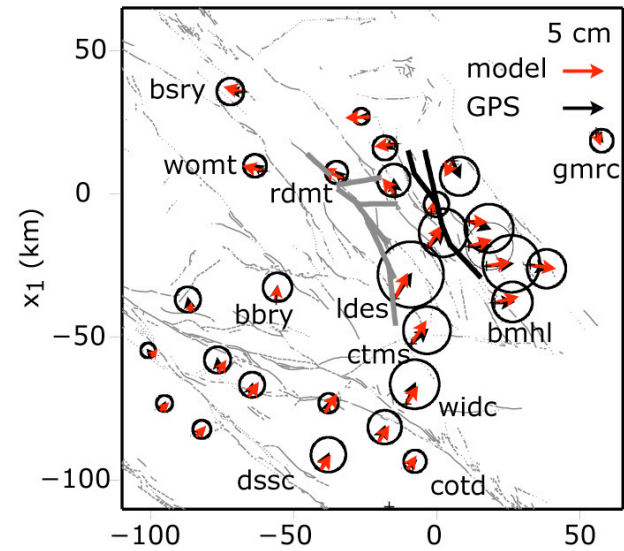
F. InSAR LOS residuals (post Hector Mine)



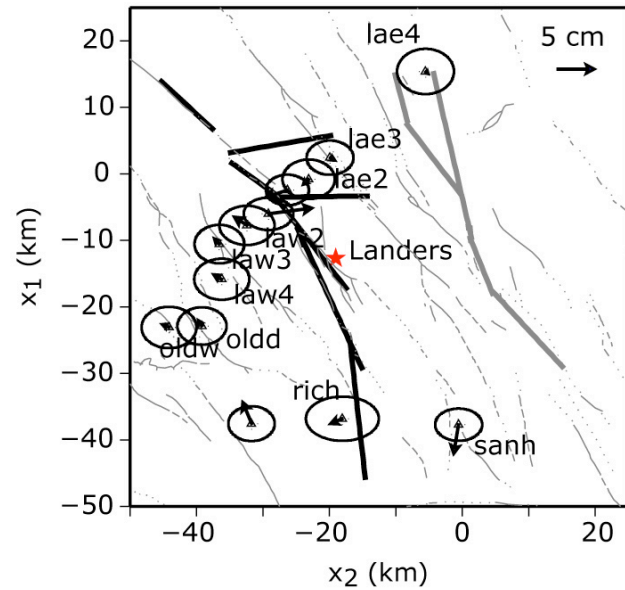
A. Post Landers campaign GPS data and model



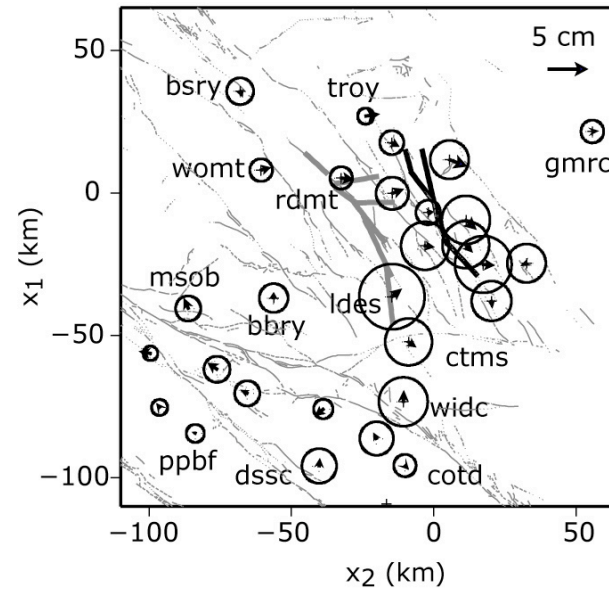
B. Post Hector Mine continuous GPS data and model



C. Residuals of post Landers viscoelastic model

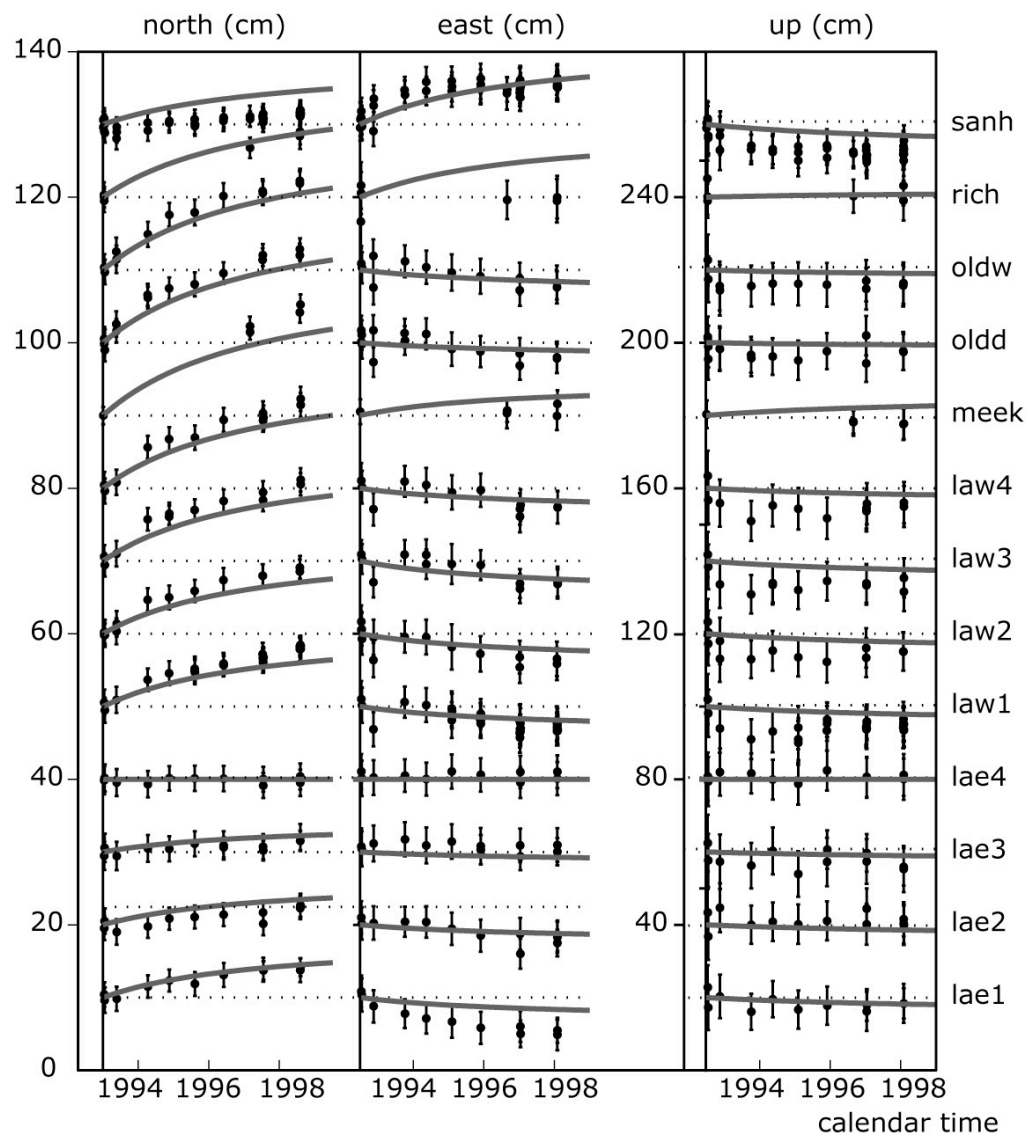


D. Residuals with post Hector Mine viscoelastic model



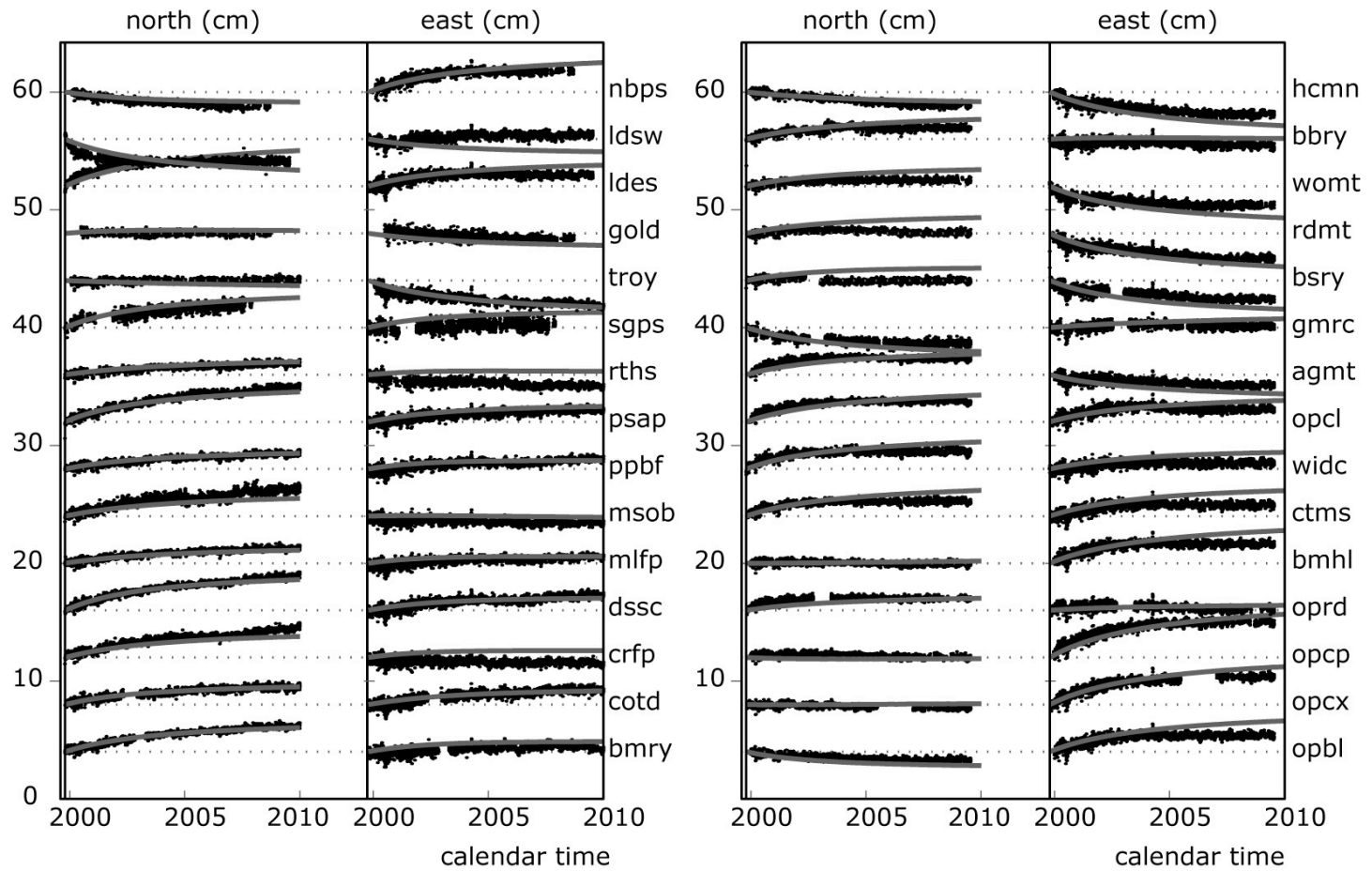
Time series: Landers

Post Landers campaign GPS and viscous model predictions



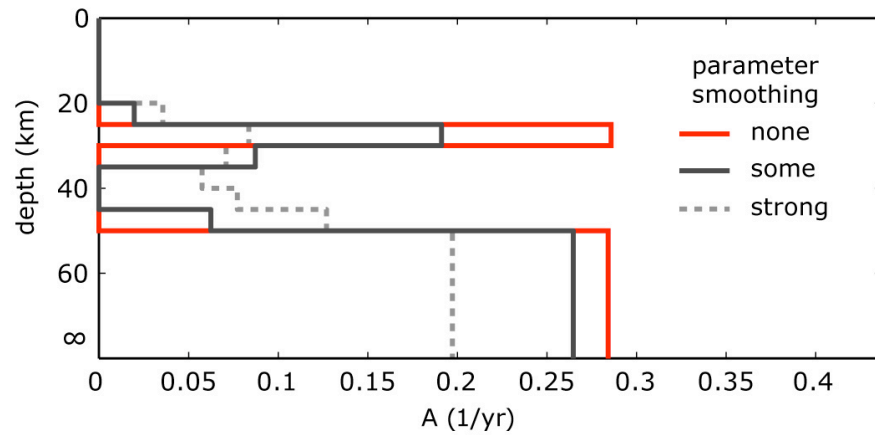
Time series: Hector Mine

Post Hector Mine continuous GPS data and viscous model predictions

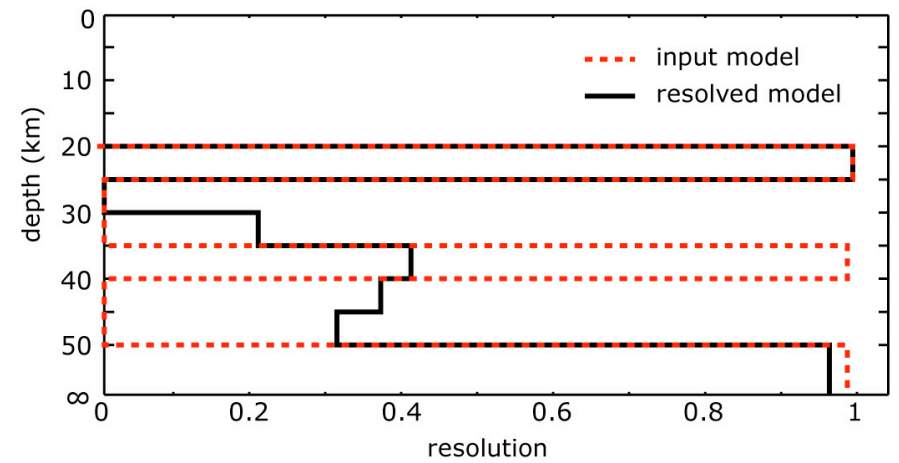


Preferred model and resolution

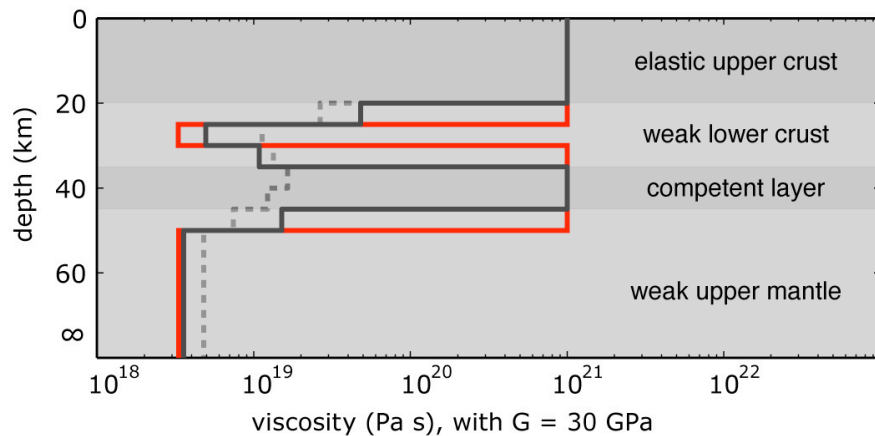
A. Models of lithosphere fluidity from post Landers and post HM data



C. Resolution of inverse problem

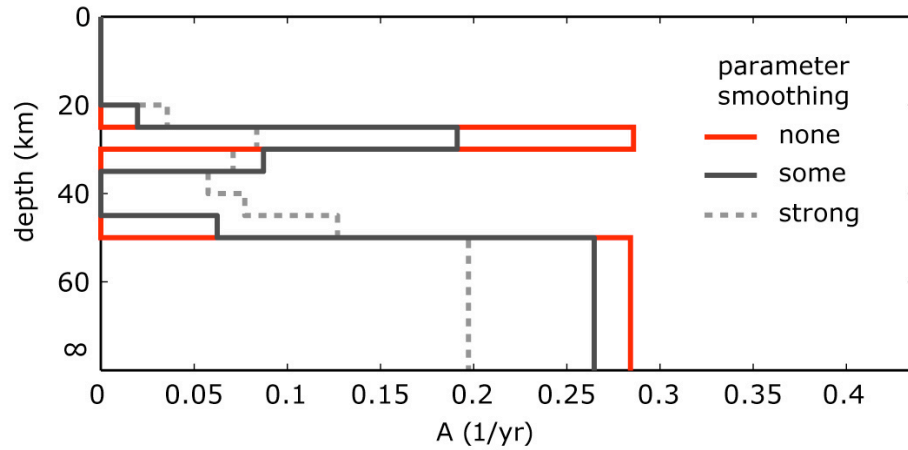


B. Inferred viscosity profiles

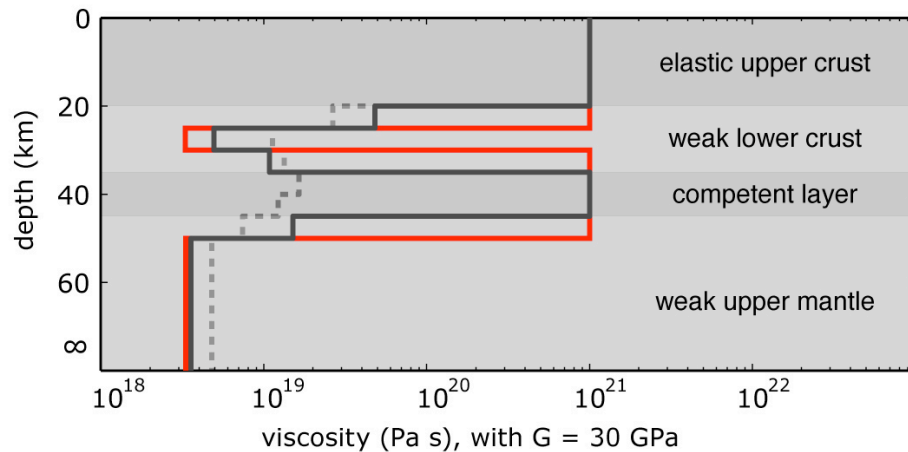


Geological implications

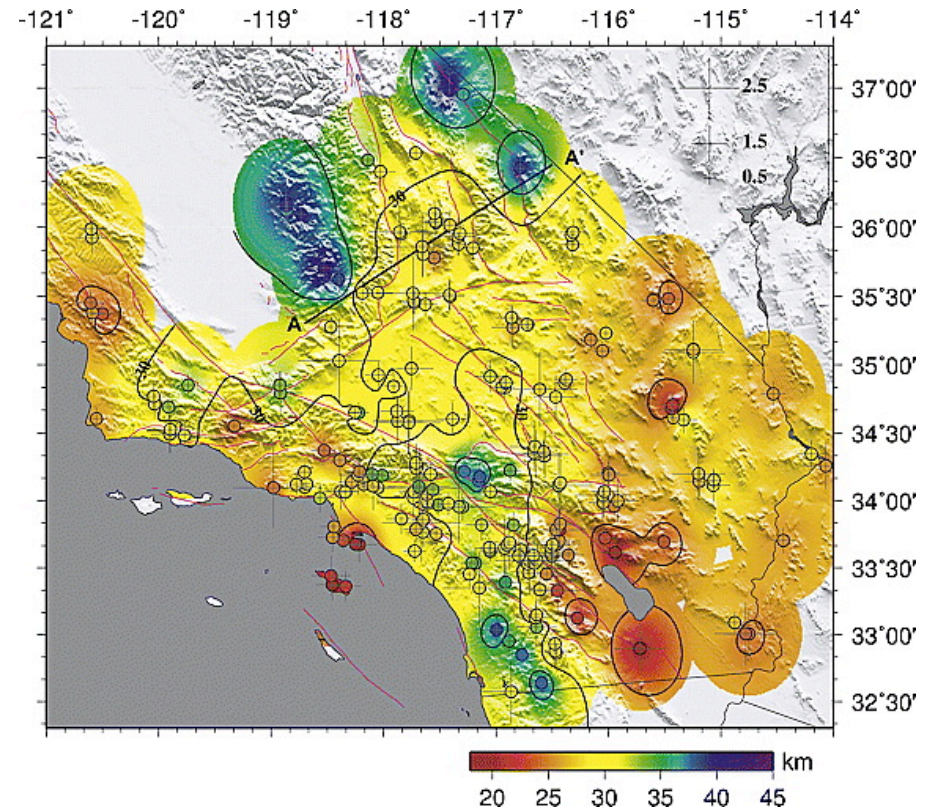
A. Models of lithosphere fluidity from post Landers and post HM data



B. Inferred viscosity profiles



Depth of crust/mantle transition (Moho) in Southern California

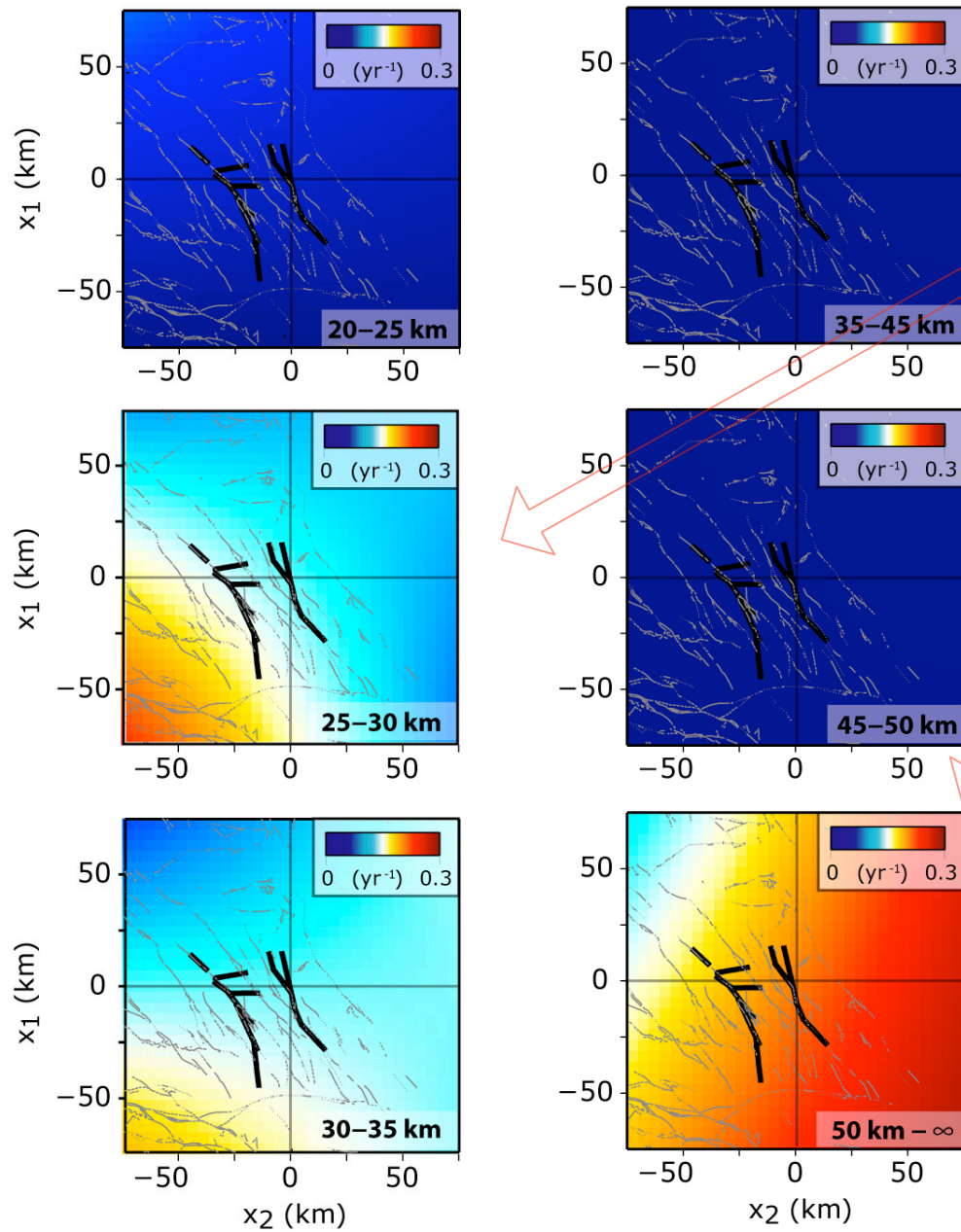


Yan & Clayton, 2007

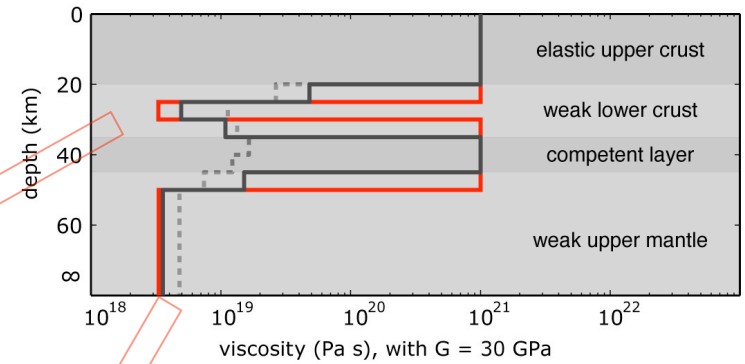
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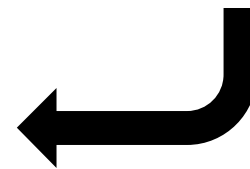
3D tomography of lithosphere viscosity

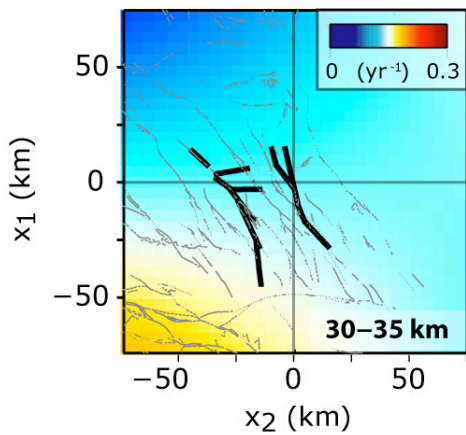
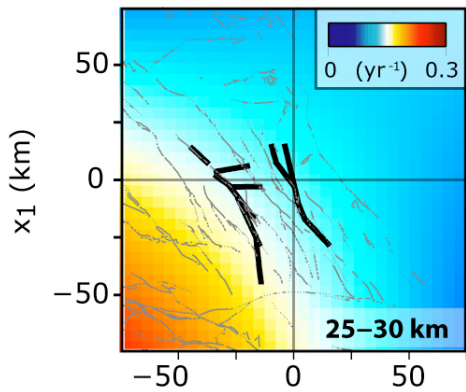
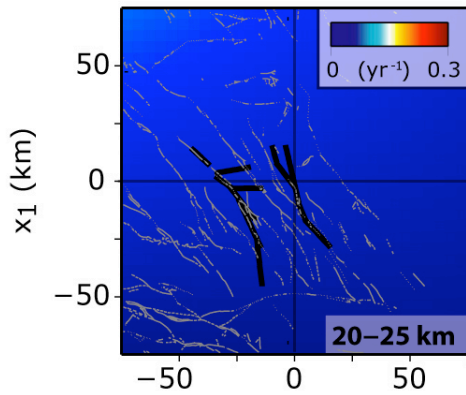


B. Inferred viscosity profiles



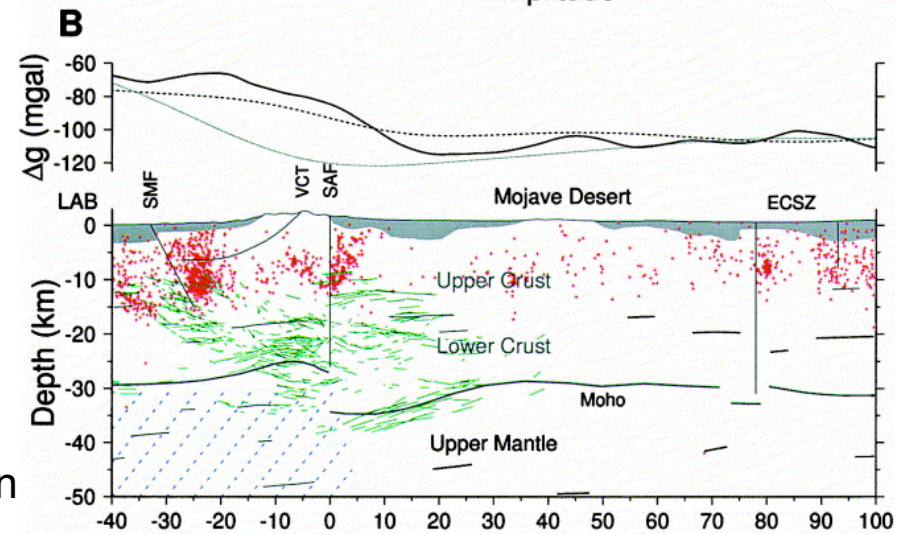
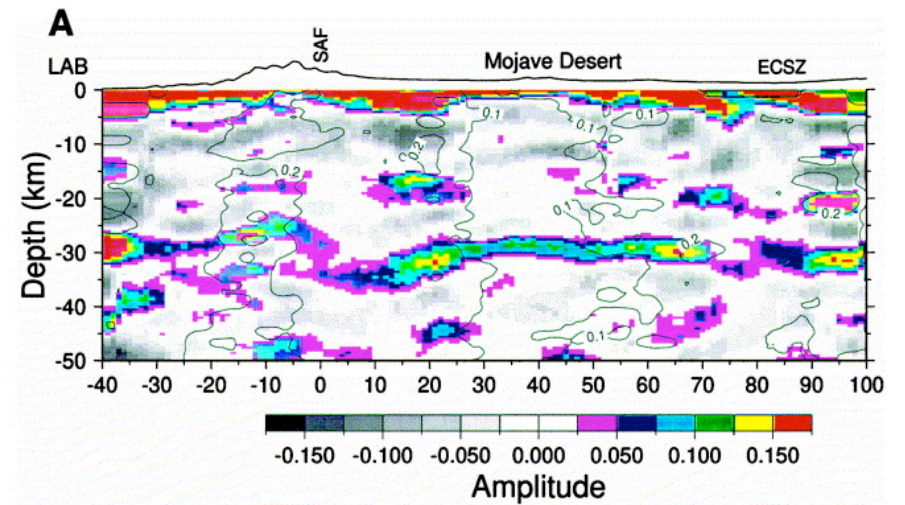
one parameter
per block





Thickness of ductile layer
is coincident with
deepening of Moho

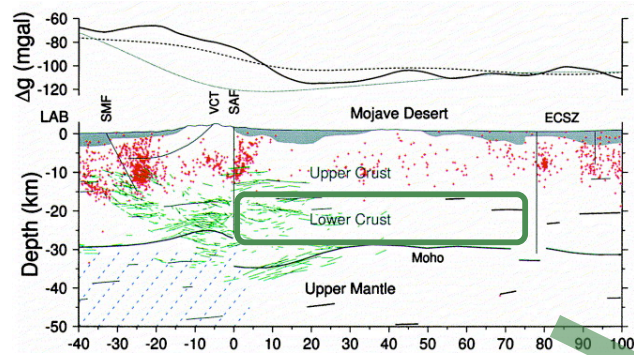
Moho marks transition
from crustal rocks
to mantle rocks and
ductile/competent transition



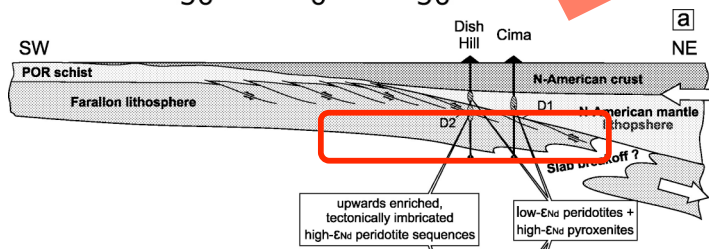
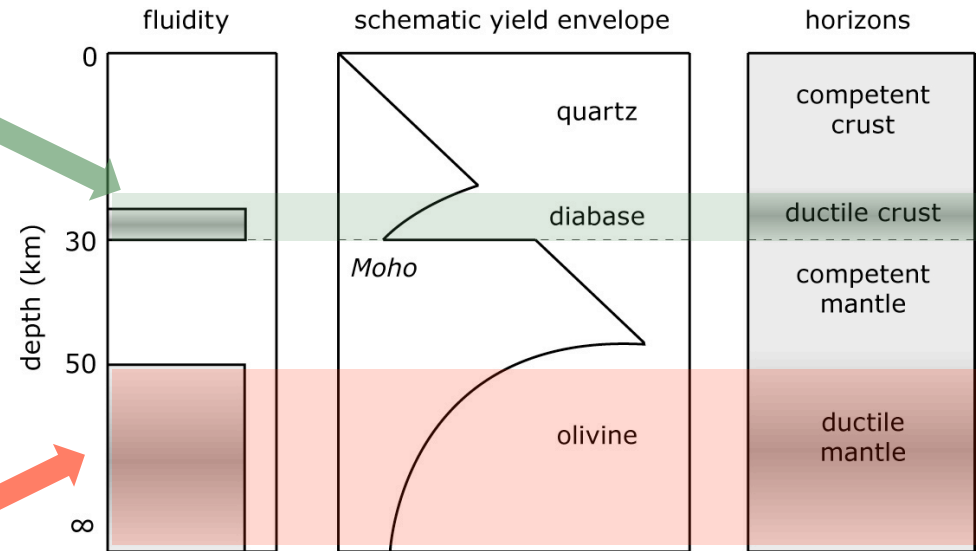
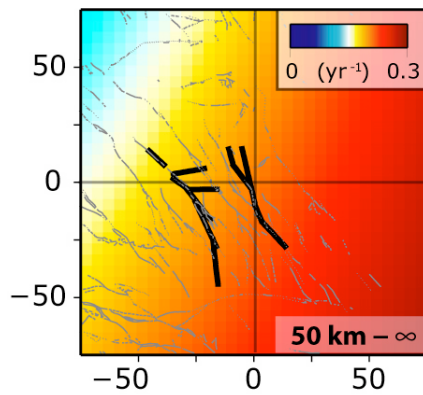
Zhu, 2000

Strength of the Mojave lithosphere

Zhu, 2000

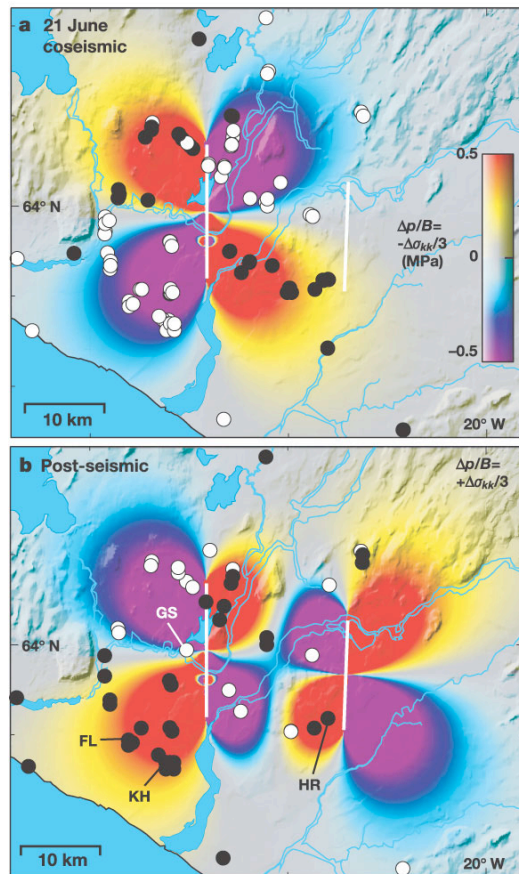


inferred lower lithosphere fluidity

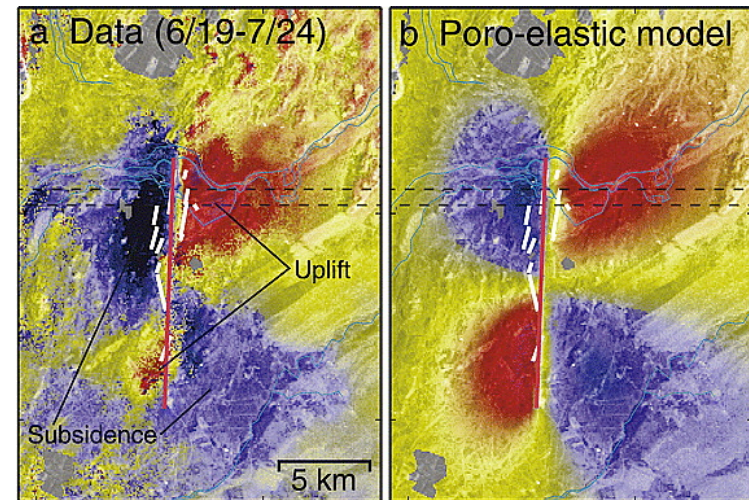


Luffi et al, 2009

A tradeoff between poroelastic rebound and lower-crust viscous flow?



Jónsson et al., 2003



Árnadóttir et al., 2005

Is poroelastic rebound
a valid contributor to far-field
postseismic deformation?

Conclusions

- Afterslip is not a preferred model but may still take place (and bias inferred location of lower-crustal flow)
- The tradeoff between poroelasticity and viscoelasticity for the Landers data is resolved by the Hector Mine geodetic data
- Resolution of ductile horizons is greatly improved by considering Landers & Hector Mine data sets
- InSAR and GPS are best explained by the presence of two viscous horizons: the lower crust and the lower lithosphere separated by a mantle lid (jelly sandwich)
- Lateral variations in viscosity are more important in the lower crust than upper mantle.
- Mojave Moho marks transition between elastic AND viscous properties of rocks