

Plasticity in rupture dynamics: what role does pore fluid play?

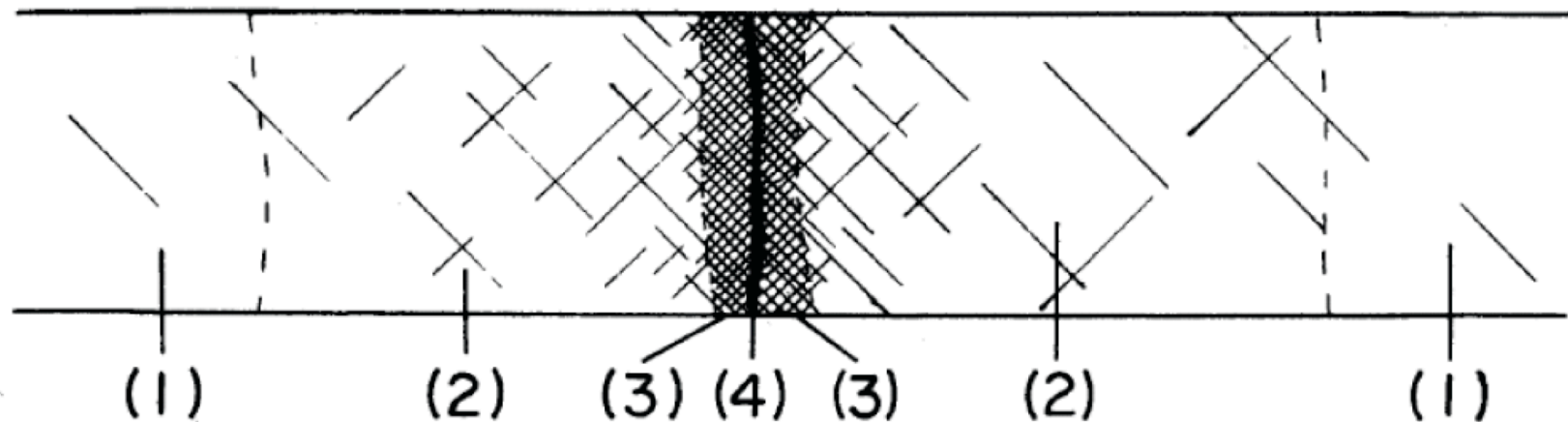
**23 June 2009
NMCDEF, Golden, CO**

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Eric M. Dunham²
James R. Rice
(Harvard University)**

**Now at: ¹ Exxon-Mobil Research
² Stanford University**

Typical structure of a mature fault

Internal Structure of Principal Faults of the North Branch San Gabriel Fault



1) Undeformed Host Rock

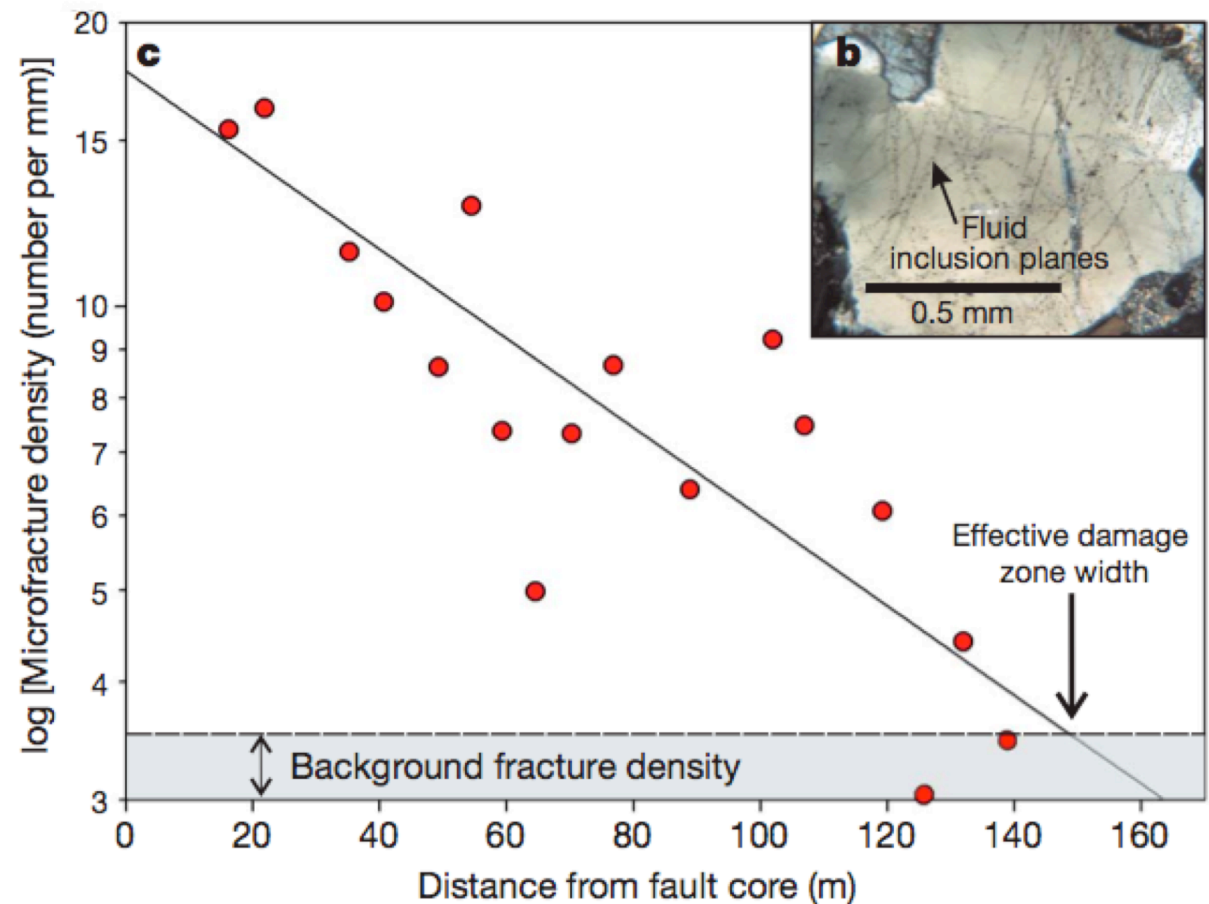
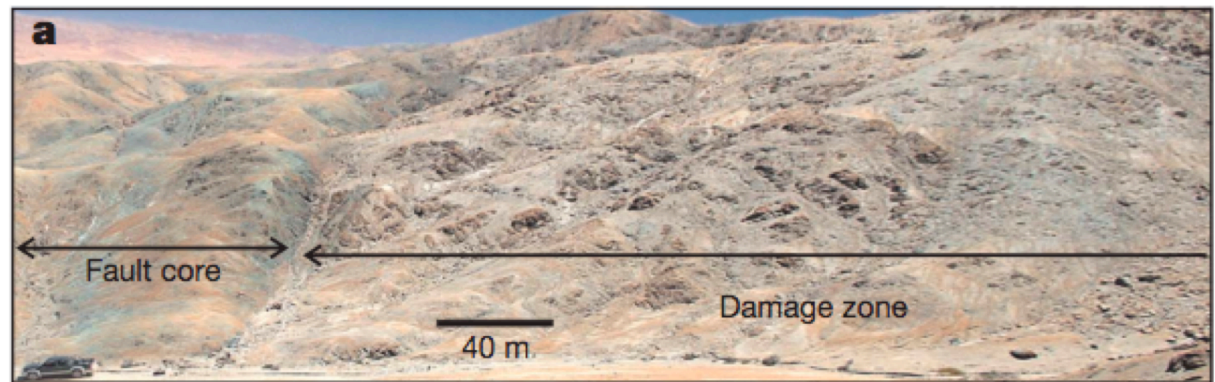
fault zone	{	2) Damaged Host Rock (<i>highly cracked, 10-100 m</i>)	}	fault core
		3) Foliated Zone (<i>granulated fault zone, 1-10 m</i>)		
		4) Central ultracataclasite layer (<i>10-100 mm</i>)		

Damage zone observations

Caleta Coloso fault,
Atacama Desert,
Chile

>5km offset

Exhumed from
4–10km

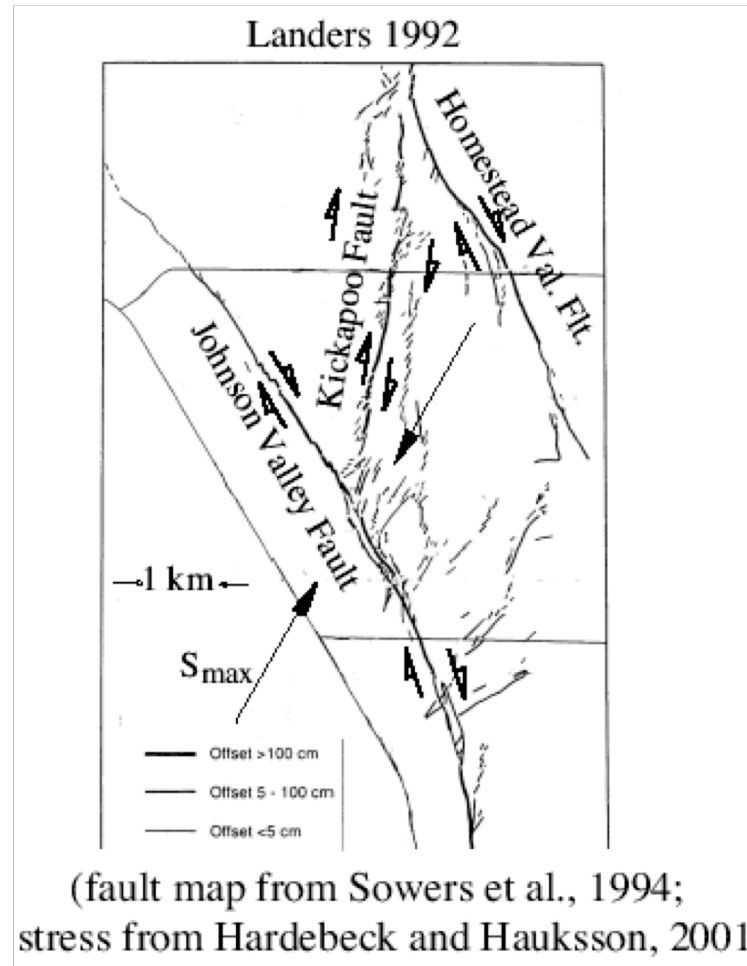


Faulkner et al. (2006)

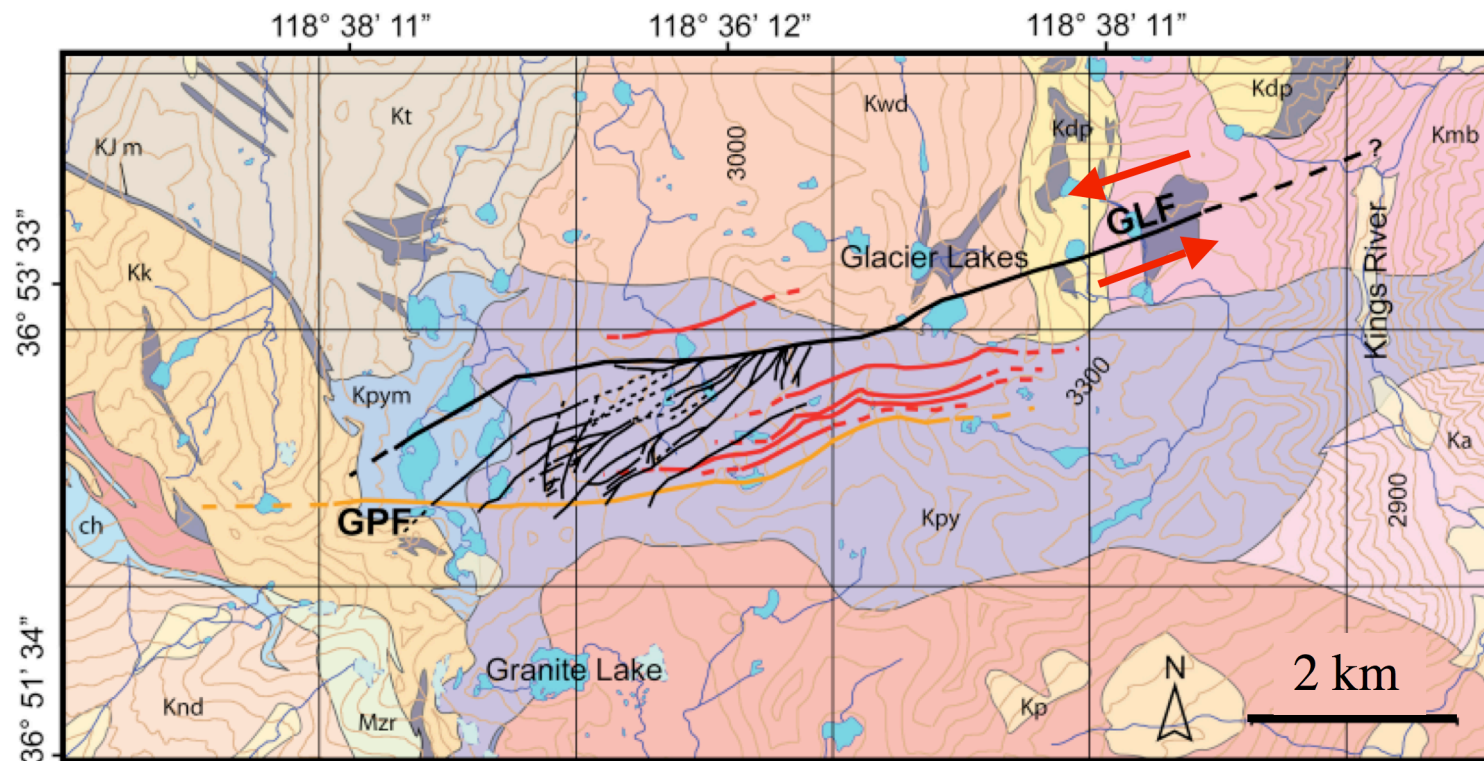
Damage zone observations

[Poliakov, Dmowska and Rice, *JGR*, 2002]

Map view: Steep S_{\max} direction, $\Psi \approx 60^\circ$;
secondary failures on *extensional* side:

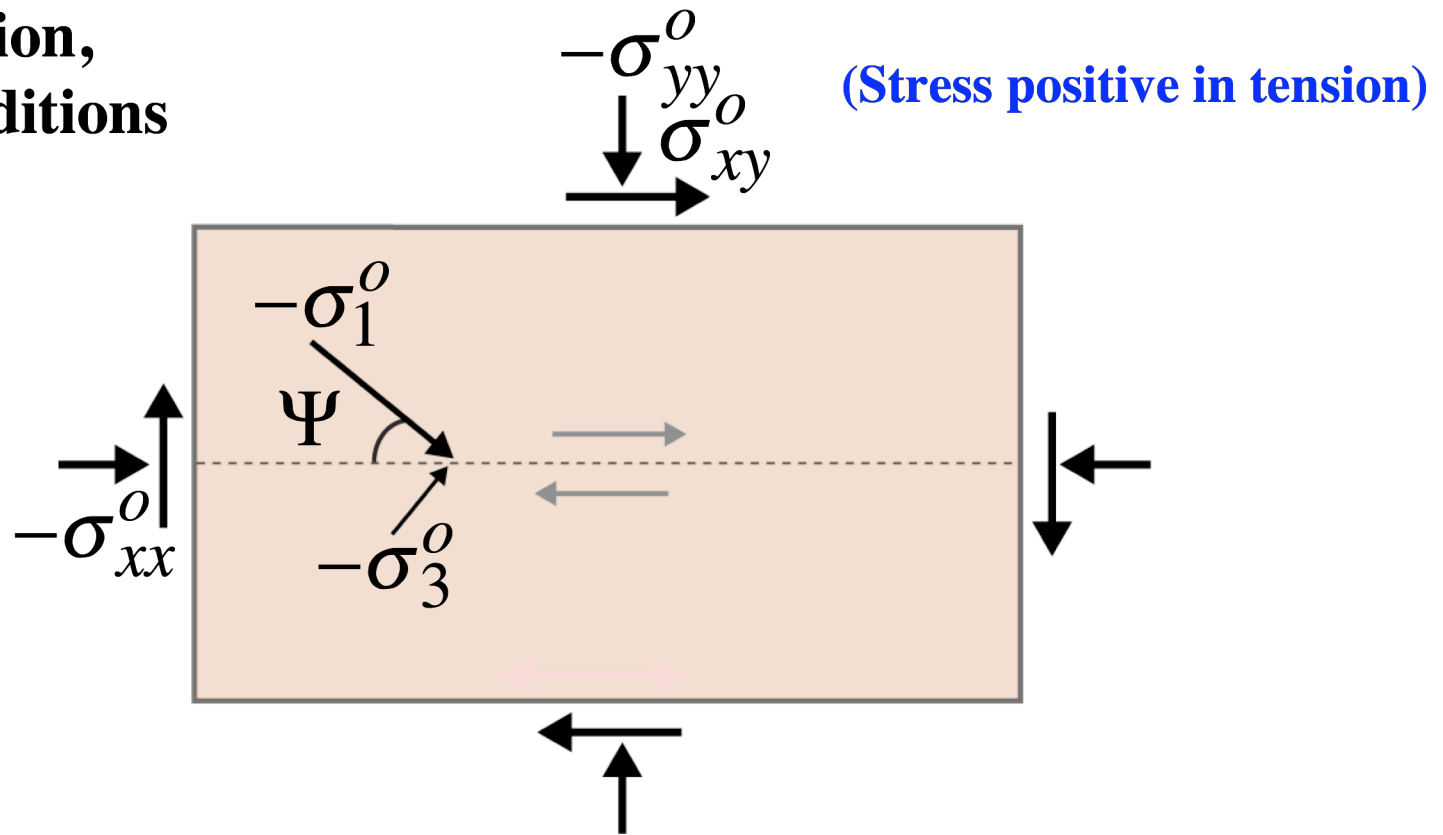


Damage zone observations

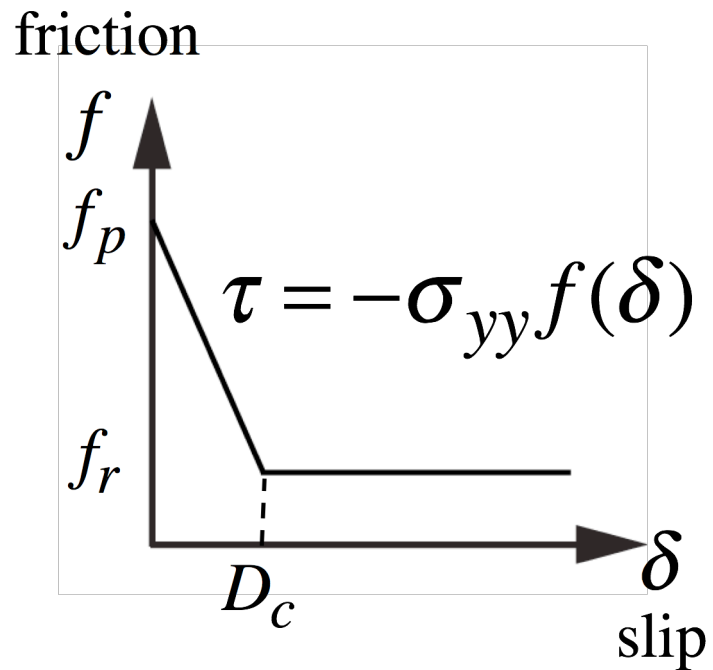
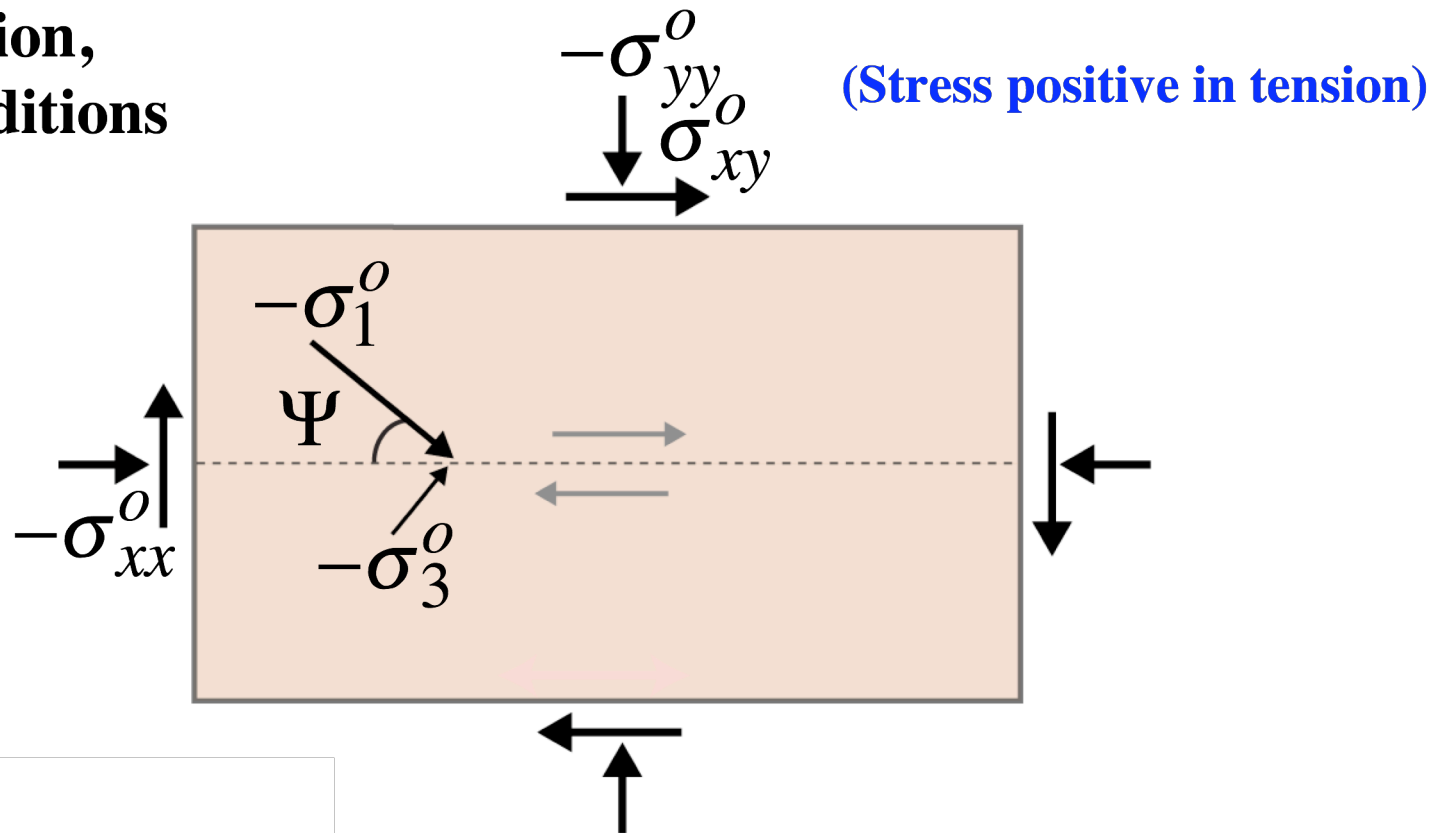


J. D. Kirkpatrick, Z. K. Shipton, J. P. Evans, S. Micklethwaite, S. J. Lim, and P. McKillop, *J. Geophys. Res.*, **113**, B04304, (2008).

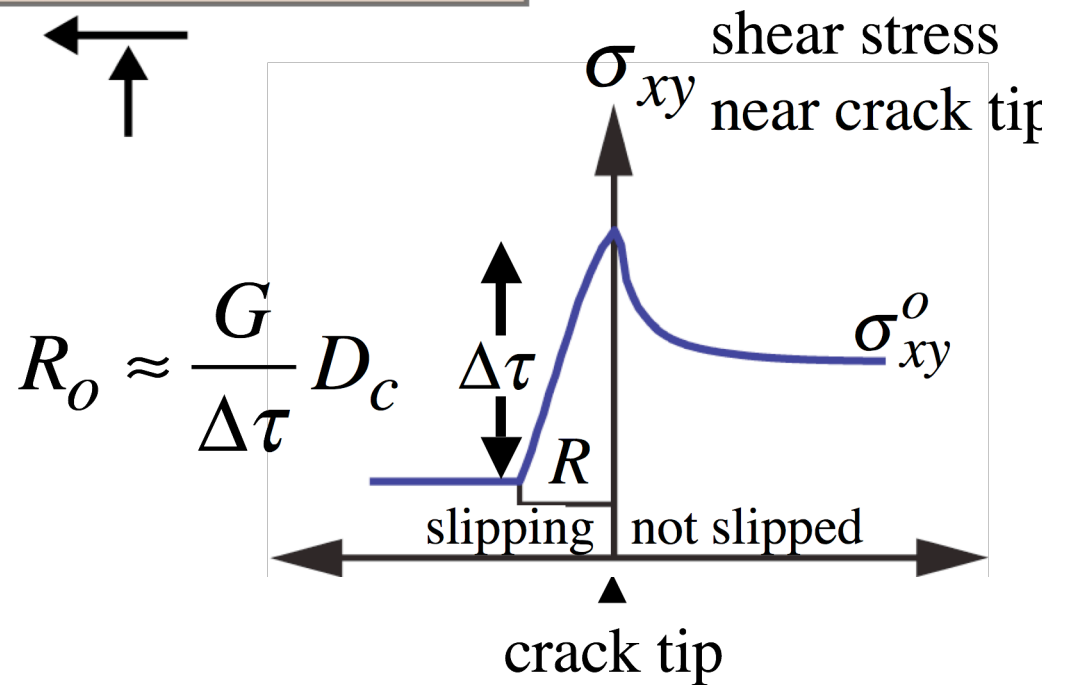
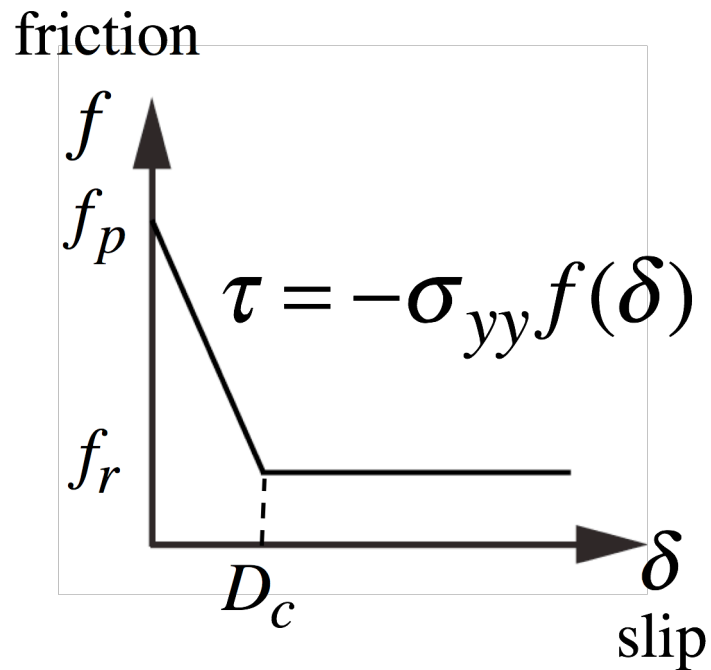
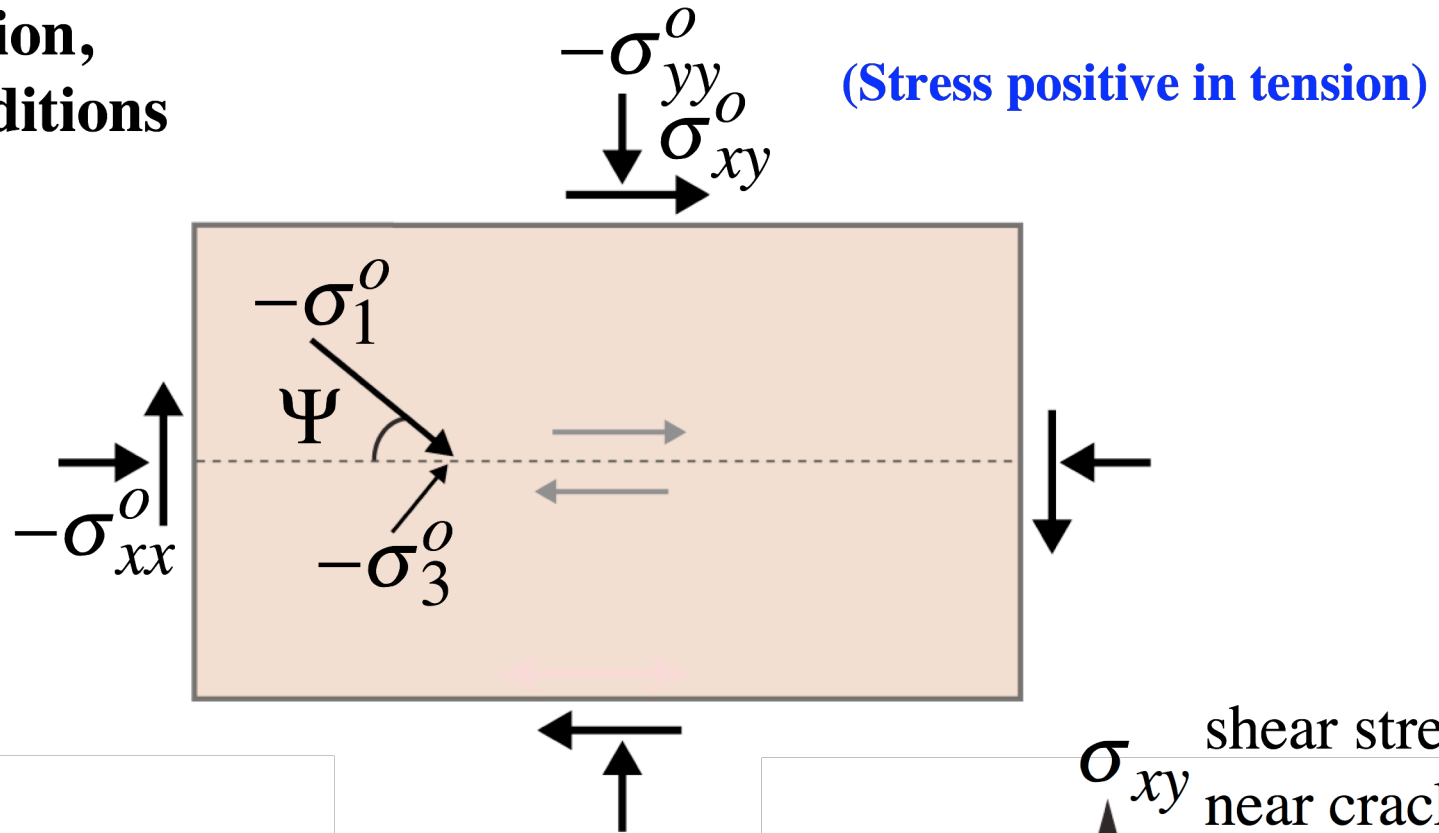
**Fault friction,
initial conditions**



Fault friction, initial conditions



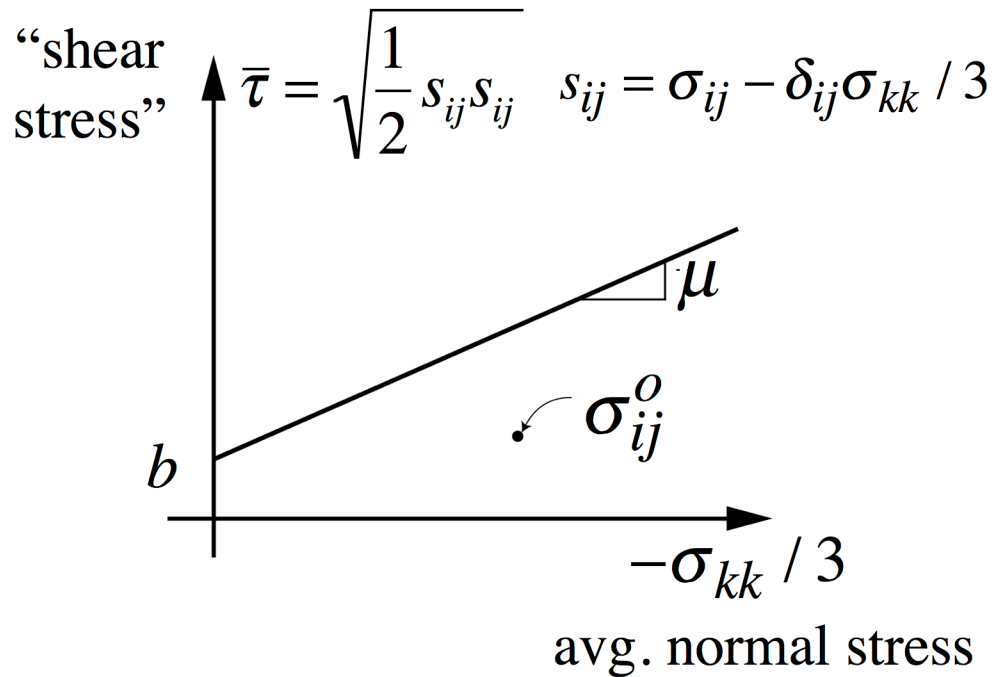
Fault friction, initial conditions



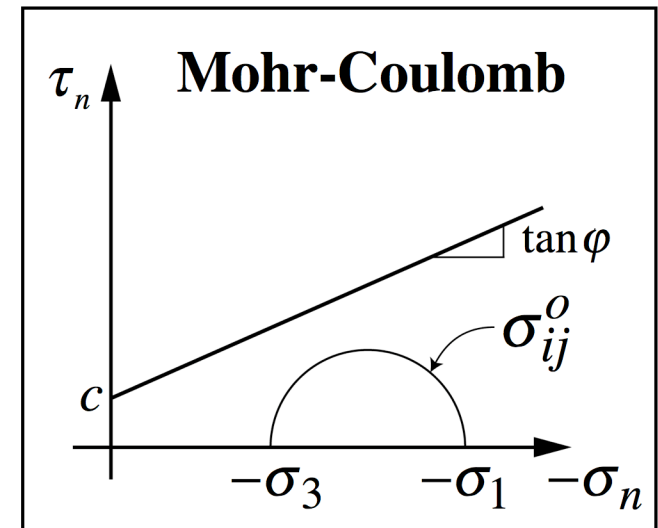
Off-fault material description

Linear elasticity with Drucker-Prager plastic yield criterion:

Drucker-Prager

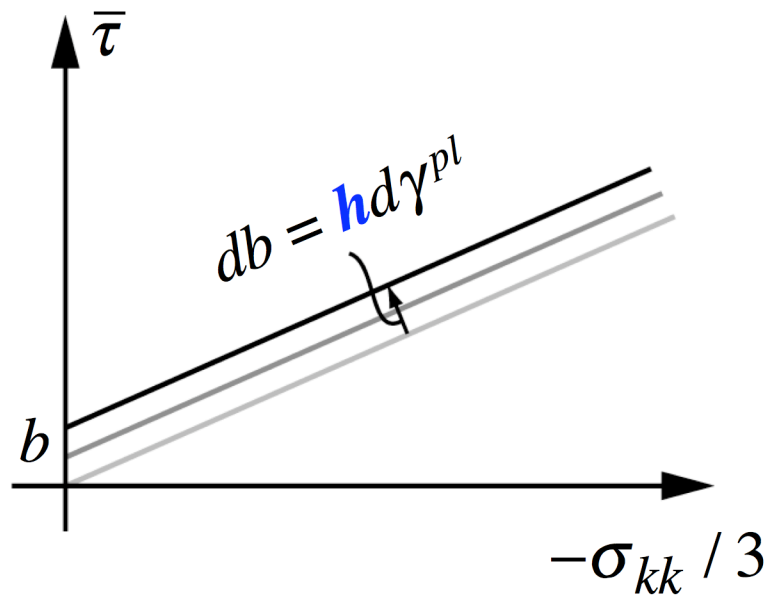


compare to:



Off-fault material description Linear elasticity with Drucker-Prager plastic yield criterion:

Hardening of yield surface, h



$h = 0$: no plastic hardening
(perfectly plastic)

Plastic dilatancy, β

$$d\epsilon_{kk}^{pl} = \beta d\gamma^{pl}$$

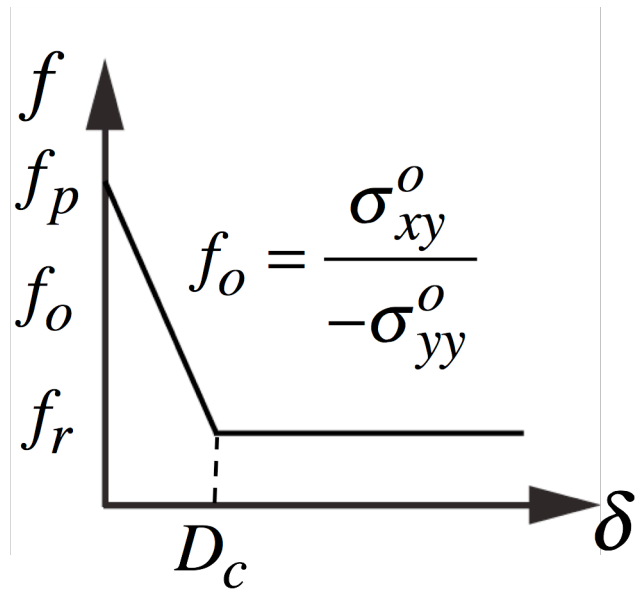
increment of
plastic volumetric
strain

increment of
plastic “shear
strain”

$\beta = 0$: no plastic dilation

Measures of proximity to failure of initial stress state

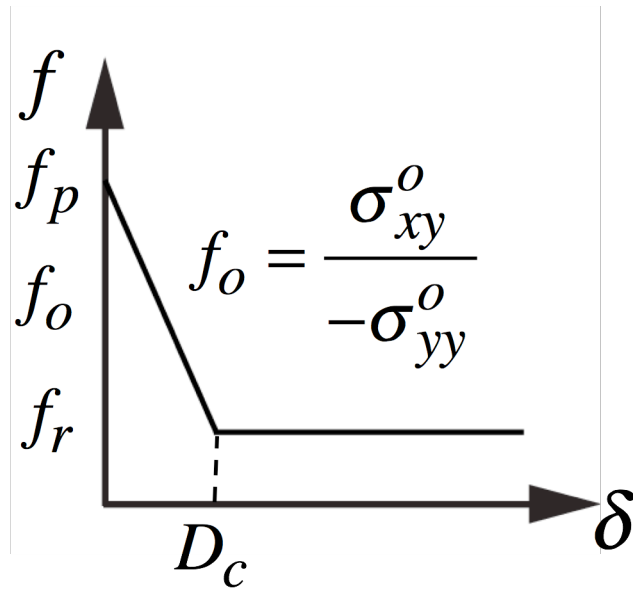
On fault



$$S = \frac{f_p - f_o}{f_o - f_r}$$

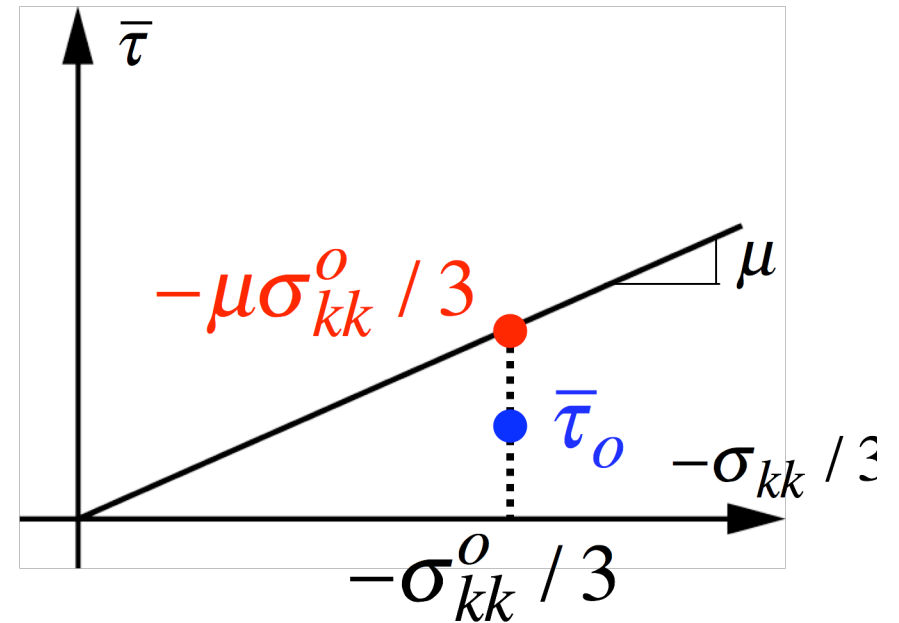
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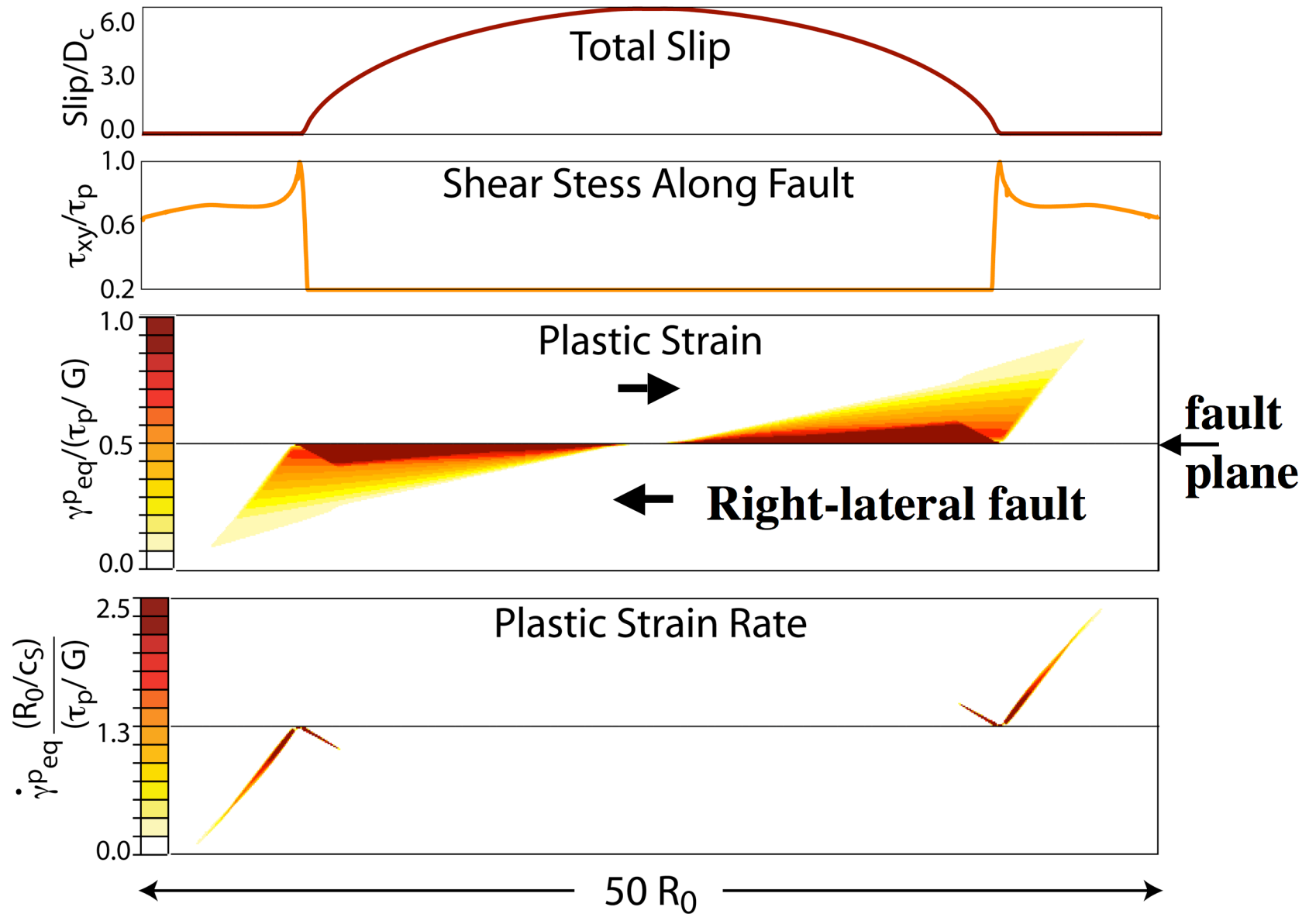
Off fault



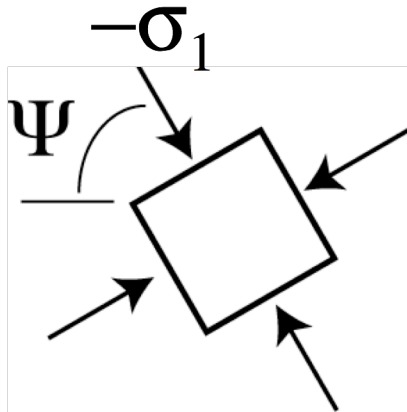
$$CF = \frac{\bar{\tau}_o}{-\mu\sigma_{kk}^o/3}$$

(S, CF, and Ψ are interdependent)

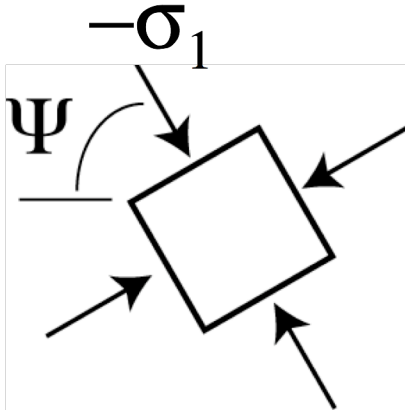
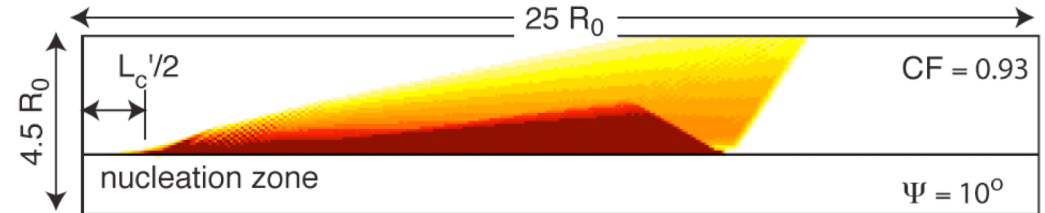
Evolution of plastic strain during rupture



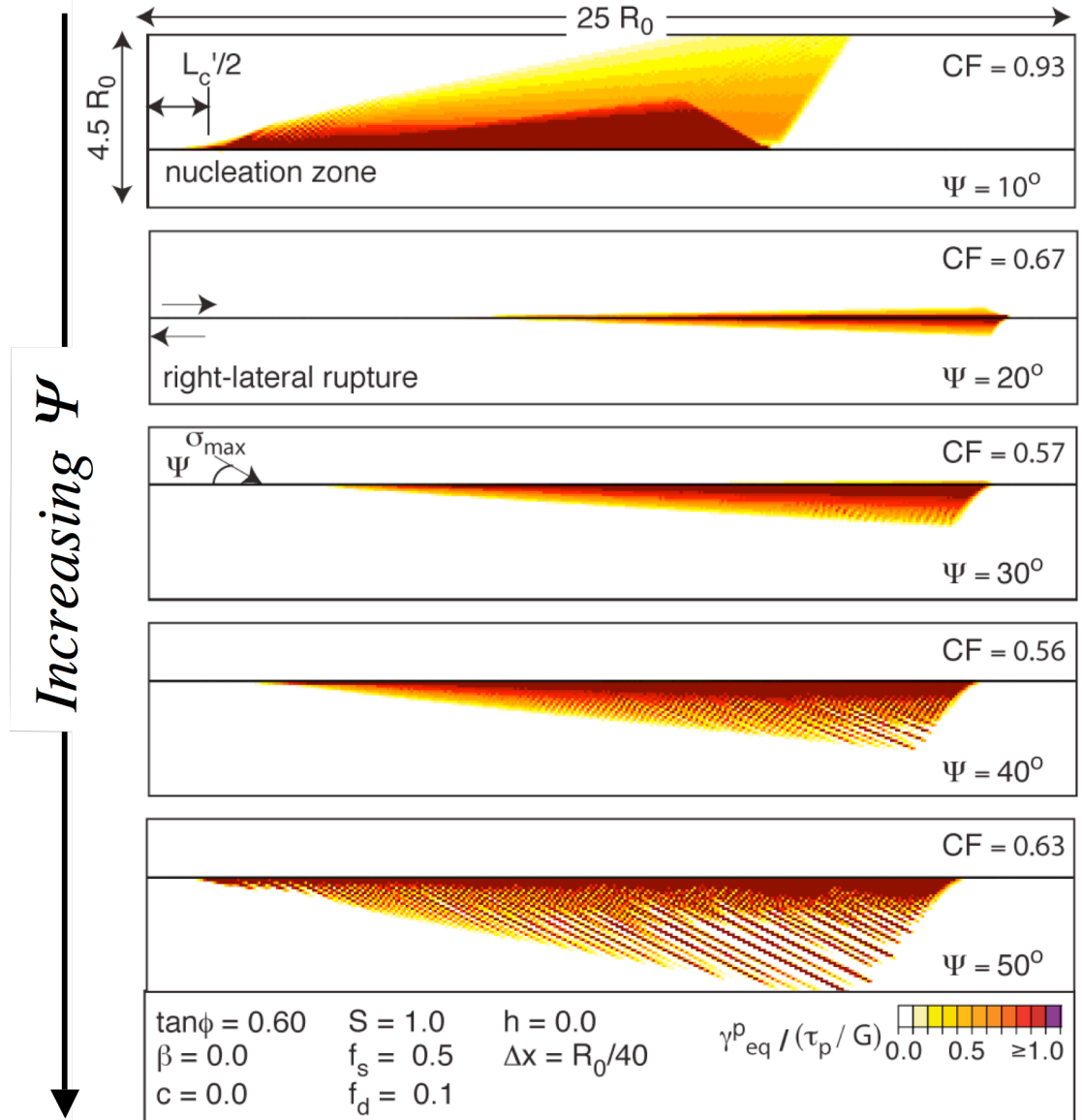
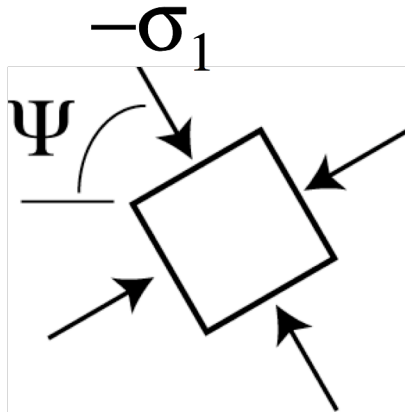
Locations of plastic strain: Effect of pre-stress angle (Ψ)



Locations of plastic strain: Effect of pre-stress angle (Ψ)

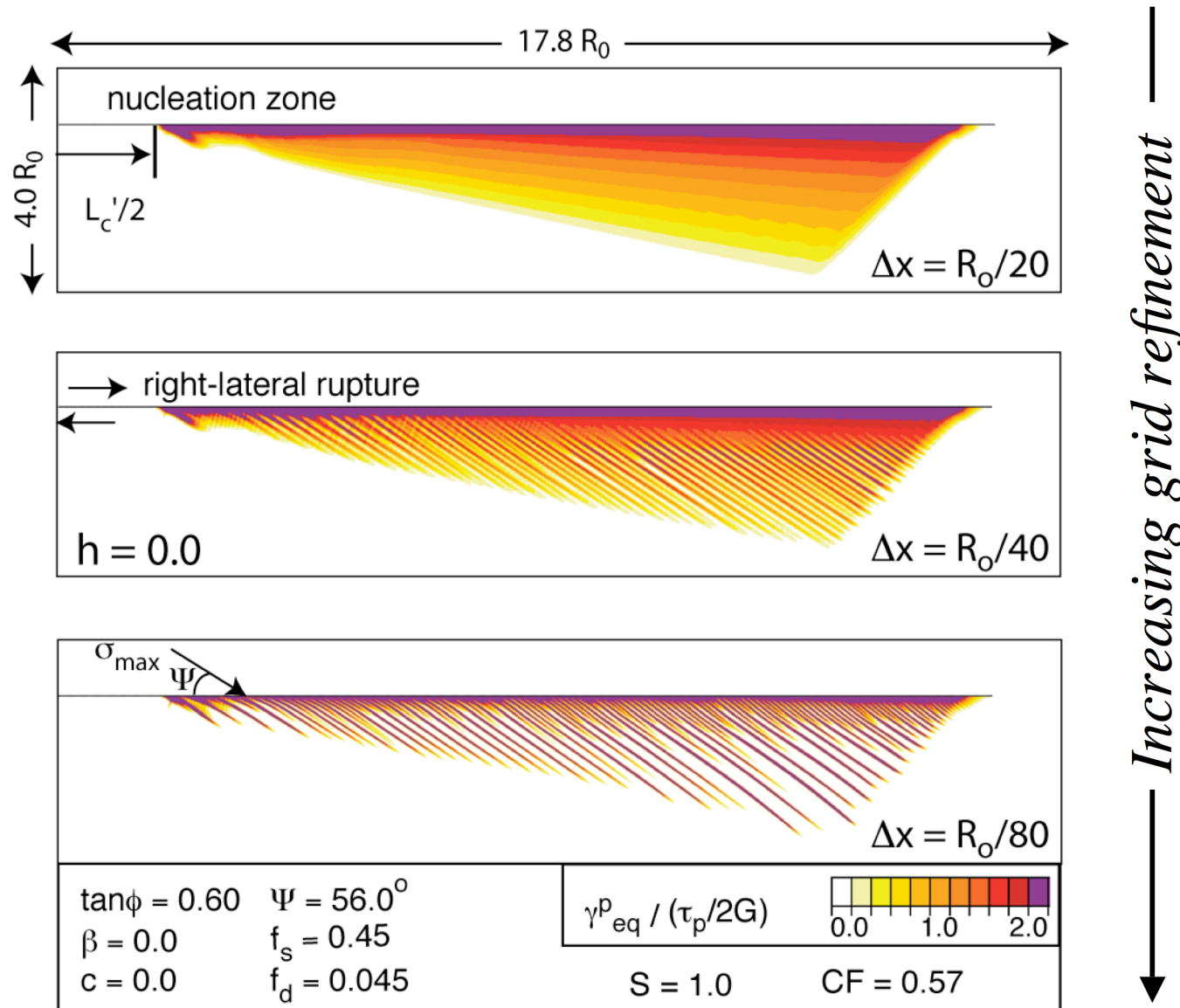


Locations of plastic strain: Effect of pre-stress angle (Ψ)



Templeton & Rice (2008)

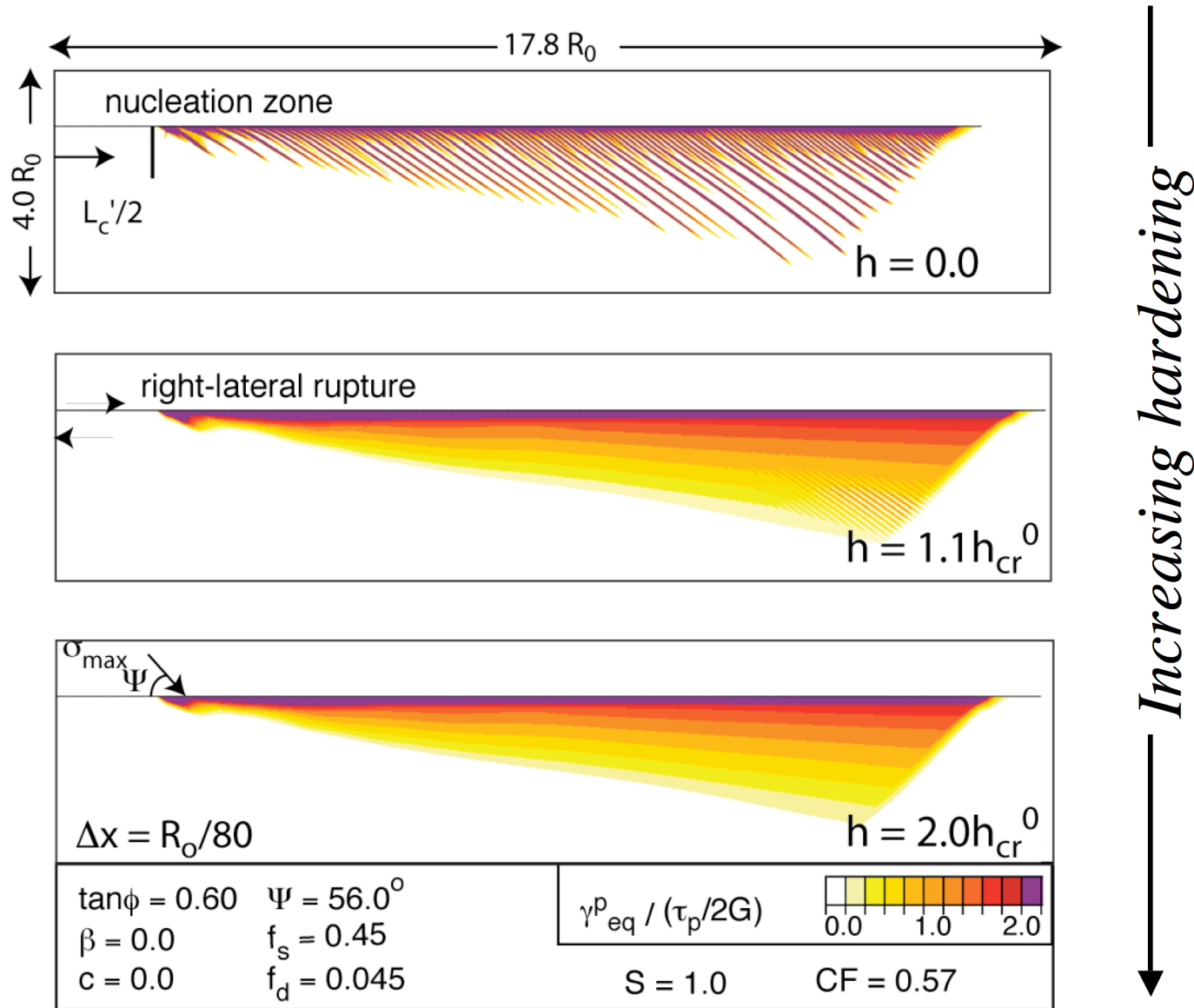
Localizations: effect of grid refinement



Templeton & Rice (2008)

Localizations: hardening eliminates features

Effects of increasing $h > h_{cr}^0$ for fixed grid refinement $\Delta x = R_0 / 80$



Templeton & Rice (2008)

How do we account for fluid saturation?

How does it affect deformation patterns?

Undrained deformation

$$\text{when } \frac{\text{stressing timescale}}{\text{diffusive timescale}} \ll 1$$

over lengthscale
of interest

For rapid stressing of dynamic rupture, pore fluid diffusion is negligible (“undrained”) down to lengths of O(mm-cm)

Undrained deformation

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For rapid stressing of dynamic rupture, pore fluid diffusion is negligible (“undrained”) down to lengths of O(mm-cm)

Undrained *poroelastic* response:

$$\Delta p_u = -B \frac{\Delta \sigma_{kk}}{3}$$

Skempton coefficient, typ. 0.5–0.9

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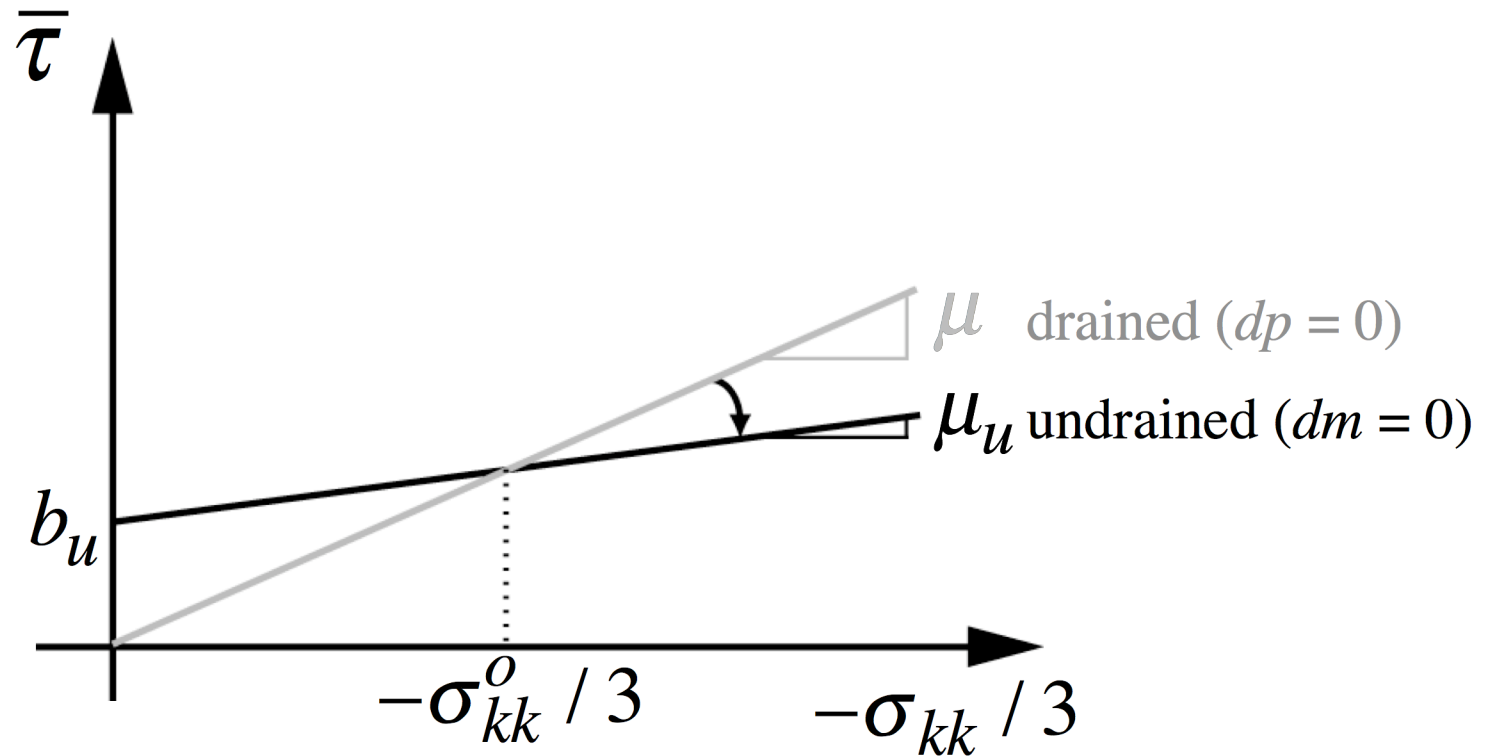
Skempton coefficient, typ. 0.5–0.9

Material strength depends on
effective stress

$$\bar{\sigma}_{ij} = \sigma_{ij} + p\delta_{ij}$$

Undrained deformation: Transformation of yield criterion

[e.g., Rudnicki, 2000; Viesca et al., 2008]

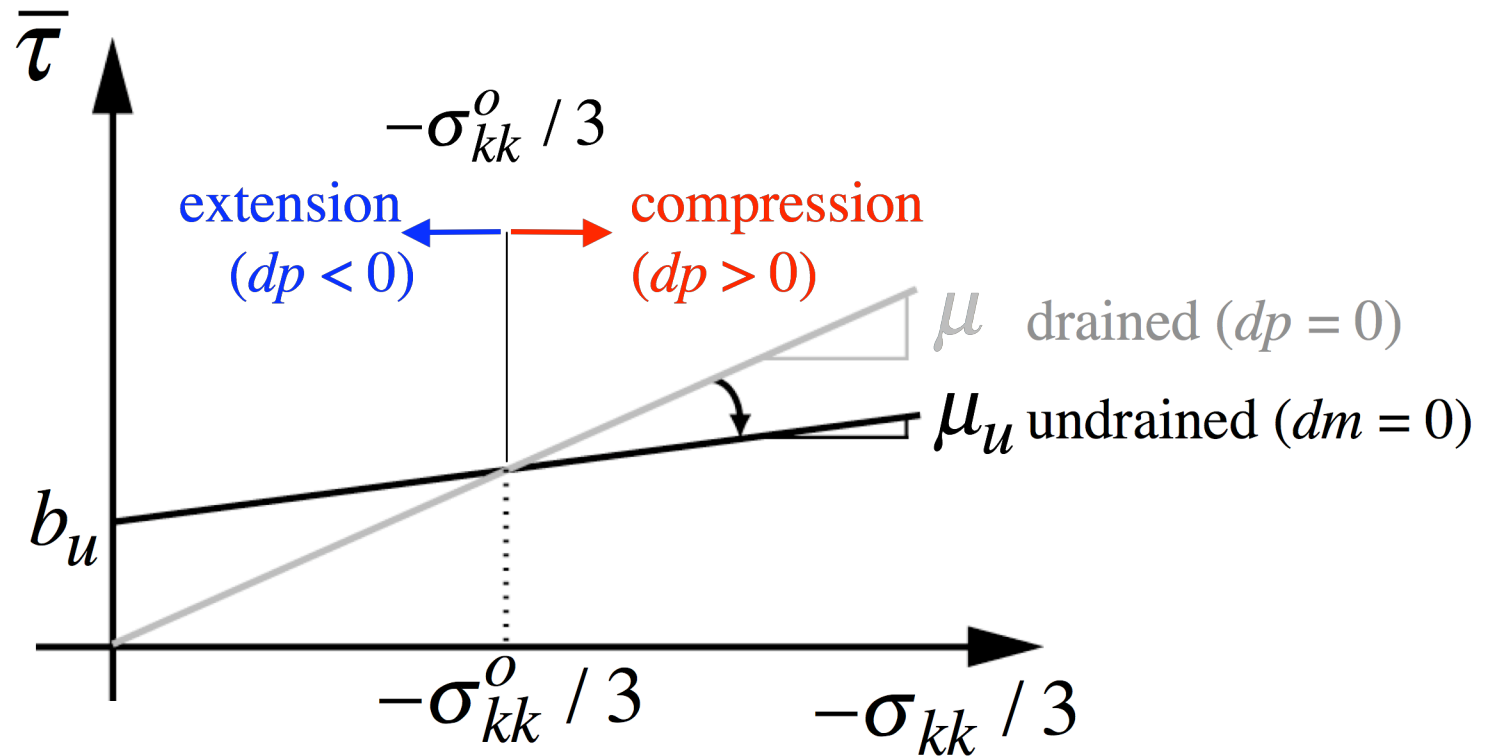


Undrained behavior
can be characterized by

$$\begin{aligned} b &\rightarrow b_u \\ \mu &\rightarrow \mu_u \\ K &\rightarrow K_u \end{aligned}$$

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Undrained behavior
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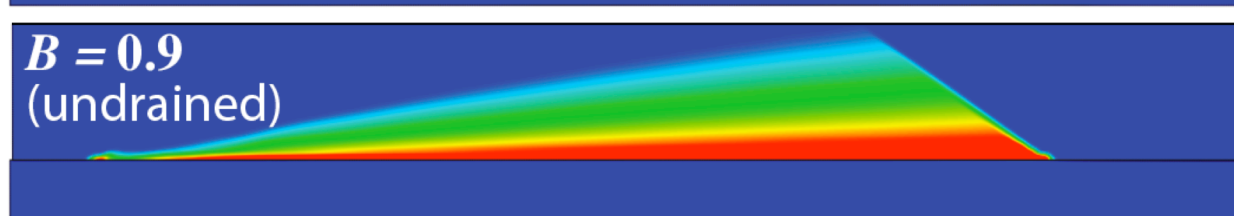
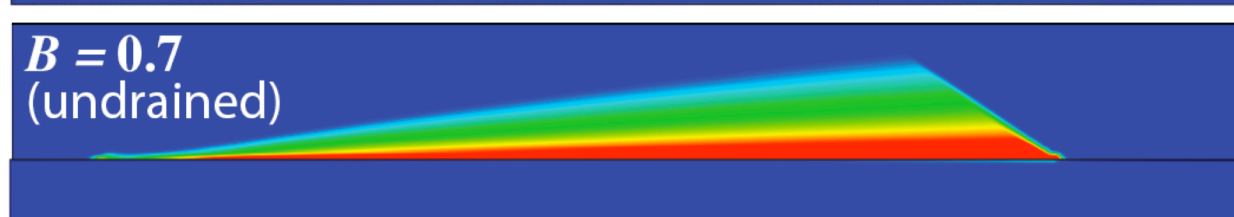
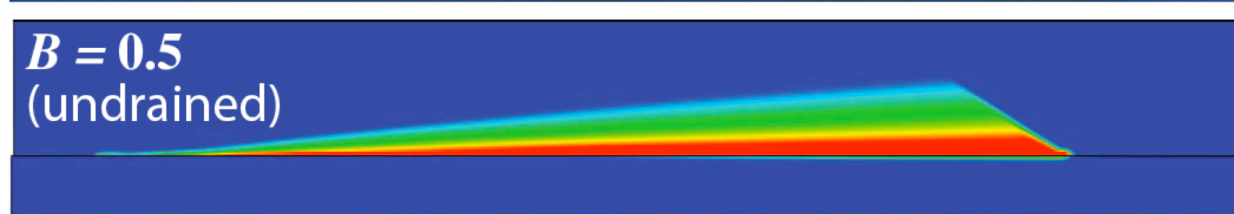
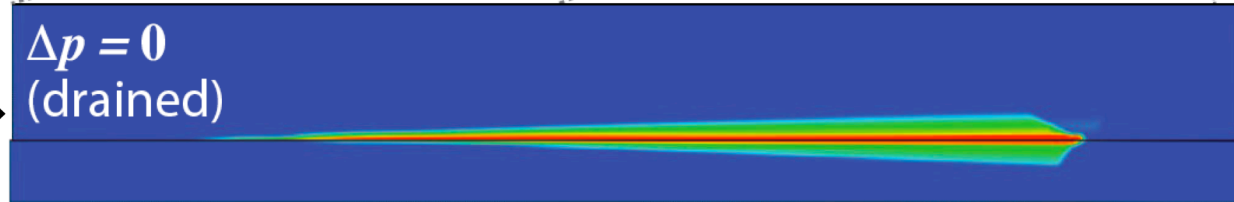
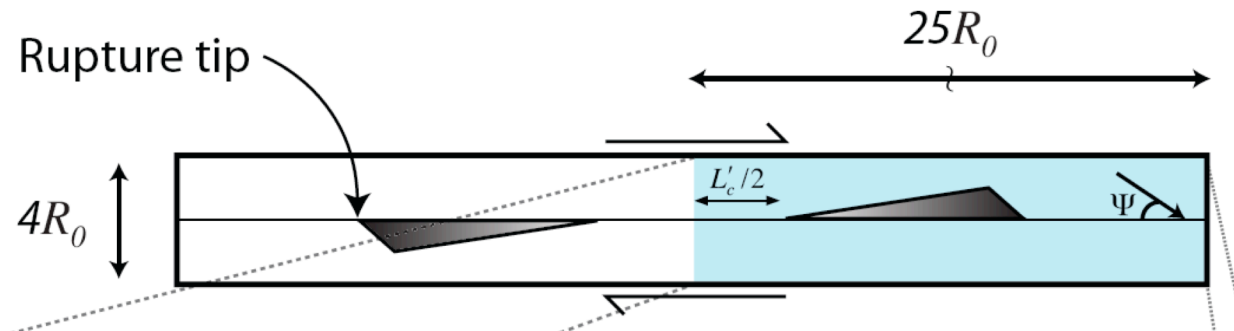
$$\mu \rightarrow \mu_u$$

$$K \rightarrow K_u$$

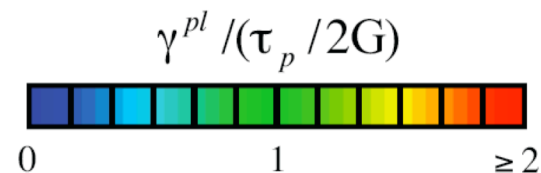
Effect of Skempton coefficient B ($h = 0$)

Neglects fluid saturation \Rightarrow

Consider saturation }

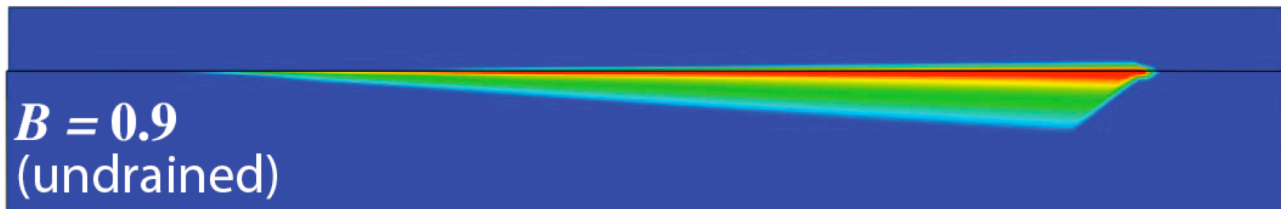
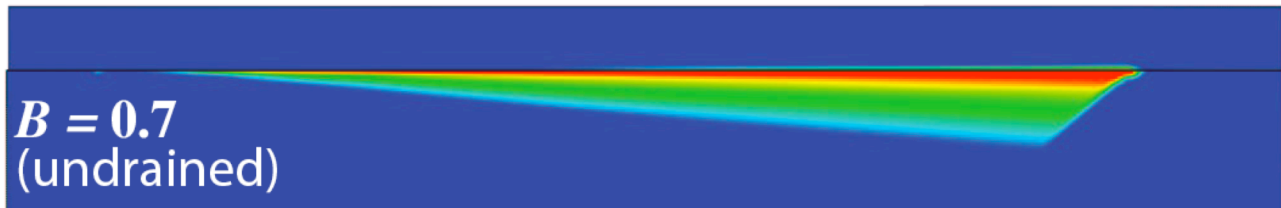
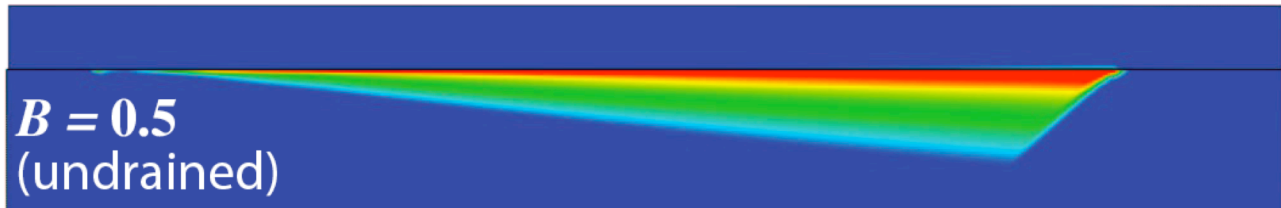
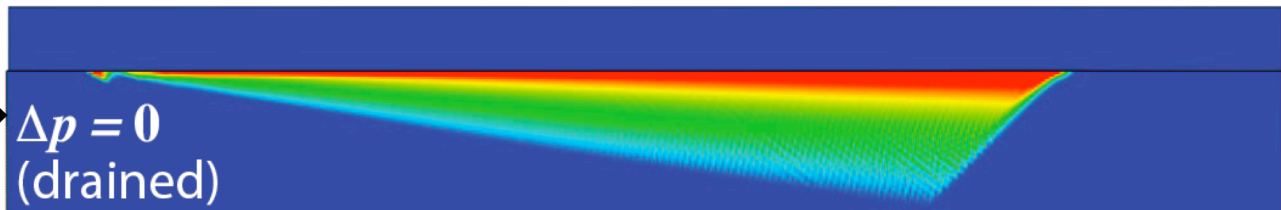

$$\Psi = 14^{\circ}$$

Viesca et al. (2008)

$$\begin{array}{lll} \mu = 0.6 & \Psi = 14^\circ & S = 1 \\ f_s = 0.65 & & CF = 0.8 \\ f_r = 0.05 & & \end{array}$$


Effect of Skempton coefficient B ($h = 0$)

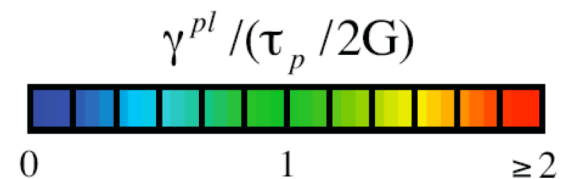
Neglects fluid saturation \Rightarrow



Consider saturation

$$\Psi = 56^\circ$$

$$\begin{array}{lll} \mu = 0.6 & \Psi = 56^\circ & S = 1 \\ f_s = 0.45 & & CF = 0.5 \\ f_r = 0.045 & & \end{array}$$



Undrained deformation: Transformation of yield criterion

[e.g., Rudnicki, 2000; Viesca et al., 2008]

Undrained **poro-elastic-plastic** response:

$$dp_u = -B \frac{d\sigma_{kk}}{3} - \beta \cdot (...)$$

dilatancy coefficient

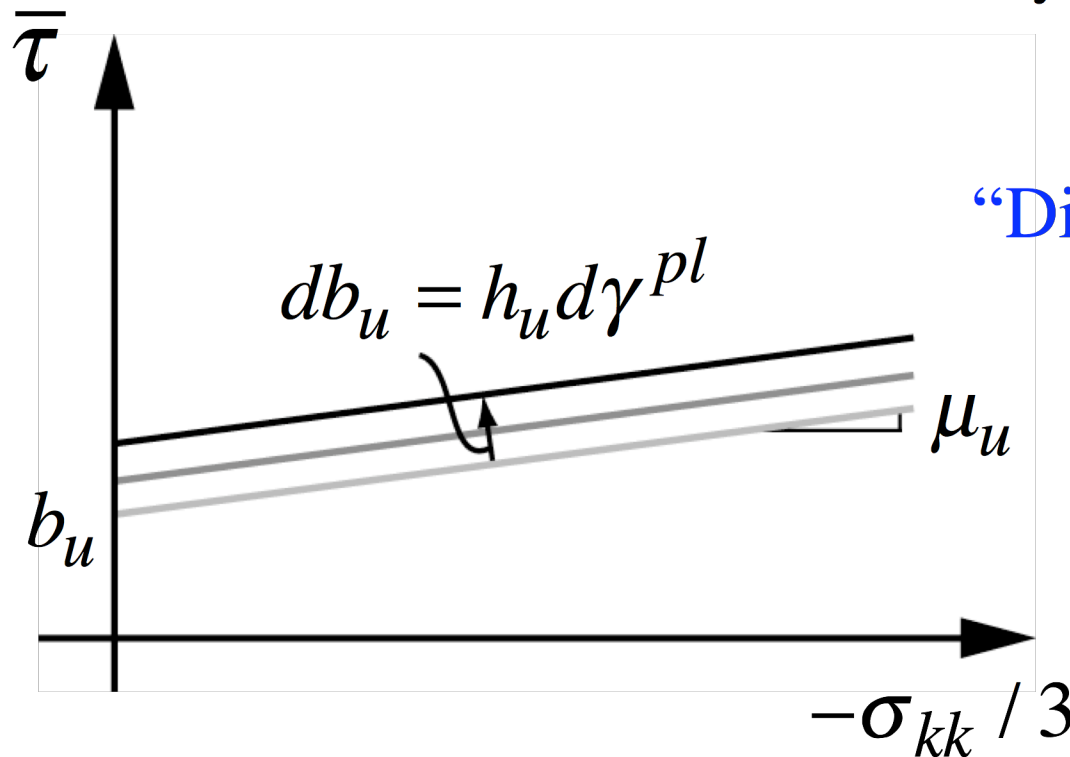
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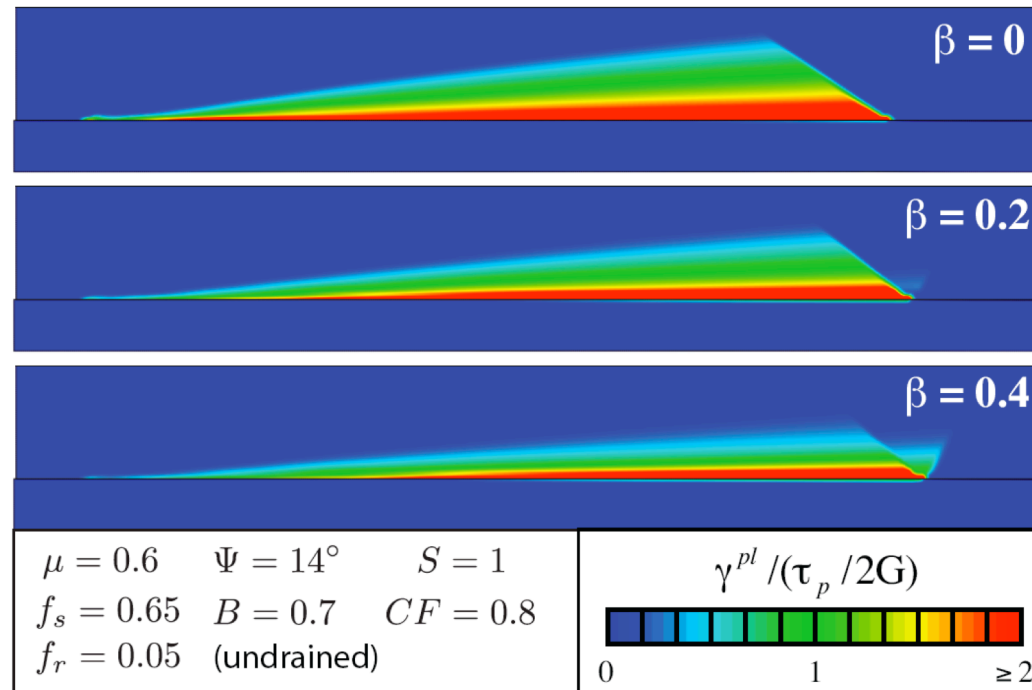
“Dilatant hardening effect”

$$h_u > h$$

for $\beta > 0$

**Effect of
dilatancy
(induces
suction in
pore fluid)
($h = 0$)**

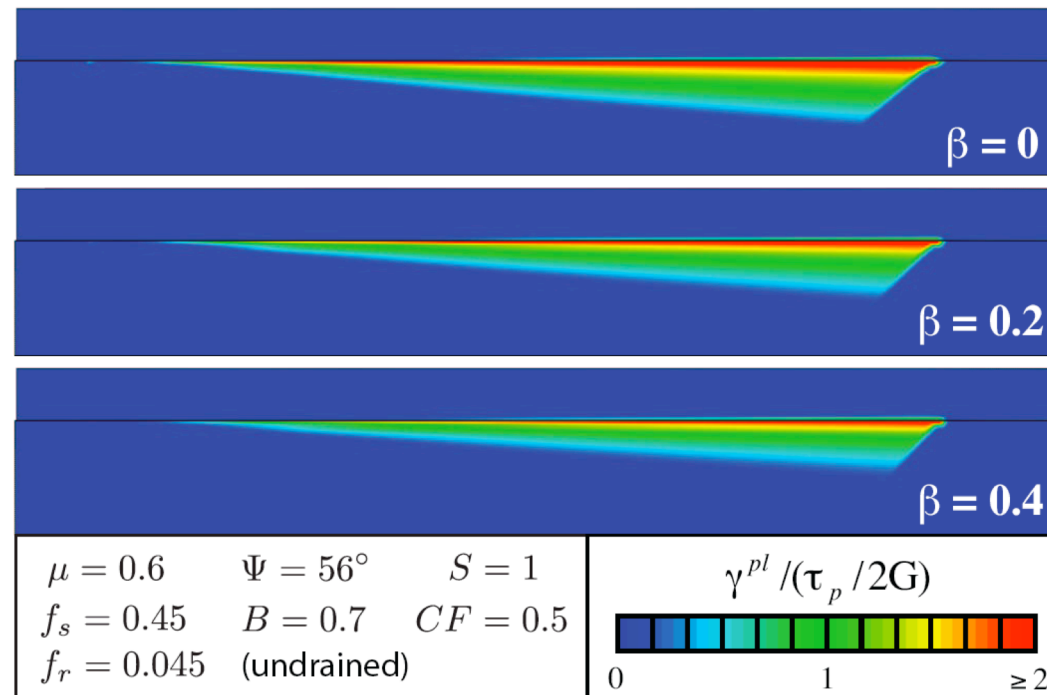
**$\Psi = 14^\circ$
 $B = 0.7$**



**← No plastic
dilatancy**

**} Some
dilatancy**

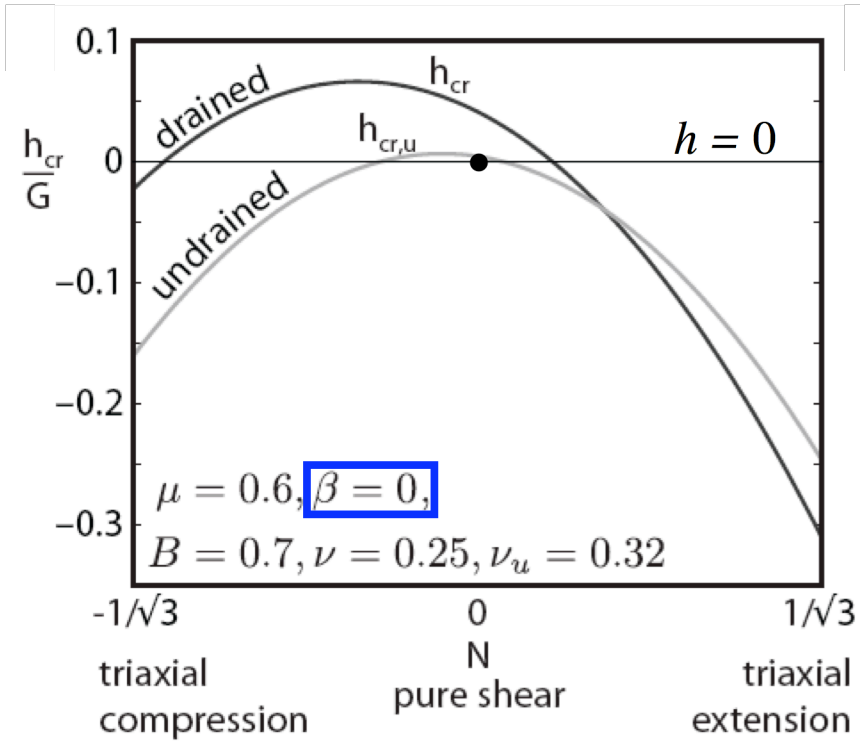
**$\Psi = 56^\circ$
 $B = 0.7$**



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dilatancy**

Suppression of localization



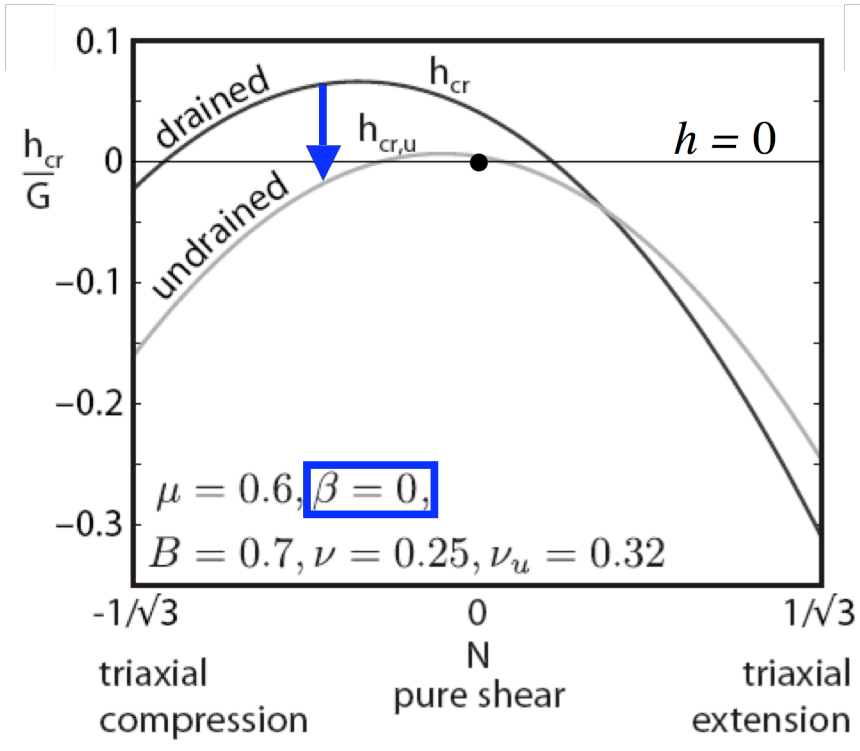
Rudnicki and Rice (1975): A **critical hardening h_{cr}** exists below which **localization is expected to occur**.

In our simulations: **$h = 0$**

Viesca et al. (2008)

No plastic dilatancy

Suppression of localization



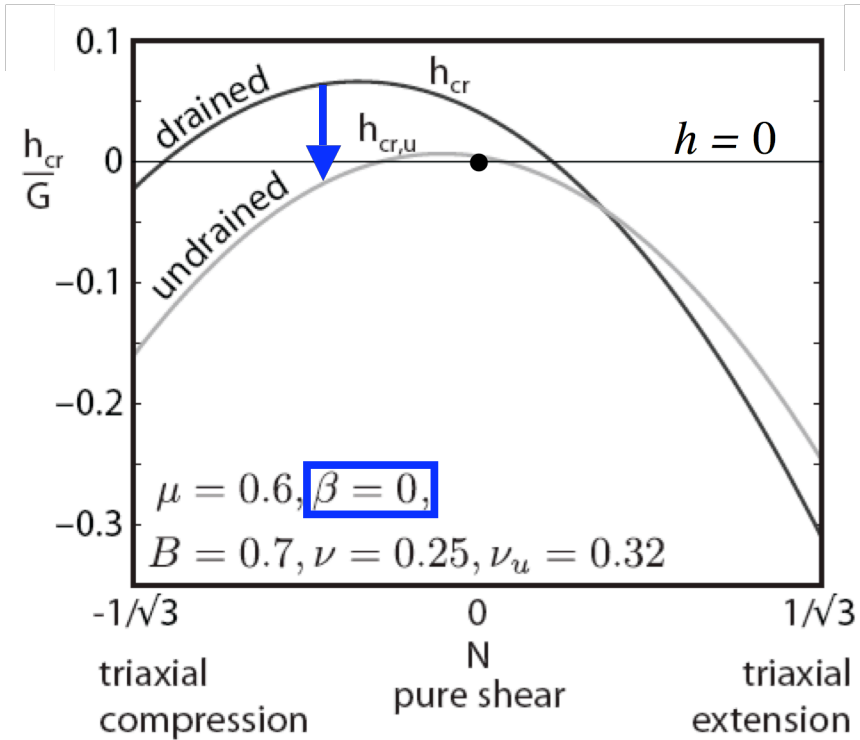
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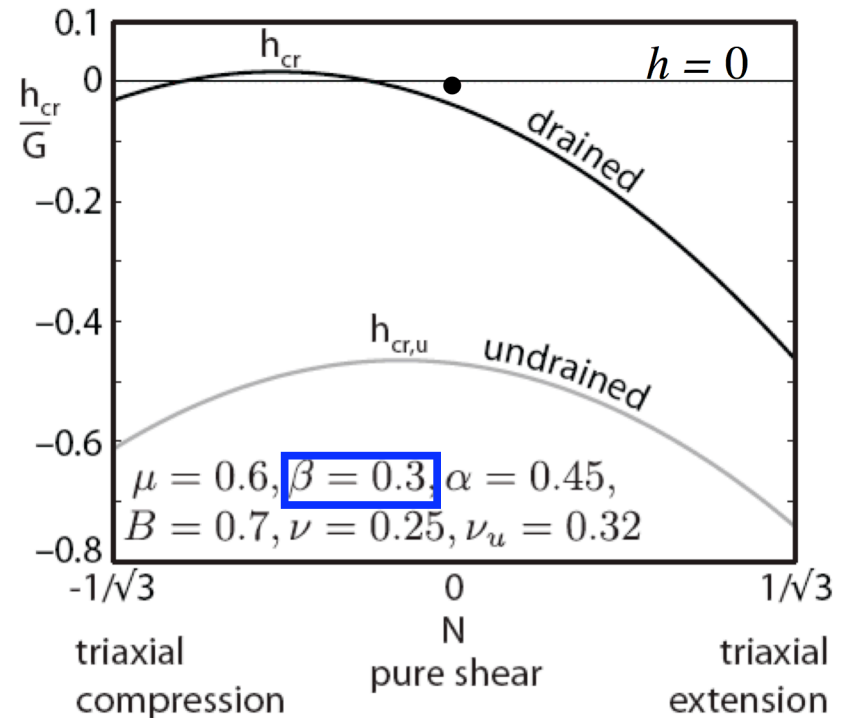
Viesca et al. (2008)

No plastic dilatancy

Suppression of localization



No plastic dilatancy

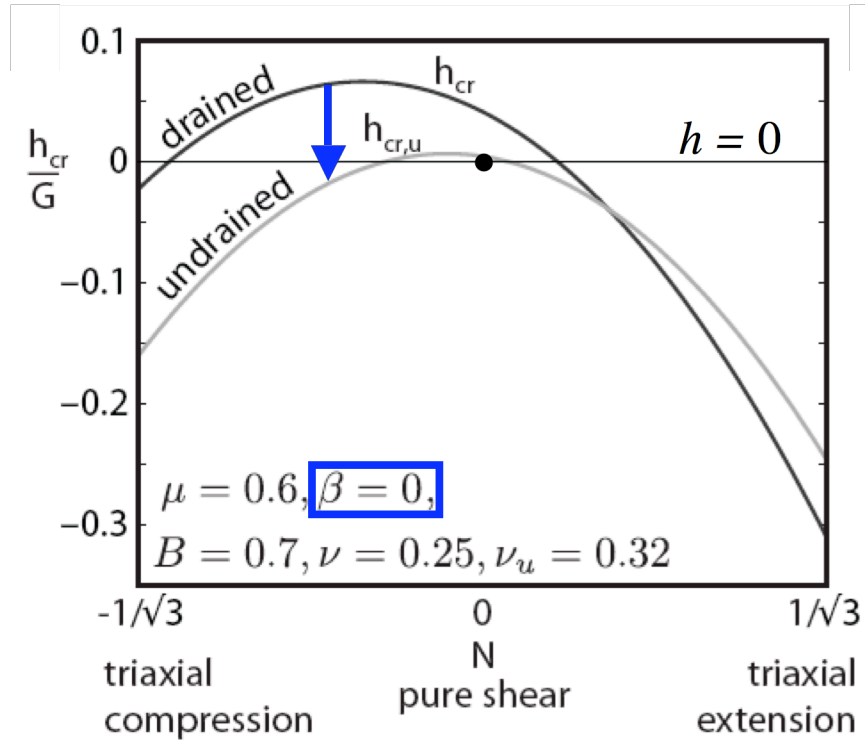


With plastic dilatancy

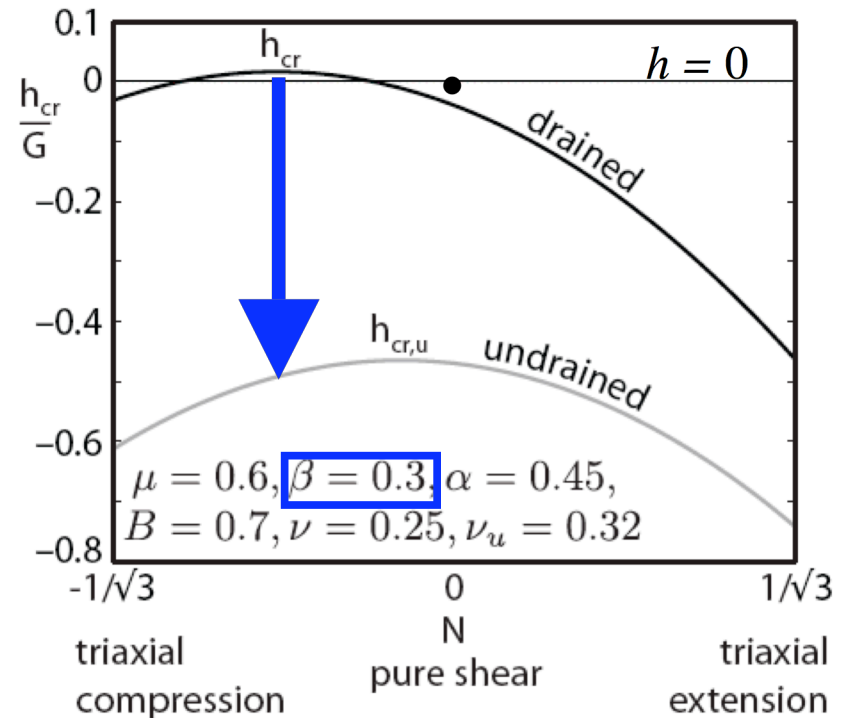
Viesca et al. (2008)

Dilatancy limits localization.

Suppression of localization



No plastic dilatancy



With plastic dilatancy

Viesca et al. (2008)

Dilatancy limits localization.

What happens at the slipping surface?

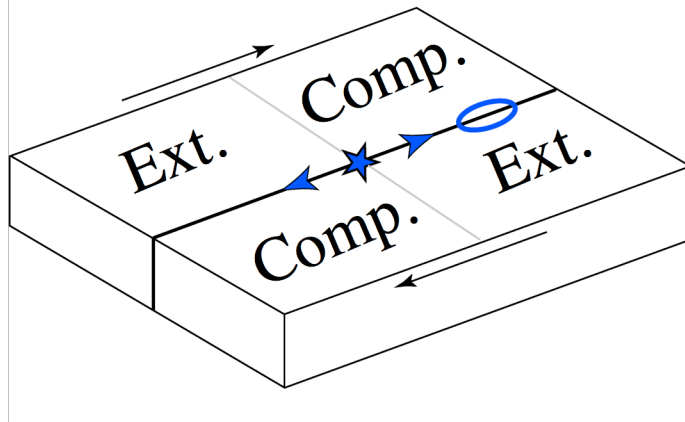
What happens at the slipping surface?

Previously, we neglected pore
pressure change on slip surface

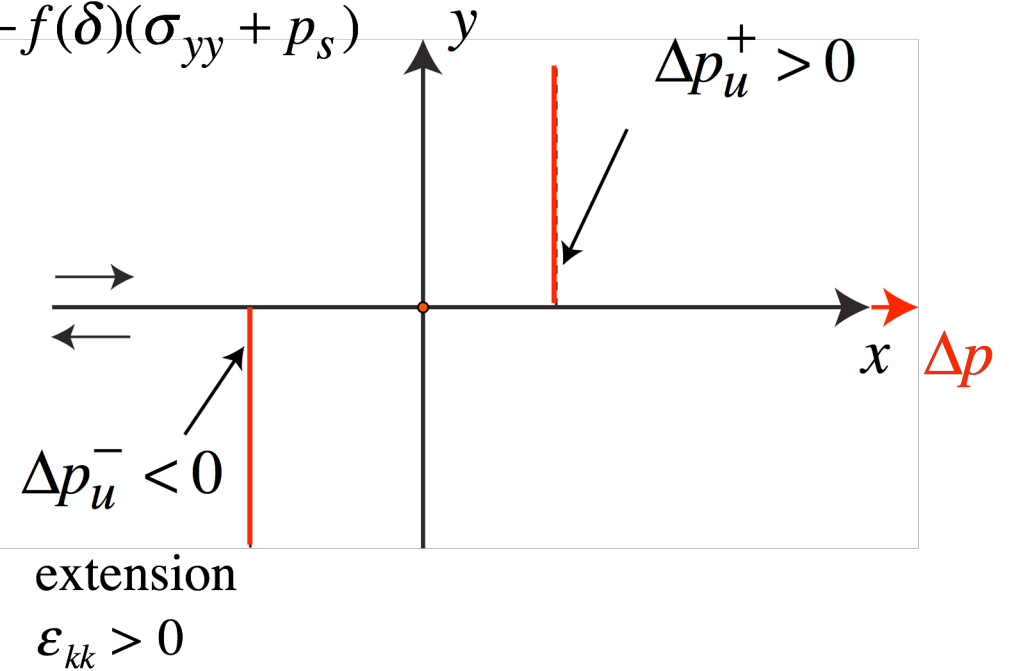
$$\tau = -f(\delta)(\sigma_{yy} + p_s)$$

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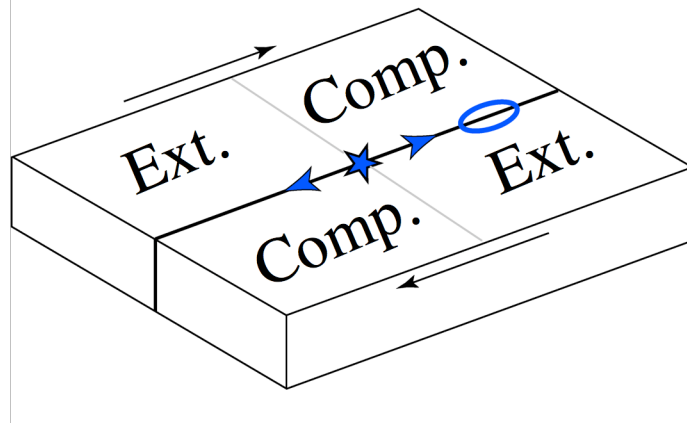
$$\tau = -f(\delta)(\sigma_{yy} + p_s)$$



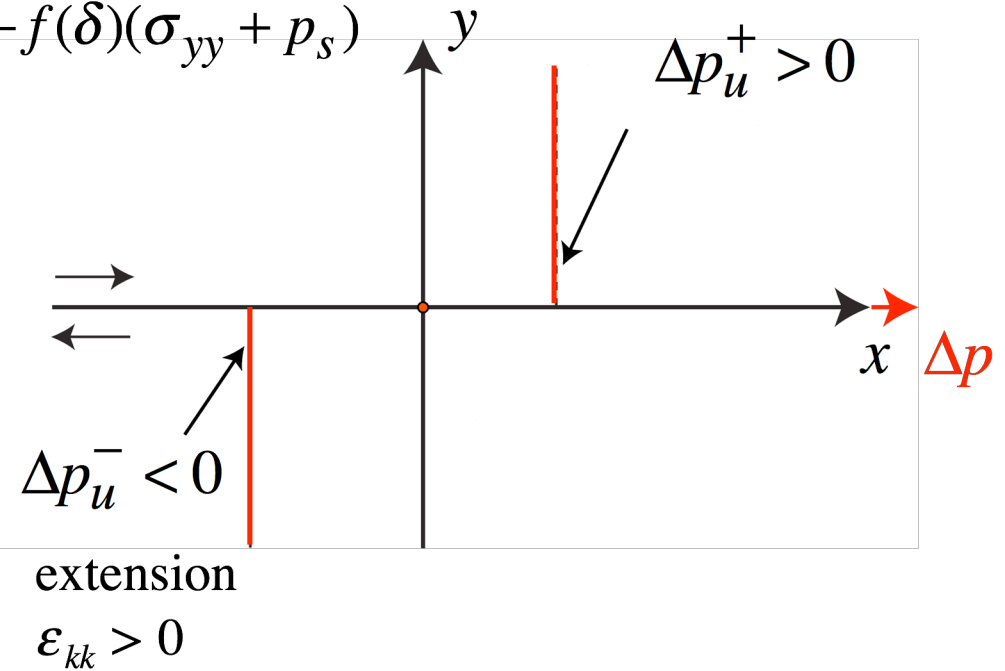
Undrained conditions \rightarrow discontinuity in pore pressure at slip surface

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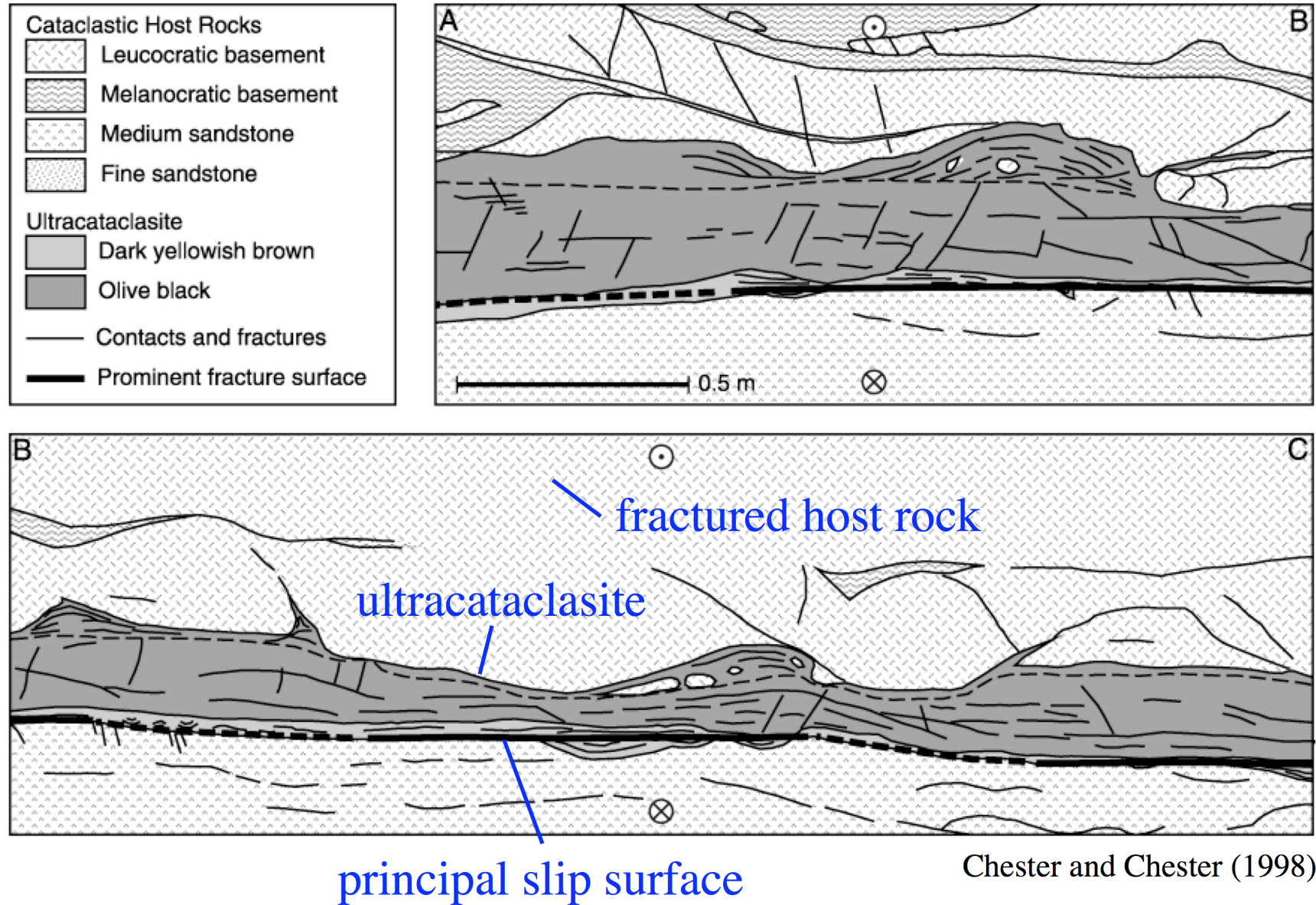


Undrained conditions → discontinuity in pore pressure at slip surface

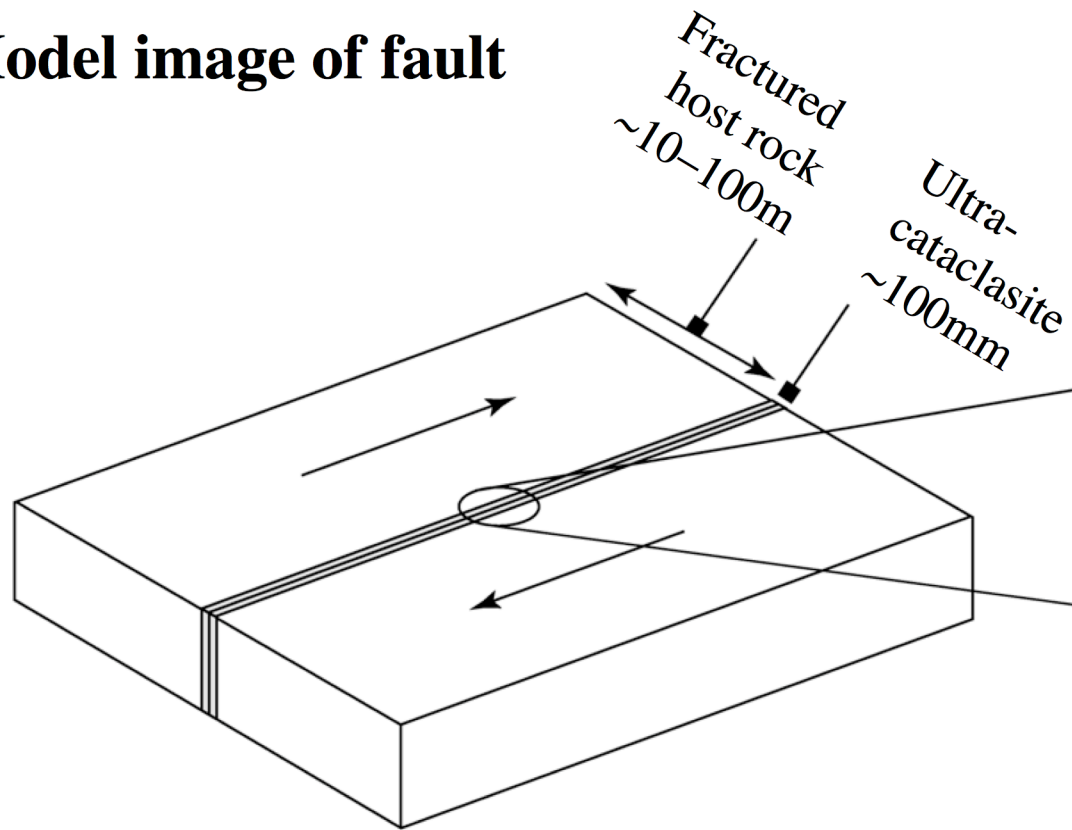
However, pore pressure should be continuous.

Will that lead to a pressure decrease or increase on the surface?
(strengthening) (weakening)

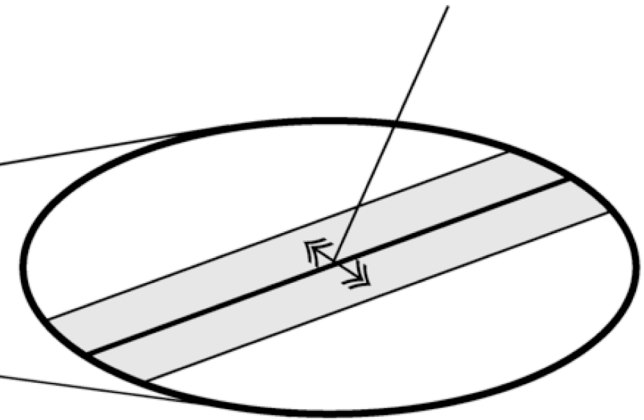
Fault observations: material surrounding principal slip surface



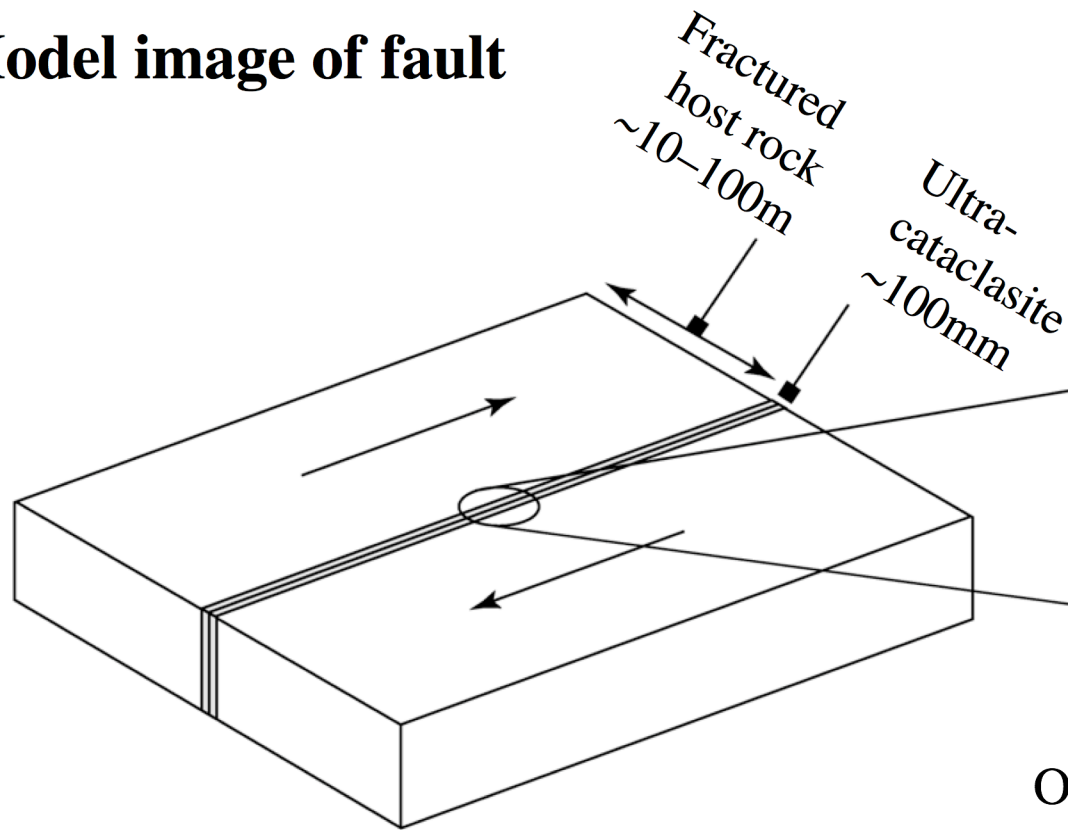
Model image of fault



Principal slip surface may lie within or to one side of ultracataclasite



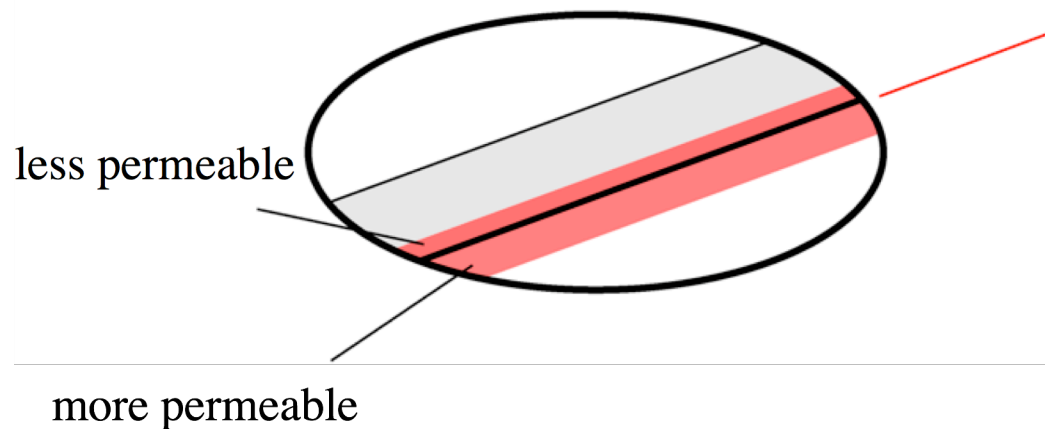
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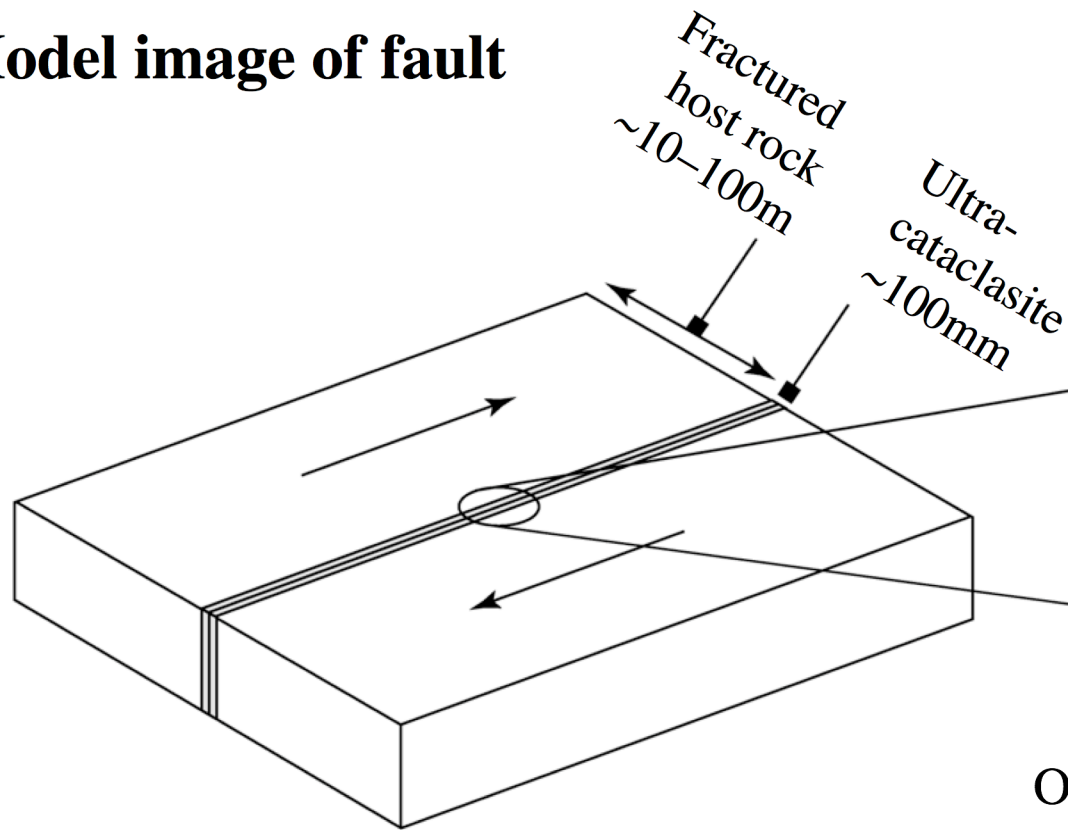
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Slip surface localized to one side:

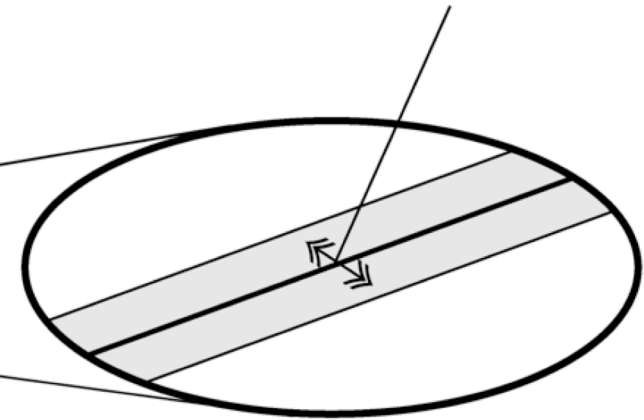
On short timescale of rupture, **diffusive region of O(mm–cm)** contributes to surface pore pressure



Model image of fault

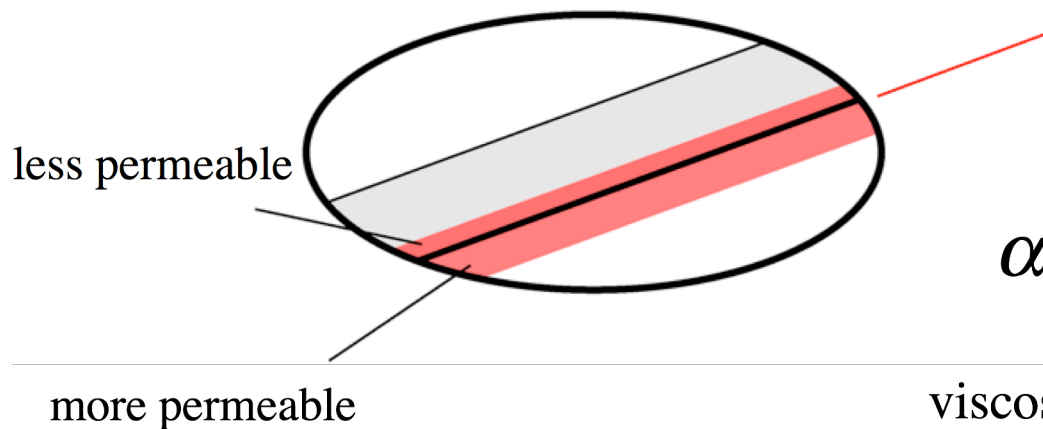


Principal slip surface may lie within or to one side of ultracataclasite



Slip surface localized to one side:

On short timescale of rupture, **diffusive region of O(mm-cm)** contributes to surface pore pressure



region size $\sim \sqrt{\alpha_{hy} t}$

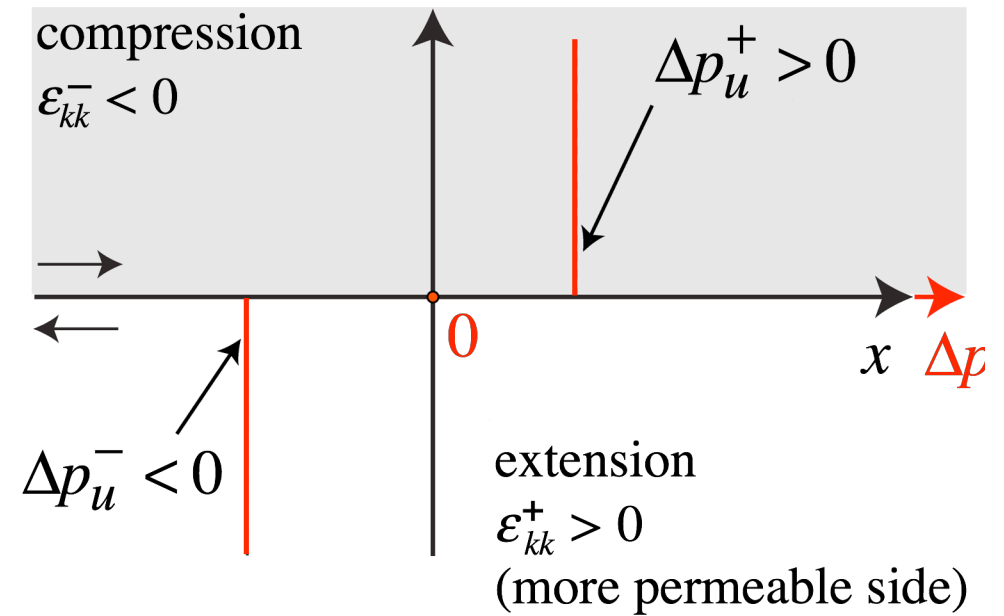
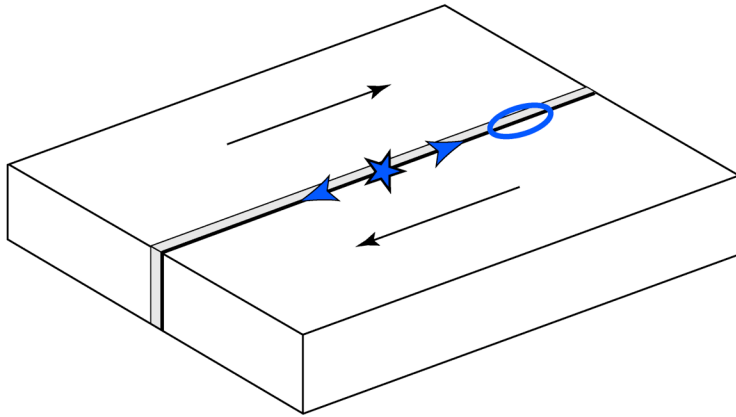
$$\alpha_{hy} = \frac{k}{\eta \beta_{stor}}$$

permeability

viscosity

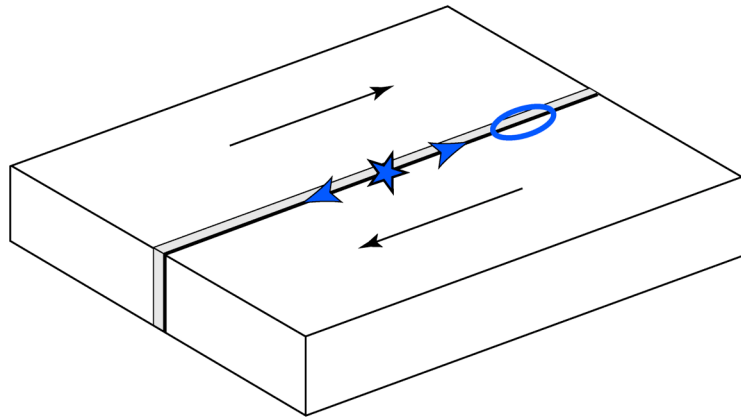
storage (compressibility)

Effects of near-fault fluid flow: poroelastic material

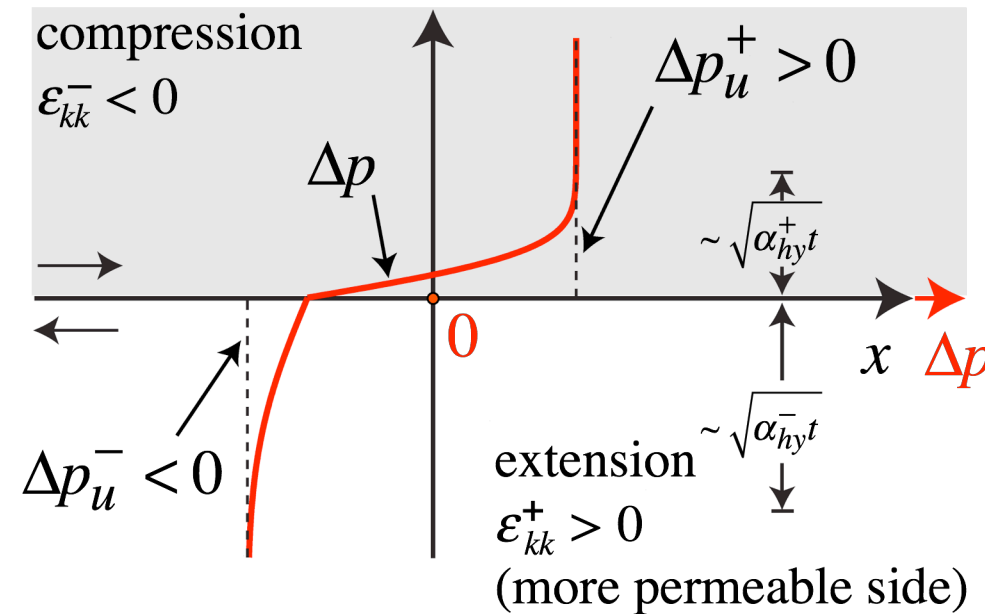


modified from Dunham and Rice (2008)

Effects of near-fault fluid flow: poroelastic material

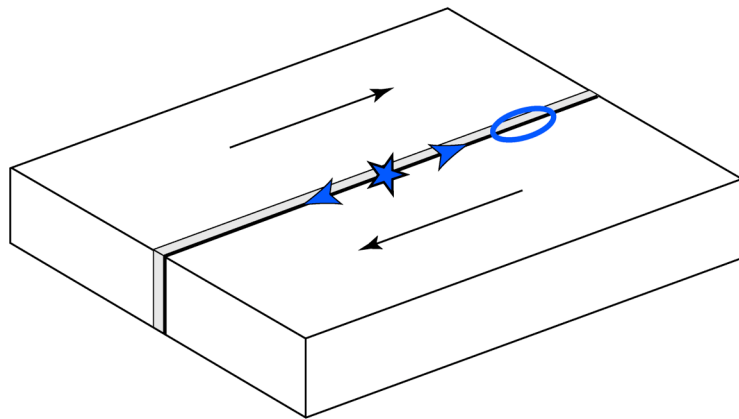


More permeable side wins:
its extension induces suction
(strengthening)

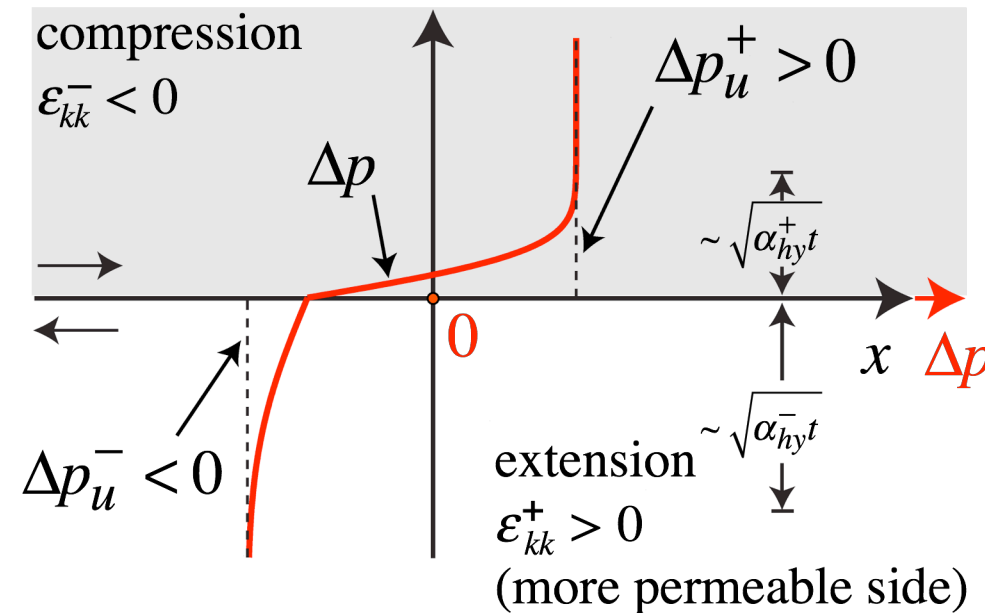


modified from Dunham and Rice (2008)

Effects of near-fault fluid flow: poroelastic material



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Pore pressure on the surface:

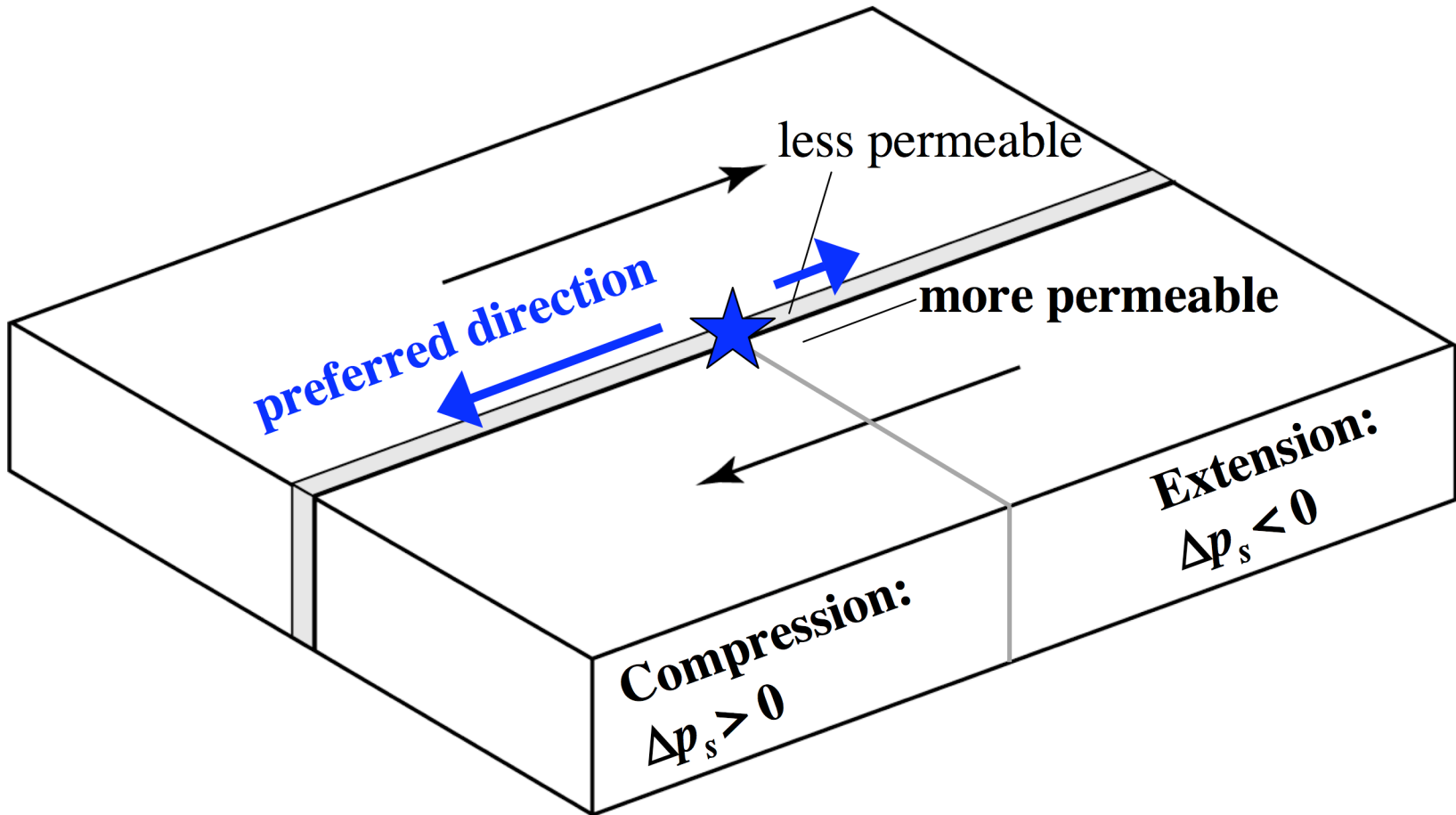
$$\Delta p_s = \zeta^+ \Delta p_u^+ + \zeta^- \Delta p_u^-$$

(Rudnicki and Rice 2006)

$$\text{where } \Delta p_u^\pm = -B^\pm \frac{\Delta \sigma_{kk}^\pm}{3}$$

and ζ^\pm are weights determined
by contrast in permeability, k ,
and storage coefficient β_{stor}^{el}

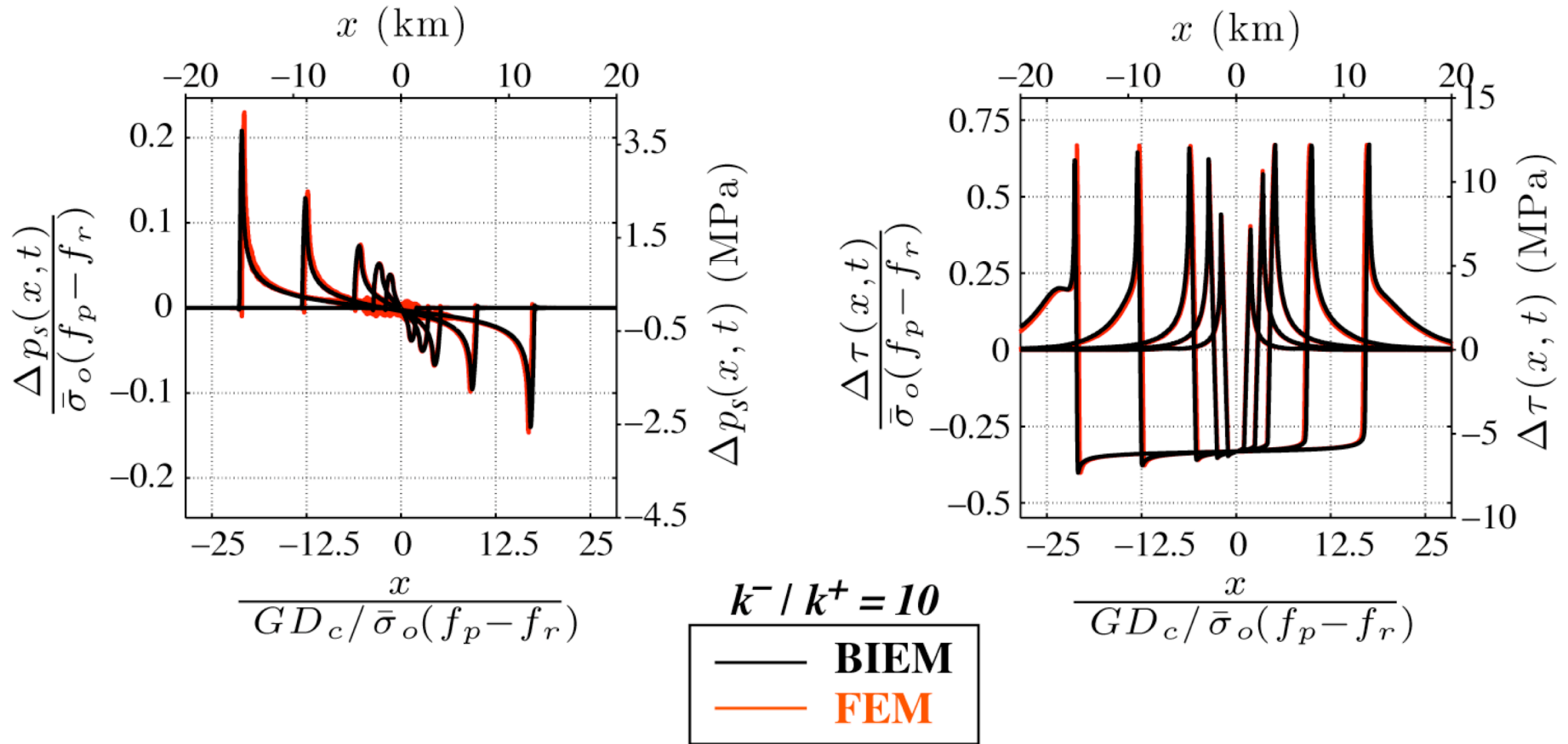
Permeability contrast induces preferred rupture direction



Dynamic plane-strain poroelastic rupture: snapshots in time

pore pressure change

shear stress change



BIEM from Dunham & Rice (2008)

Here, contrast in permeability leads to rupture direction preference.



Accounting for plastic deformation near slip surface

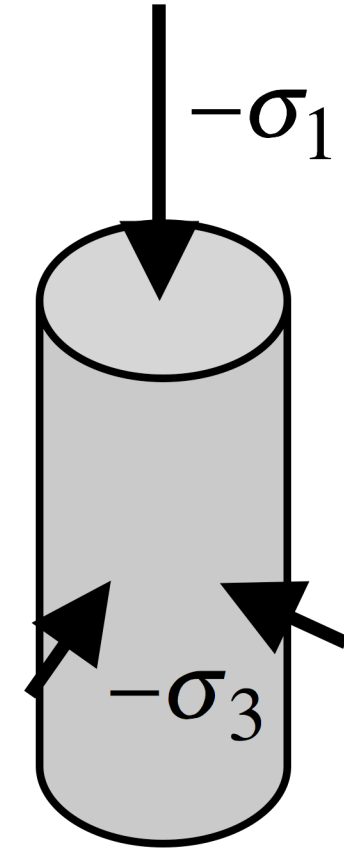
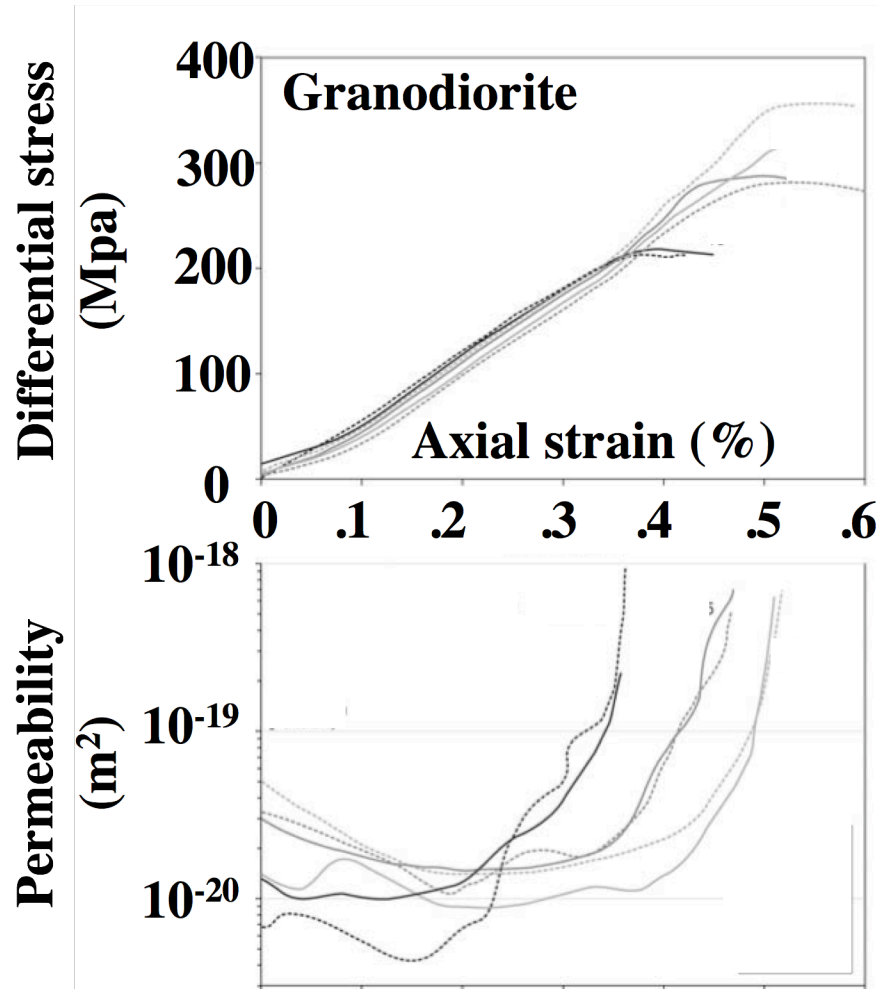
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Differential stress:

$$-(\sigma_1 - \sigma_3)$$

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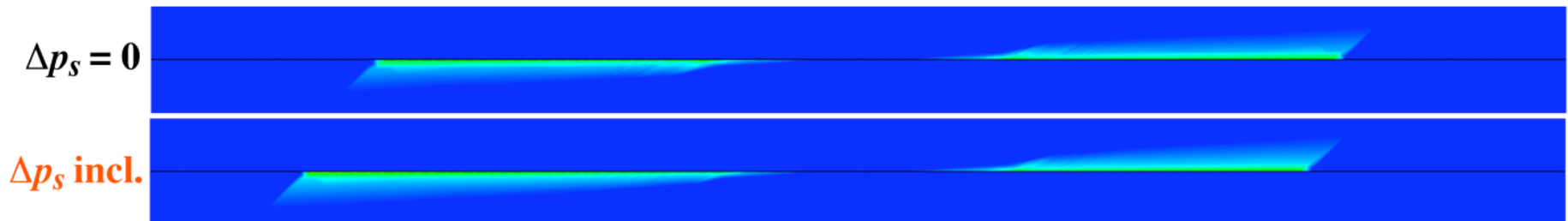
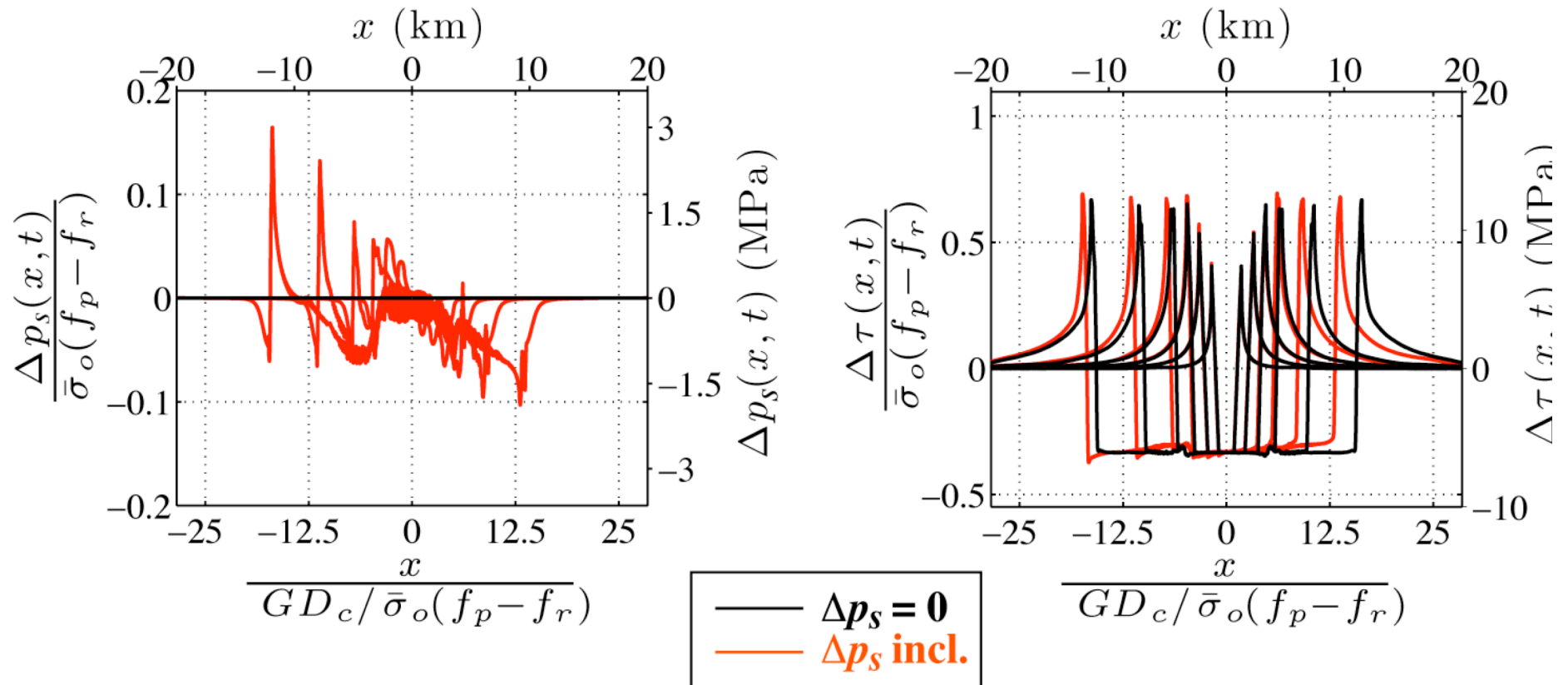
With simplifications, find similarity to poroelastic case

$$\alpha_{hy}^{pl}(t) = \frac{k(t)}{\eta\beta_{stor}^{pl}} \quad \text{Viesca \& Rice (2009, proceedings in press)}$$

Next, approximate surface pore pressure accounting for some of the above
(here neglect evolution of k)

using weighting similar to poroelastic case: $dp_s = \xi^+ dp_u^+ + \xi^- dp_u^-$

Does plastic deformation near the PSS affect rupture dynamics?



Poroelastic directivity preserved

Conclusions

- **Location** of plastic straining depends on angle, Ψ , of most compressive principal pre-stress:
 - For $\Psi < 10^\circ$, plastic strain on **compressional** side
 - For $\Psi > 45^\circ$, plastic strain on **extensional** side
- **Undrained pore fluid response:** $\Delta p = -B \Delta \sigma_{kk}/3$
 - increase plastic strain on compressional side
 - decrease plastic strain on extensional side
- **Undrained plastic dilatancy:** induces suction, decreases extent of plasticity
- For completely undrained deformation, fluid saturation **limits localization**.
- Poroelastic deformation can **change fault surface pore pressure** and propagation direction.
- Considering near-fault plastic deformation: **poroelastic directivity is preserved**.