



# **Megathrust friction in the 2010 Maule earthquake area in relation to forearc morphology and mechanical stability, and to earthquake rupture dynamics**

**Nadaya Cubas**

J.P. Avouac, N. Lapusta

Coll. : Y. Leroy, P. Souluoumiac

# **Megathrust friction in the 2010 Maule earthquake area**

1. Introduction

2. From the Critical Taper Theory

3. From Limit Analysis

4. From Dynamic Simulation of EQ cycle

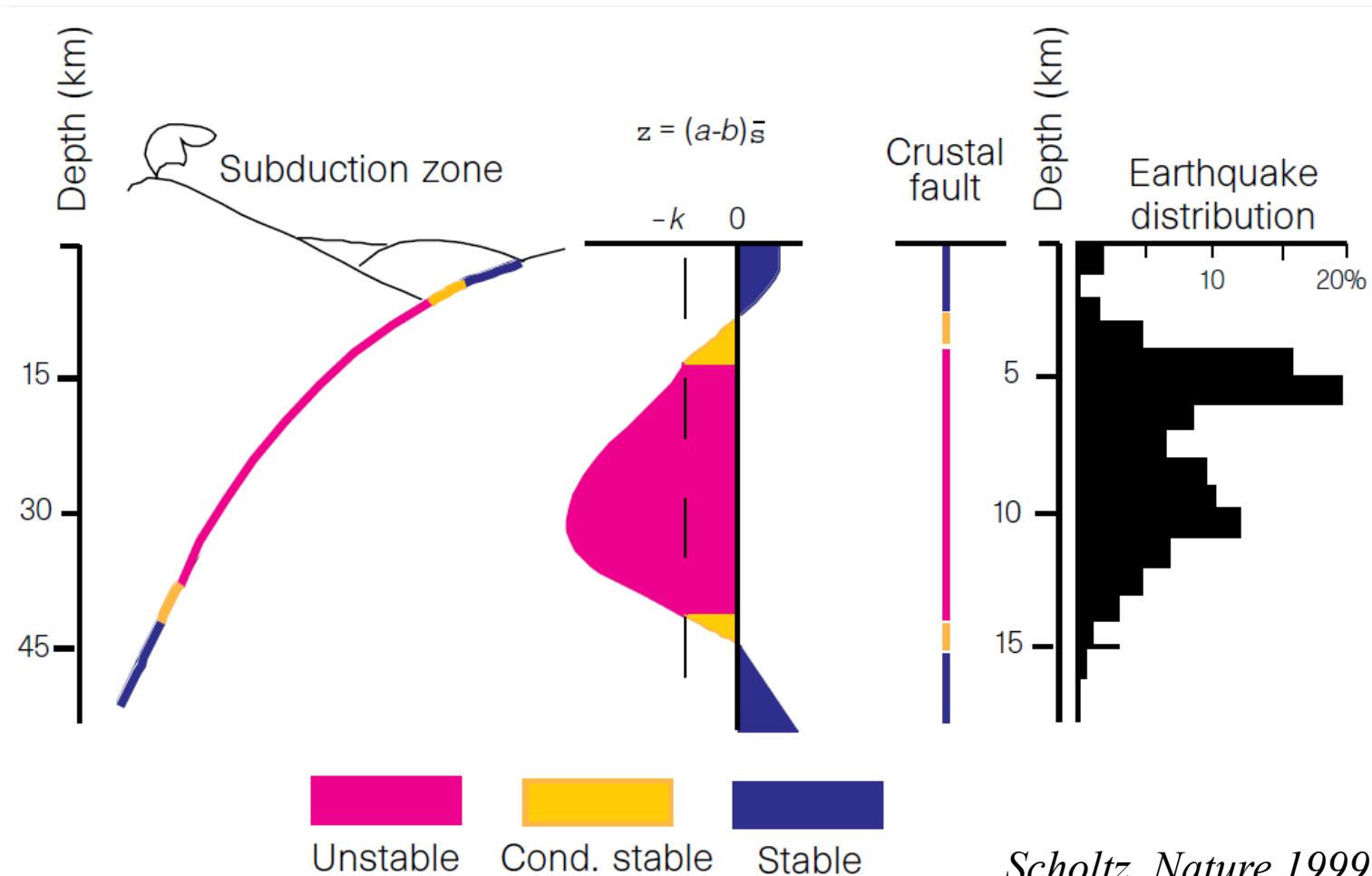
# 1. Introduction

## Spatial variations of frictional properties: Rate-and-state laws

$$\mu_{ss} = \tau/\sigma = \mu_* + (a-b) \ln(V/V_*)$$

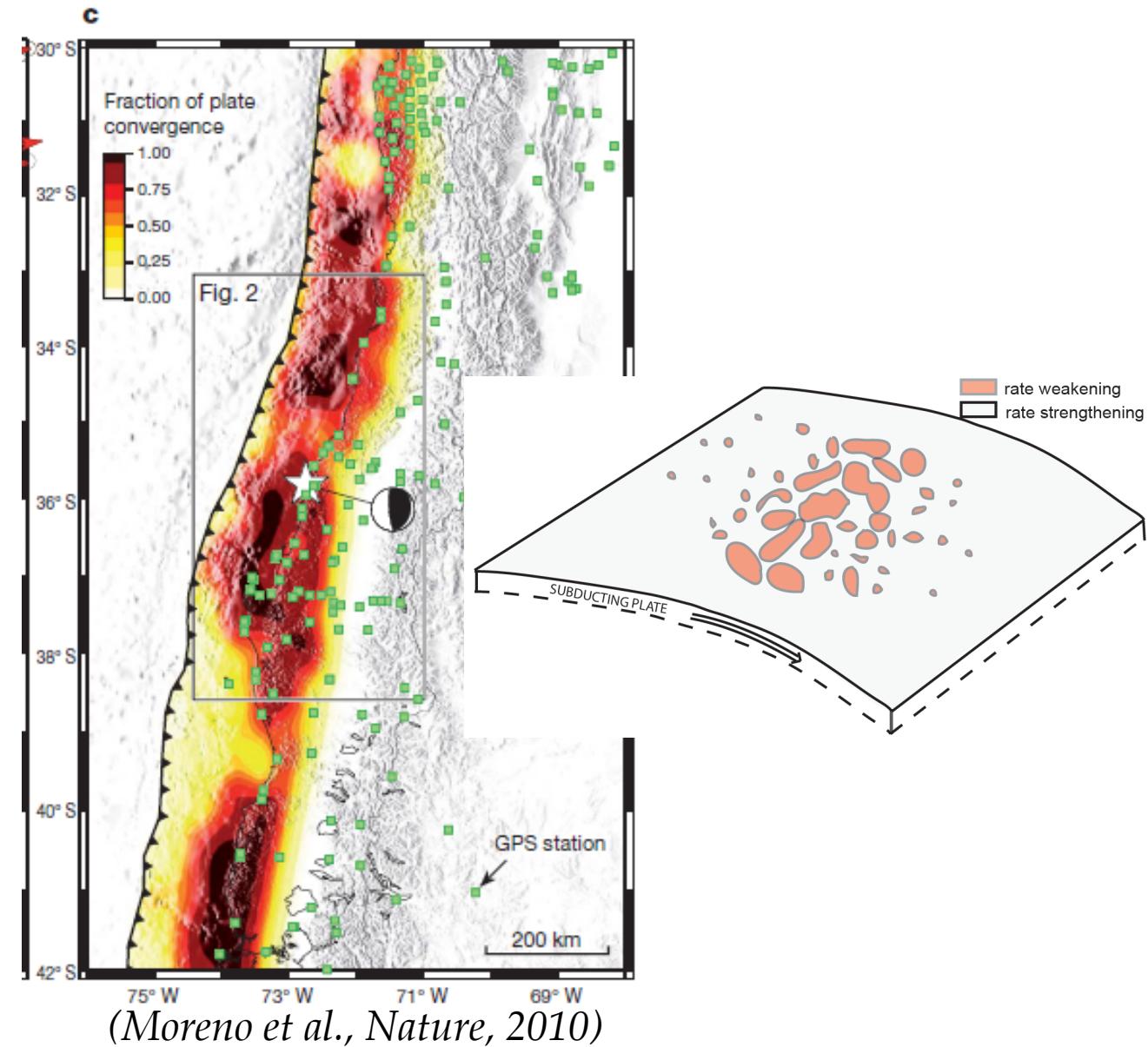
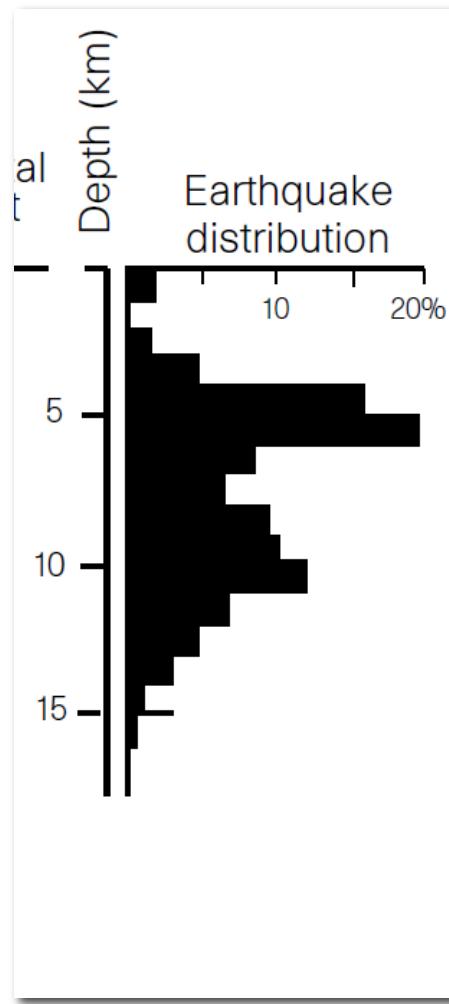
$(a-b) > 0$  rate-strengthening :  $\mu_s < \mu_d$

$(a-b) < 0$  rate-weakening :  $\mu_s > \mu_d$

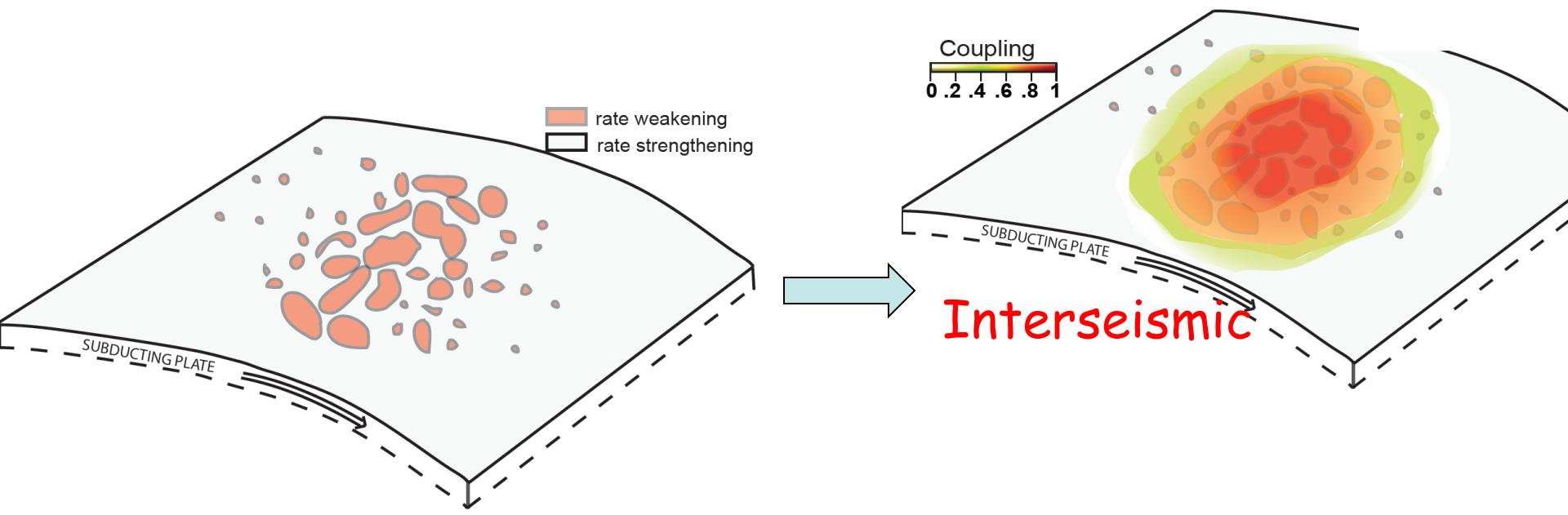


# 1. Introduction

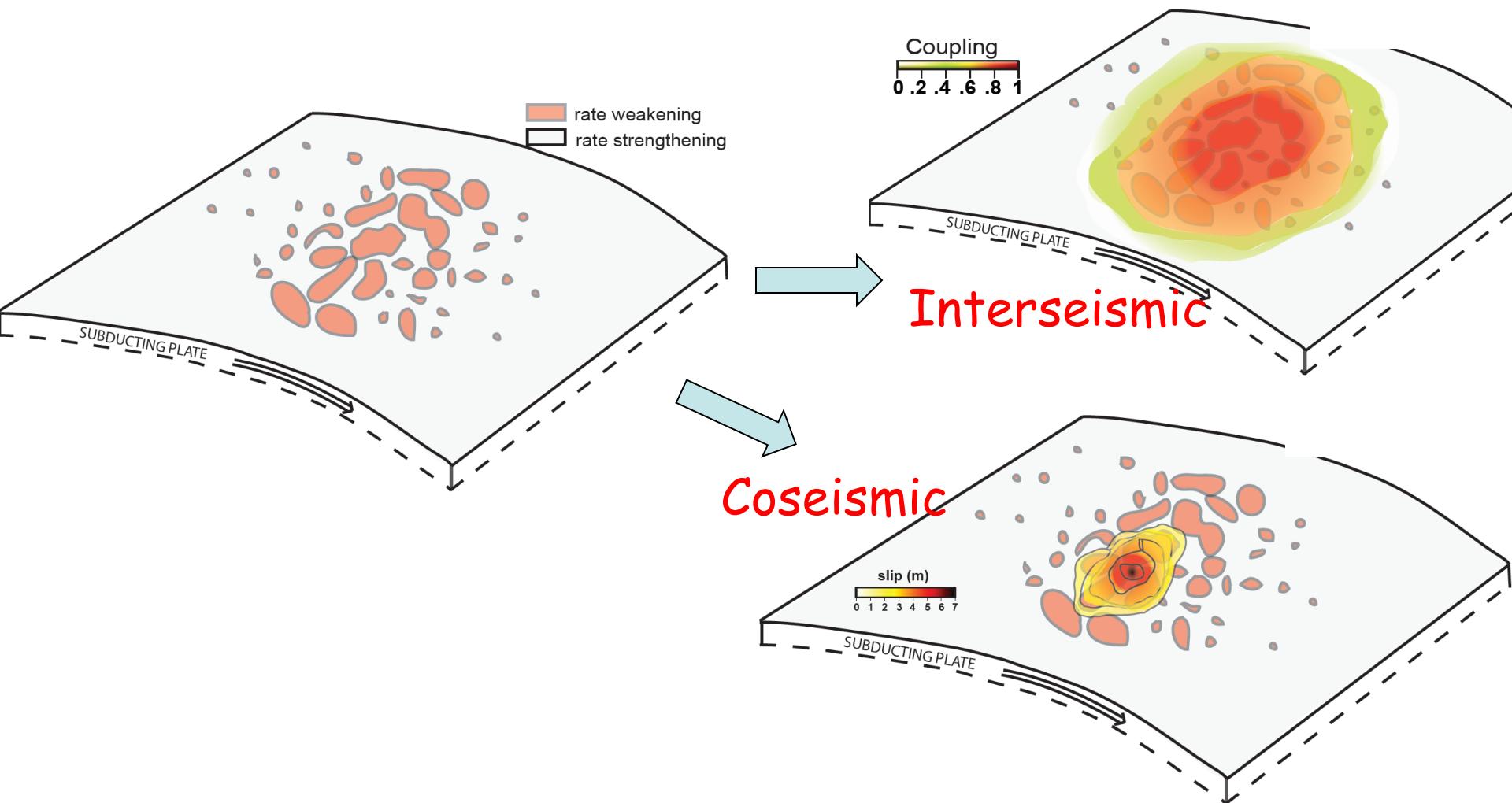
## Spatial variations of frictional properties: Interfingering patches



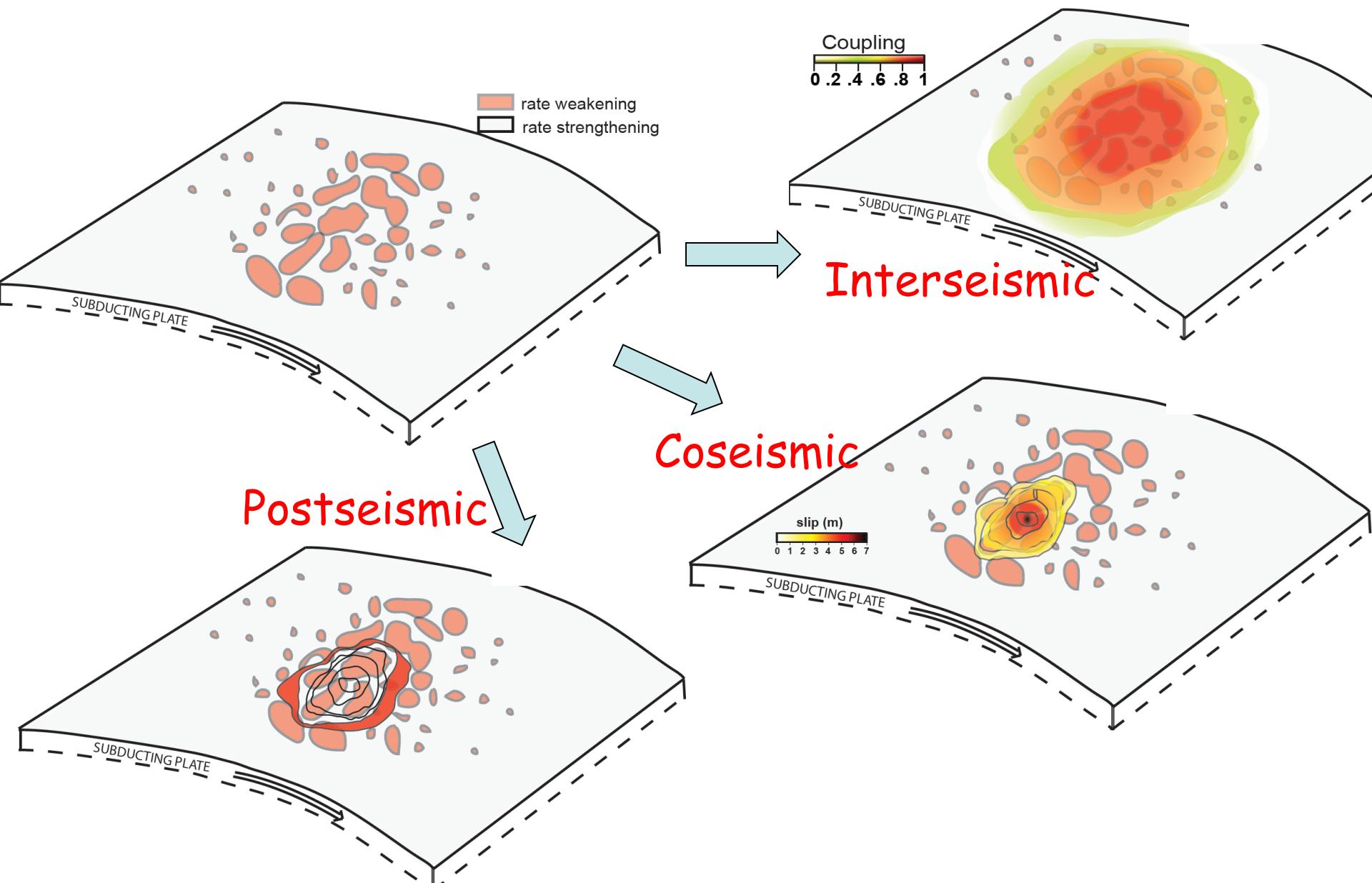
# 1. Introduction



# 1. Introduction



# 1. Introduction



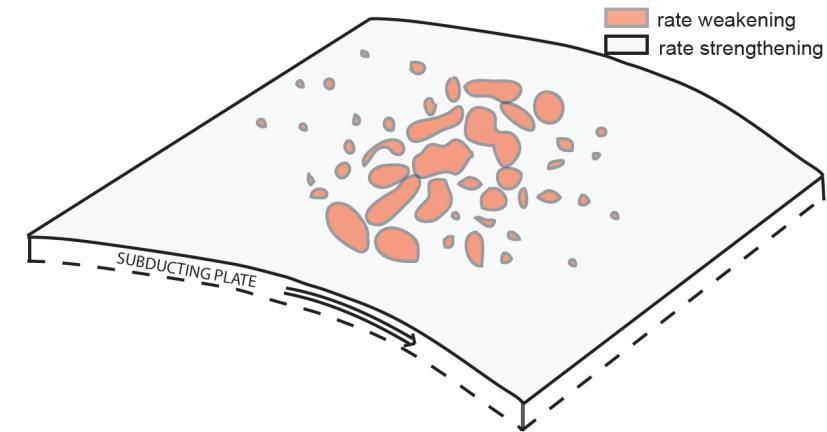
# 1. Introduction

## Objective :

Spatial variations of fault friction: observations  
and implication for fault dynamics

develop realistic (predictive?) dynamic  
models of the seismic cycle.

$$\mu_{ss} = \tau/\sigma = \mu_* + (a-b) \ln(V/V_*)$$



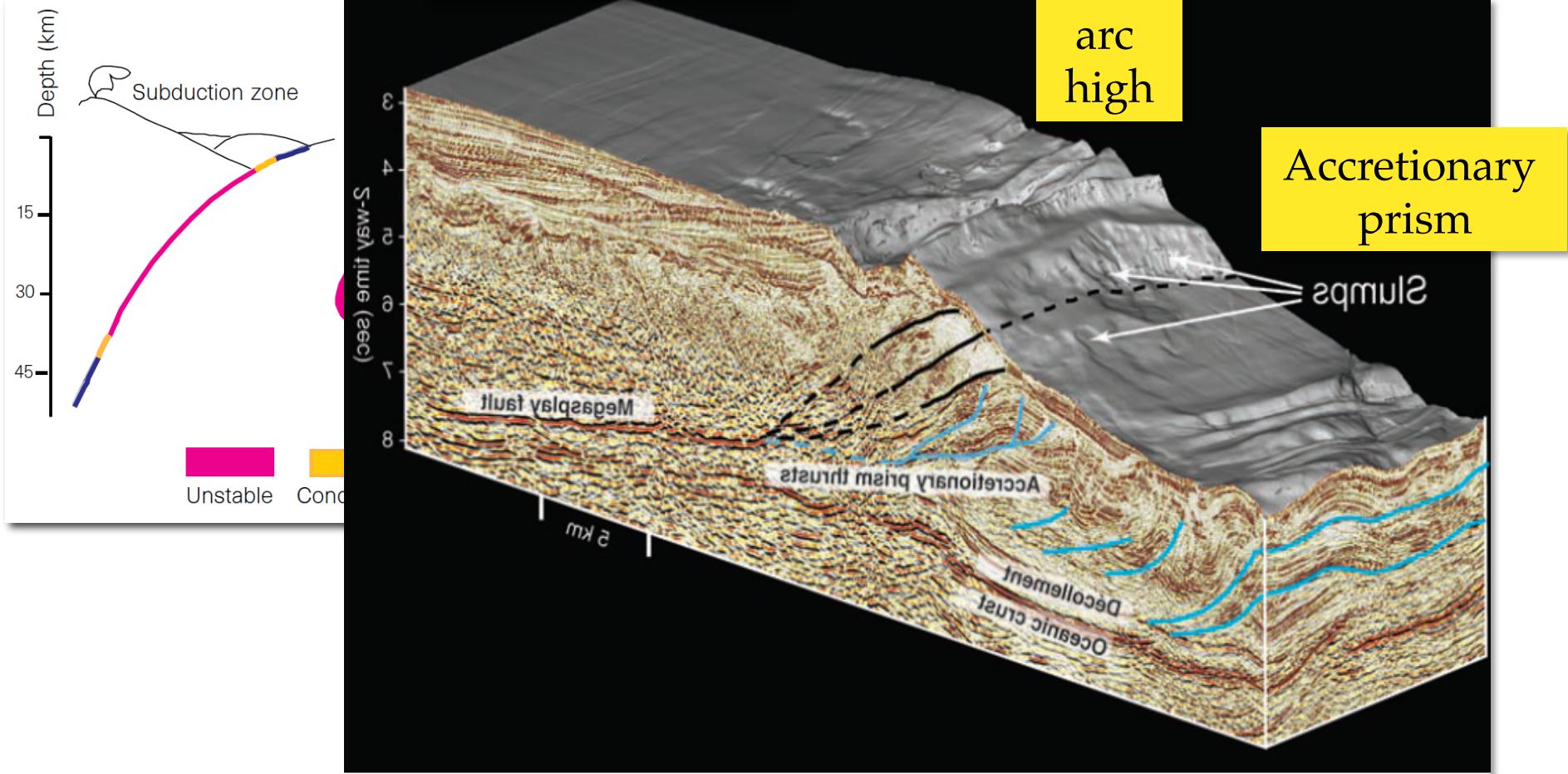
Some outstanding questions:

- What are the frictional properties of faults?
- How do these properties vary in space and time?
- How do they influence individual earthquakes or the long-term seismic behavior of a fault?

# 1. Introduction

## Morpho-tectonic segmentation of forearc

Nankai:

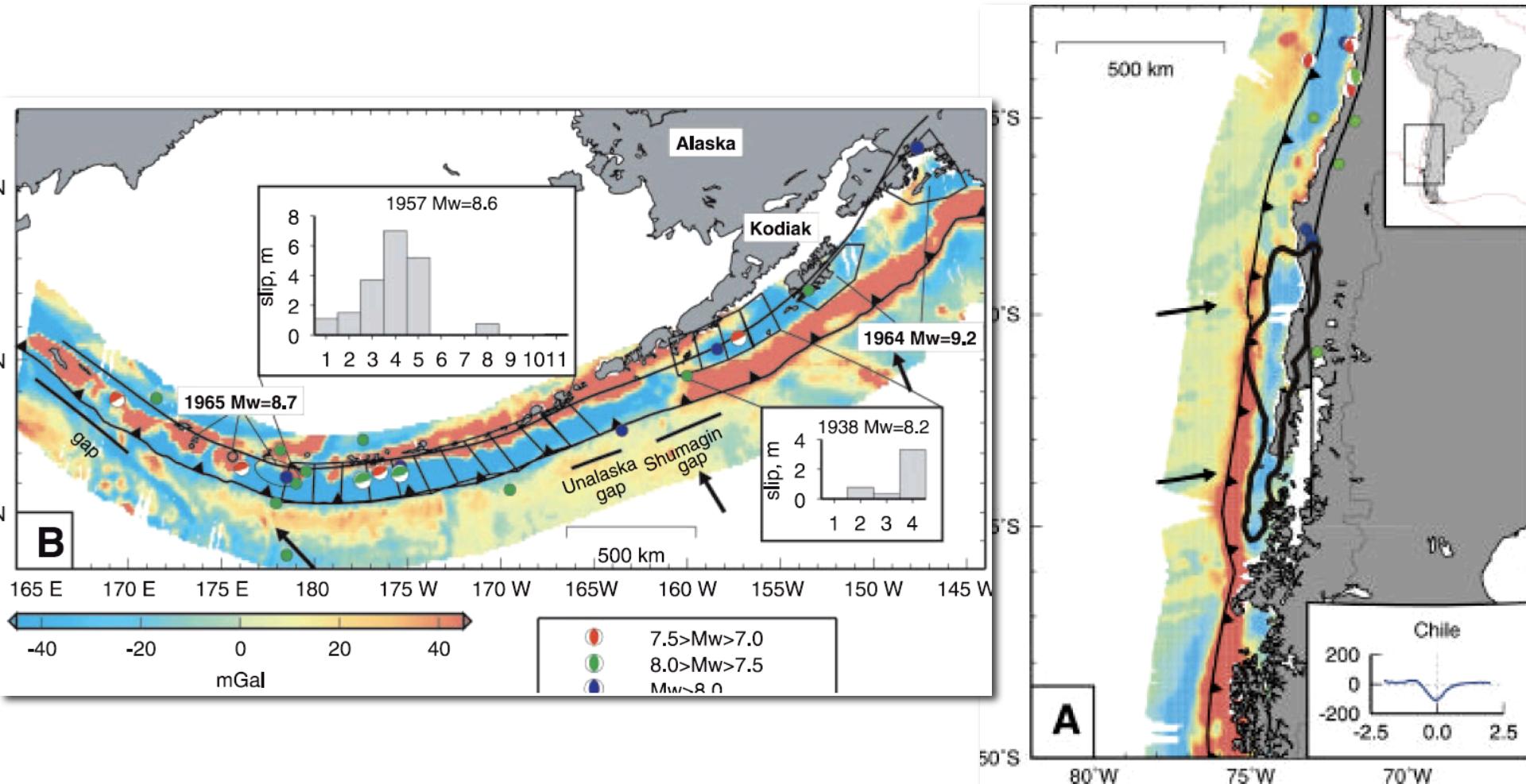


Moore et al., Science 2007

# 1. Introduction

## Spatial variations of frictional properties: Related to the forearc morphology

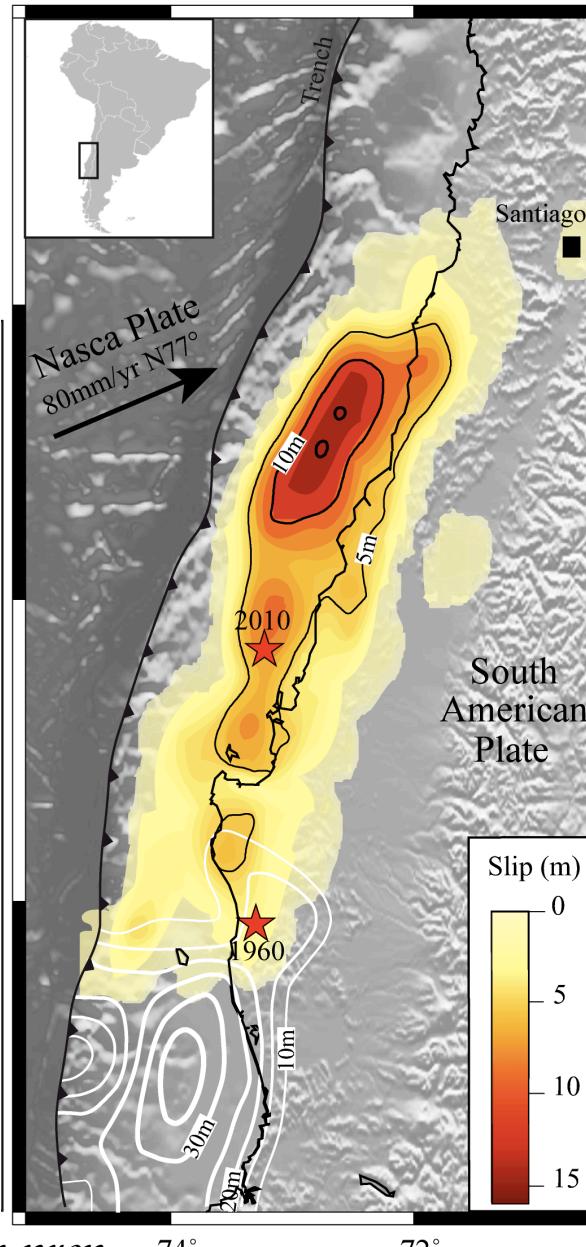
*Song & Simons, Science 2003*



Correlation between seismic asperities of great earthquakes and  
trench-parallel gravity anomaly

# 1. Introduction

## Maule 2010, Mw 8.8



Coseismic slip from Lin et al., in prep.  $-74^{\circ}$   $-72^{\circ}$

# **Megathrust friction in the 2010 Maule earthquake area**

1. Introduction

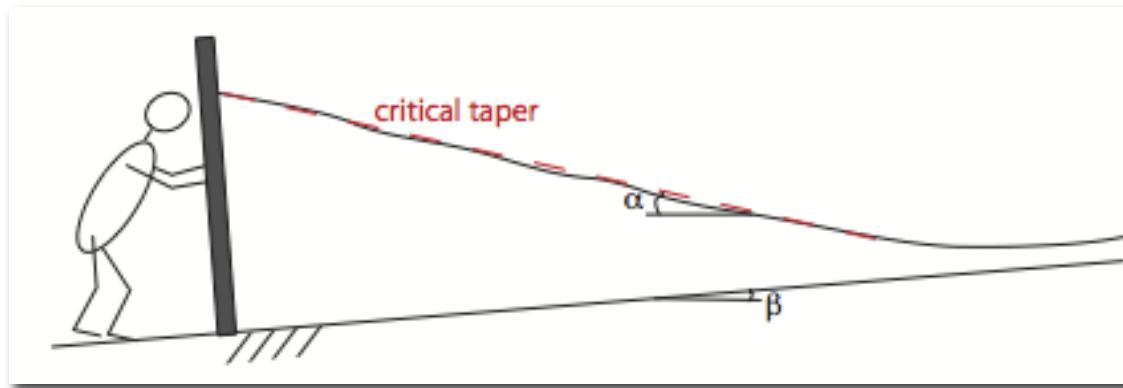
2. From the Critical Taper Theory

3. From Limit Analysis

4. From Dynamic Simulation of EQ cycle

## 2. Critical Taper

Analogue of sand wedges pushed by bulldozer:  
(Davis *et al.*, JGR 1983)



Nankai wedge :

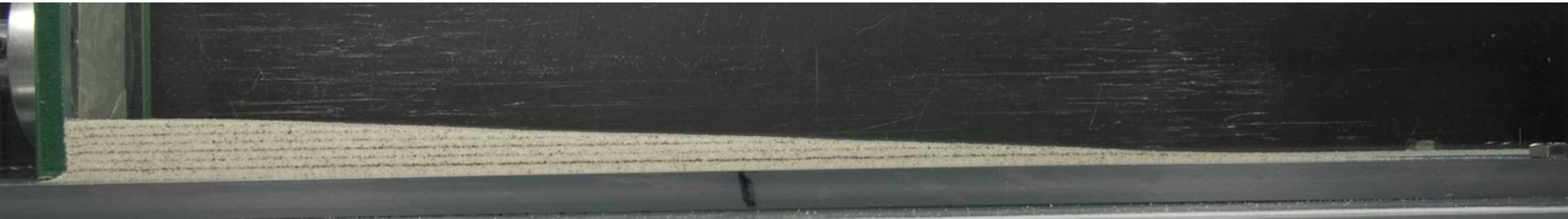


Morgan and Karig, 1994

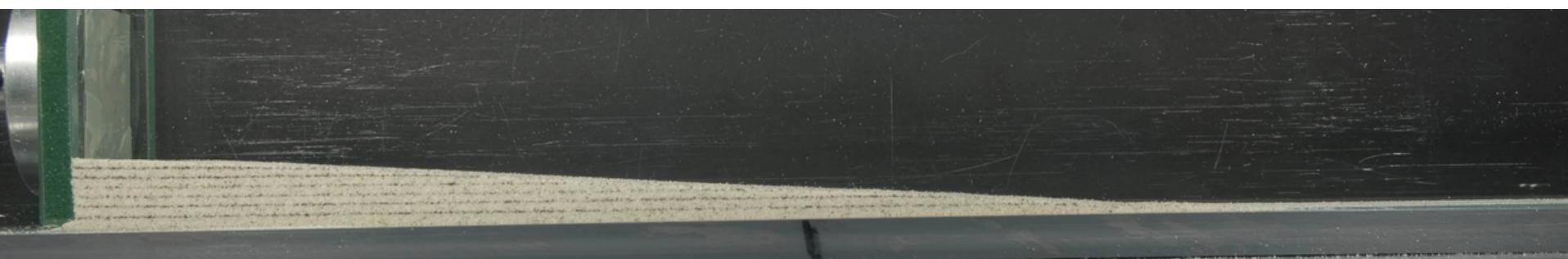
1km

## 2. Critical Taper

**Unstable / Sub-critical :**



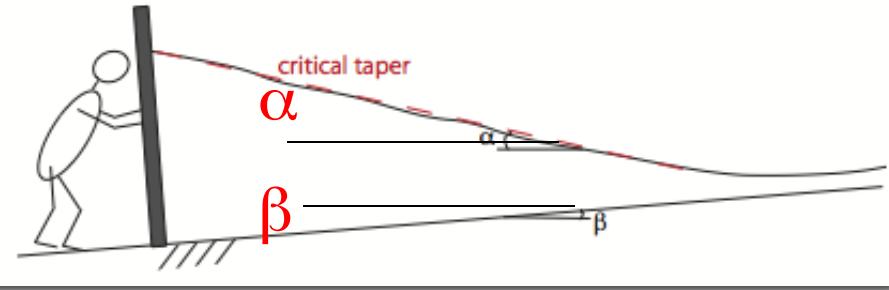
**Stable / over-critical :**



*Courtesy of Souloumiac P.*

## 2. Critical Taper

Theory (Dahlen, JGR 1984):



$$\boxed{\alpha_c} = \frac{1}{2} \arcsin\left(\frac{\sin\phi'_b}{\sin\phi_b}\right) - \frac{1}{2}\phi'_b - \frac{1}{2} \arcsin\left(\frac{\alpha'}{\sin\phi}\right) - \frac{1}{2}\alpha' - \boxed{\beta}$$

Critical topographic slope

Basal friction

Internal friction

Decollement dip

$$\mu = \tan\phi$$

$$\mu_b = \tan\phi_b$$

$$\mu'_b = \mu_b \frac{(1-\lambda_b)}{(1-\lambda)}$$

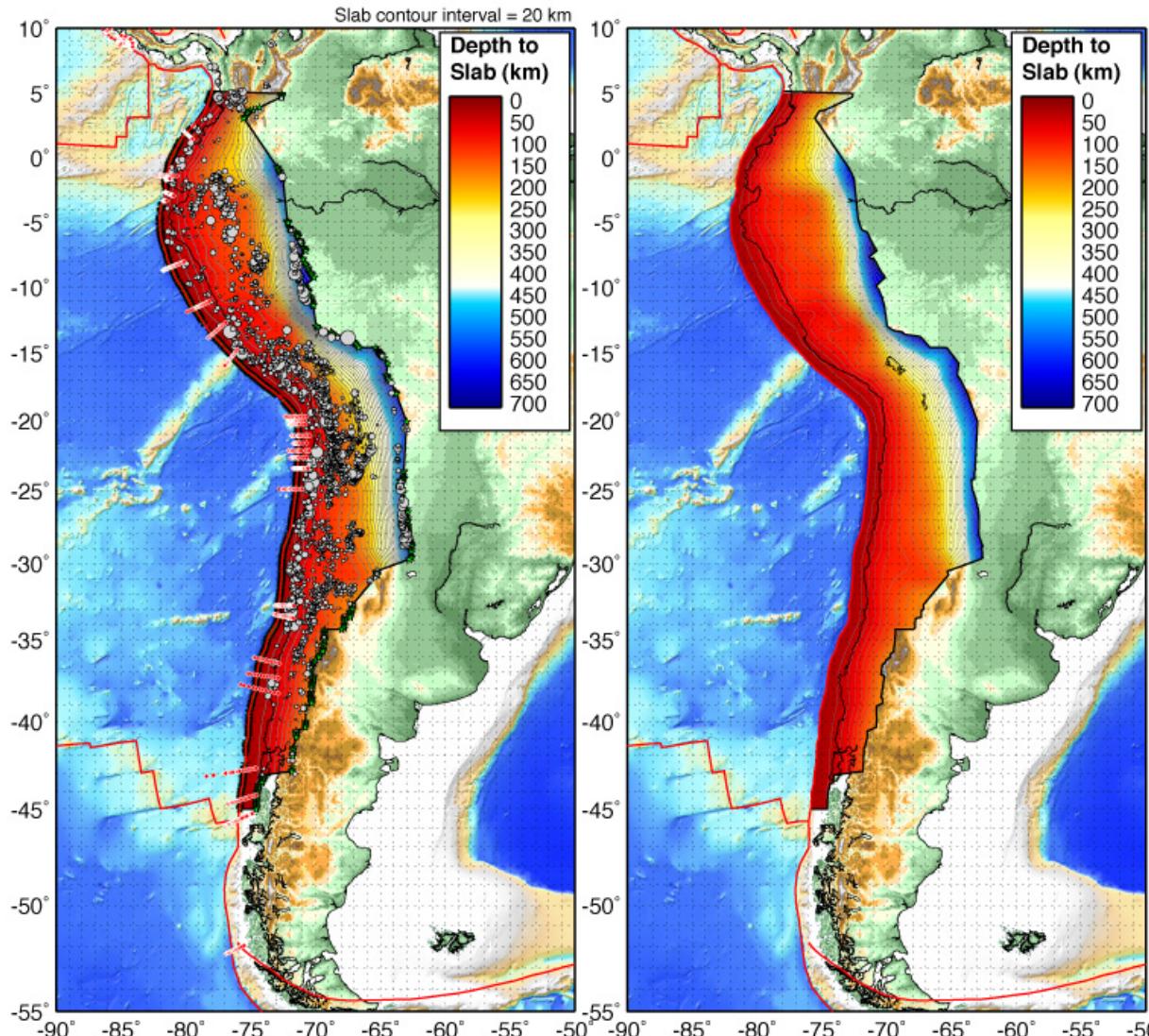
$$\mu' = \mu(1 - \lambda)$$

$$\alpha' = \arctan\left(\frac{1-\rho_w/\rho}{1-\lambda} \tan\alpha\right)$$

$$\Lambda \sim p_f / \sigma_z$$

## 2. Critical Taper

### Covariation $\alpha/\beta$ : Slab morphology (Hayes & Wald, GJI 2009)

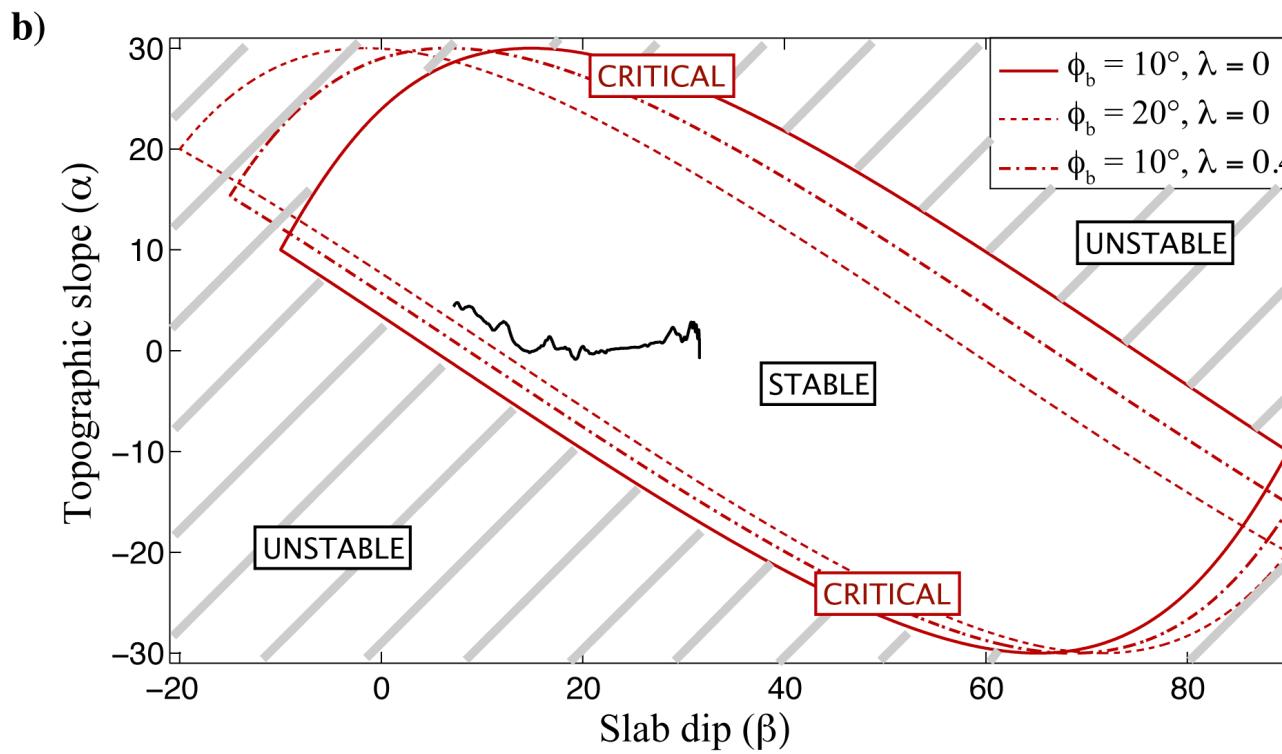
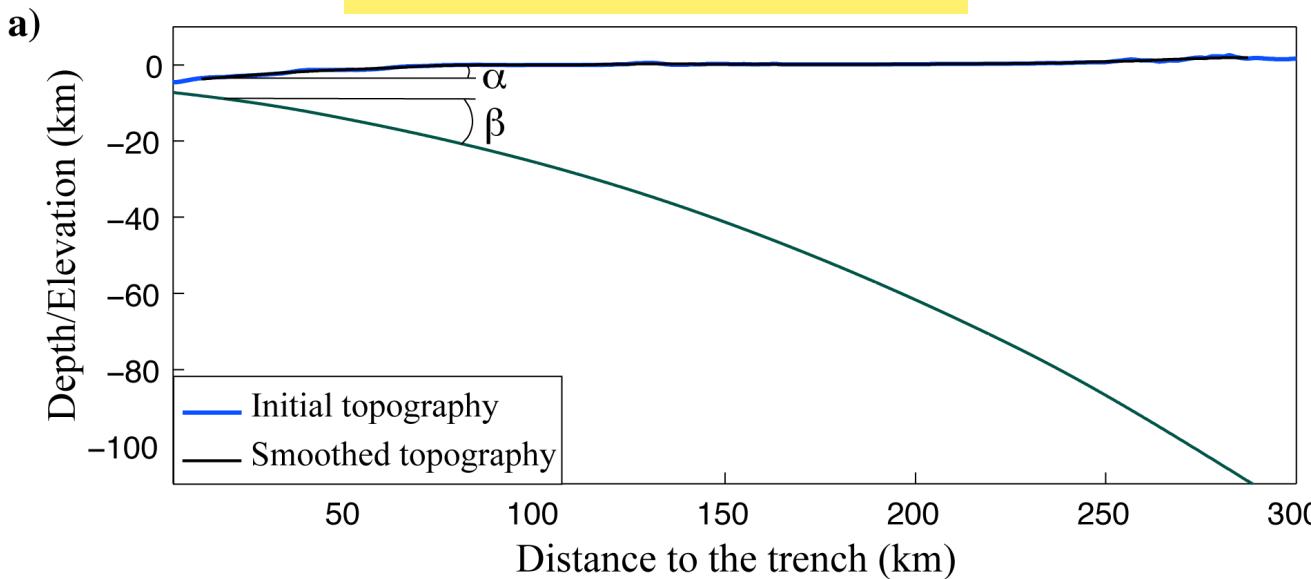


**Slab 1.0 :** Hayes & Wald, GJI 2009, construct probability density functions to solve for the 'most-likely' fault plane, by incorporating data from historic earthquake catalogues (gCMT, NEIC PDE and the global relocation catalogue of Engdahl et al. (1998)), locations of trench breaks on the seafloor (from the plate boundary files of Tarr et al. 2009) and any 'new' event location (both NEIC hypocentre and gCMT centroid)

**Topography :** ETOPO1, Amante and Eakins, 2009.

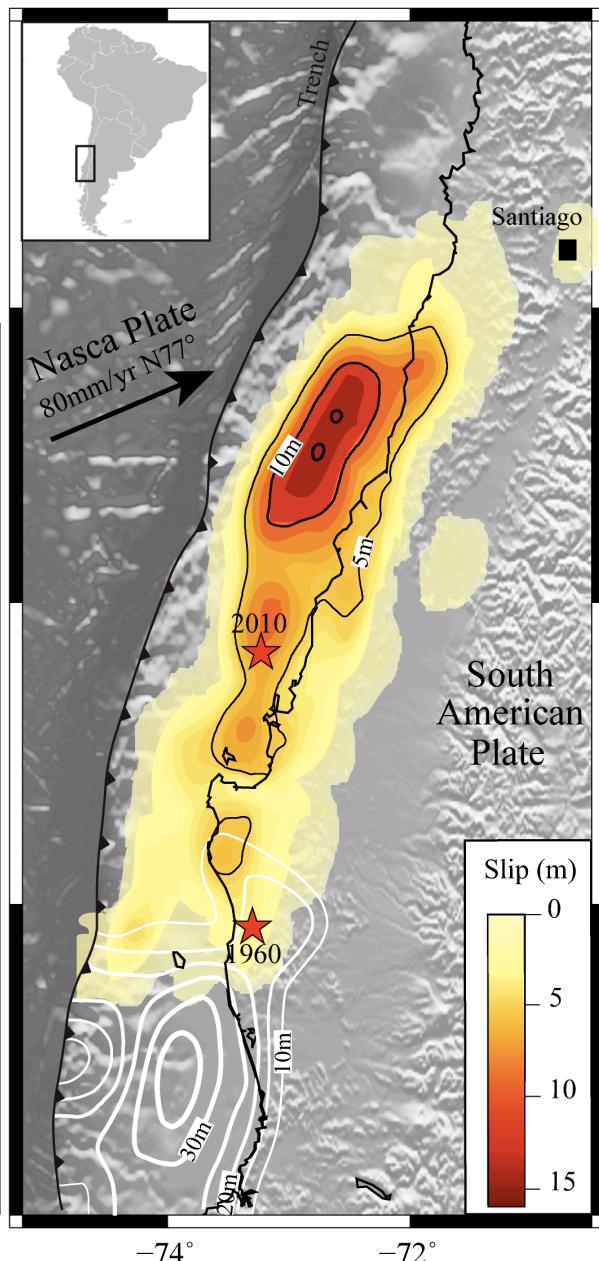
## 2. Critical Taper

Forearc: At critical state?

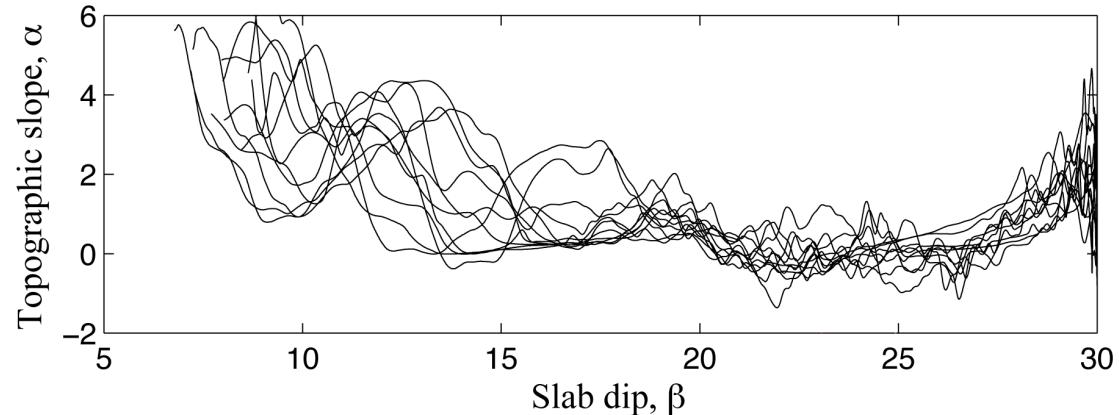


## 2. Critical Taper

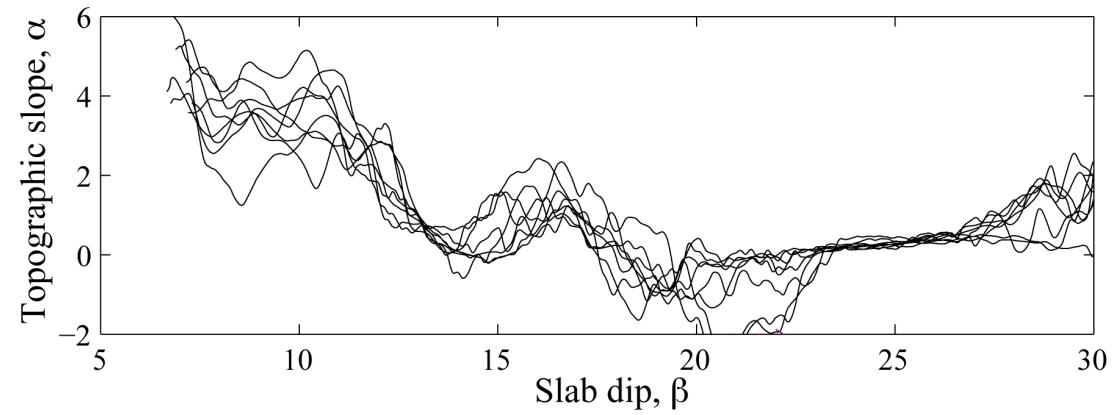
Forearc: At critical state?



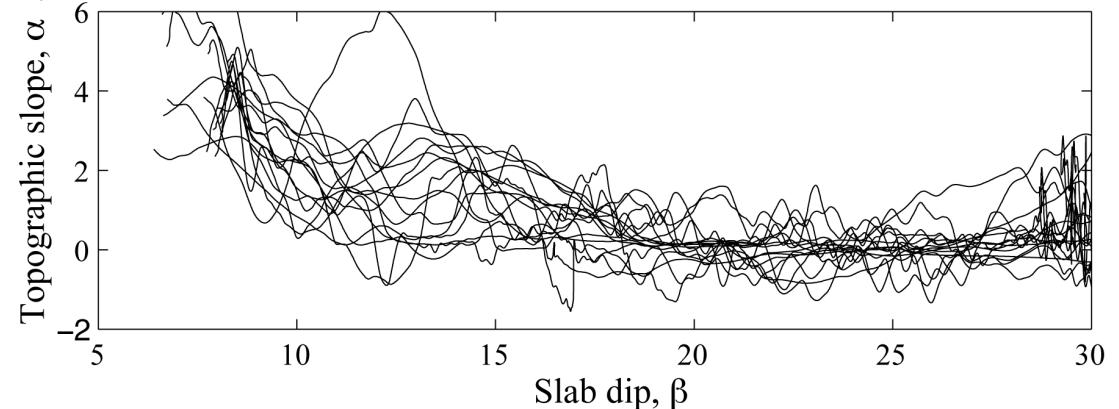
### a) Maule segment



### b) Arauco Peninsula segment

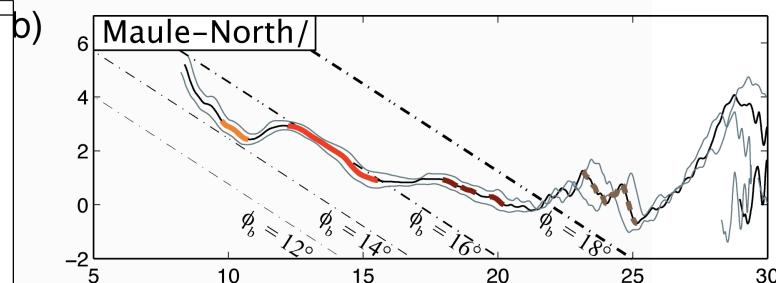
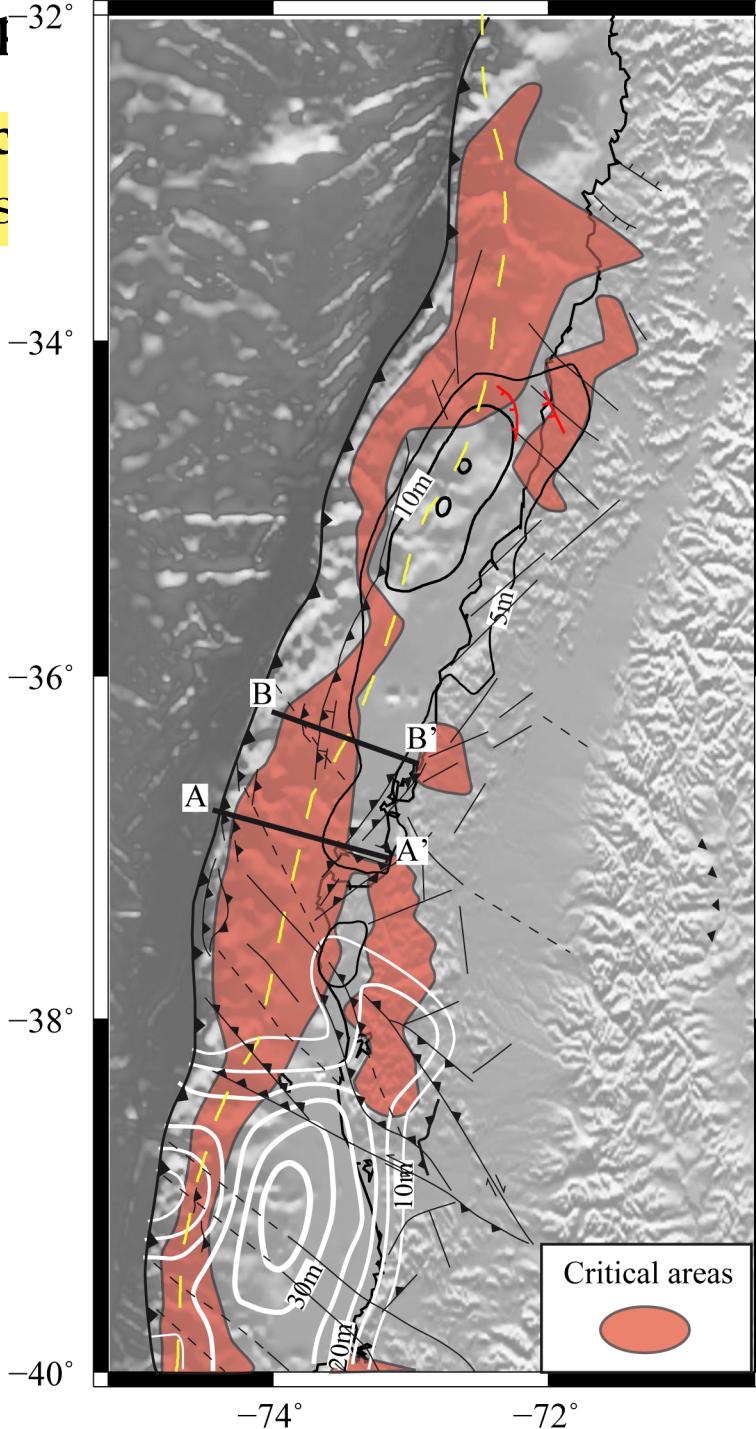


### c) North Valdivia segment



## 2. Critical Tectonic Forearc

At critical stage



### Arauco peninsula:

Uplift rate =  $1.8 \pm 0.4$  mm/a over the past 50 ka (Melnick *et al.*, 2006) and of  $2.3 \pm 0.2$  mm/a over the past 3 ka (Bookhagen *et al.*, 2006)

### Nahuelbuta range:

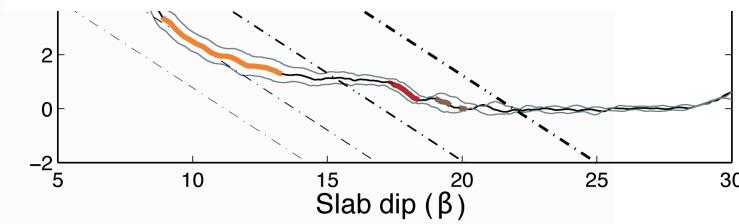
twice the relief of coastal cordillera, with an increase of uplift rate since 4Ma >0.2 mm/a (Glodny *et al.*, 2008)

### Tolten:

no evidence

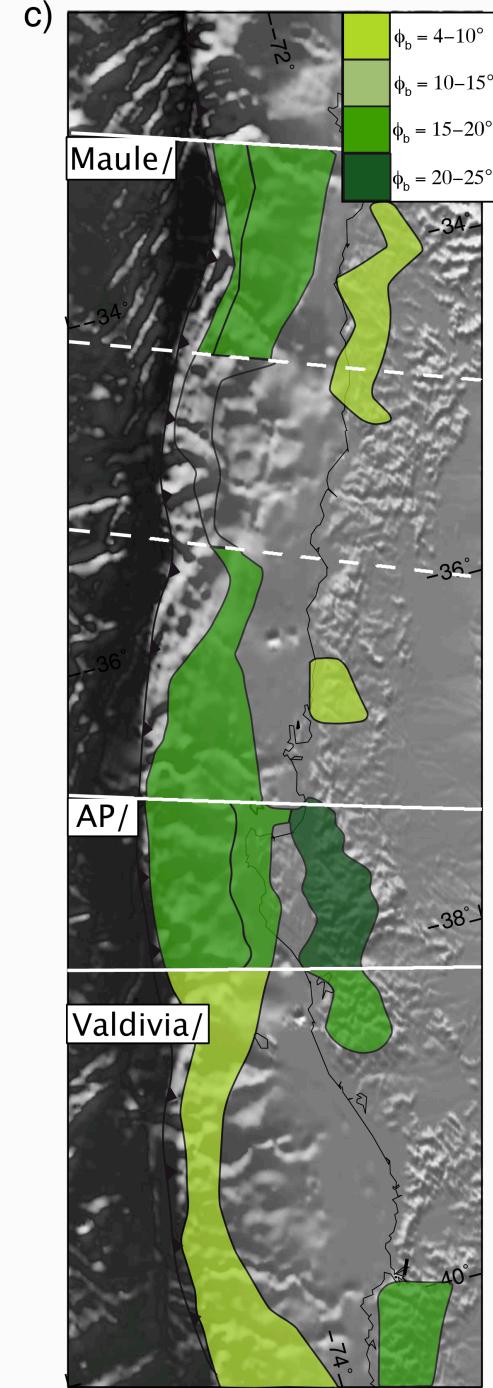
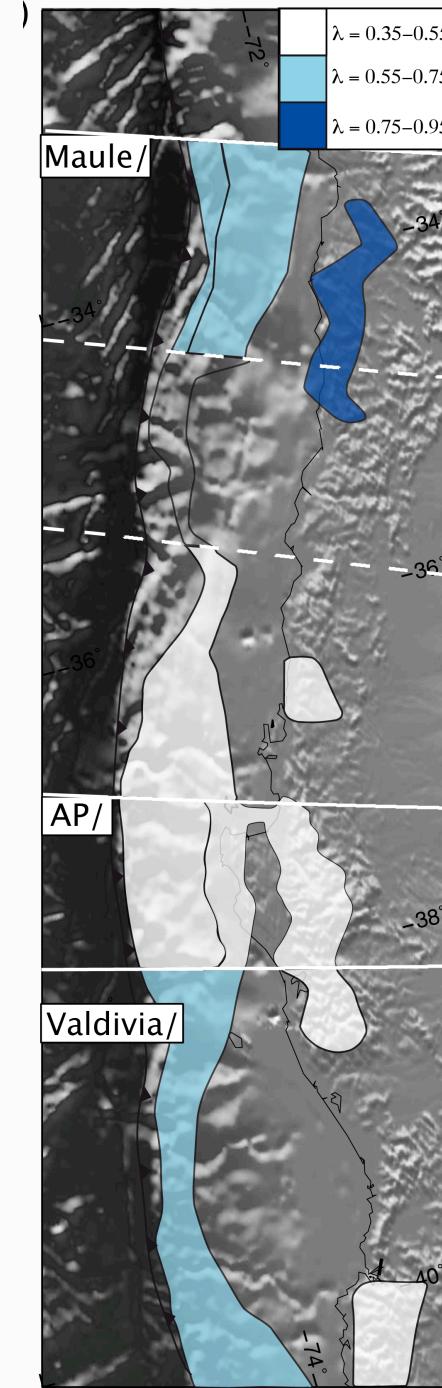
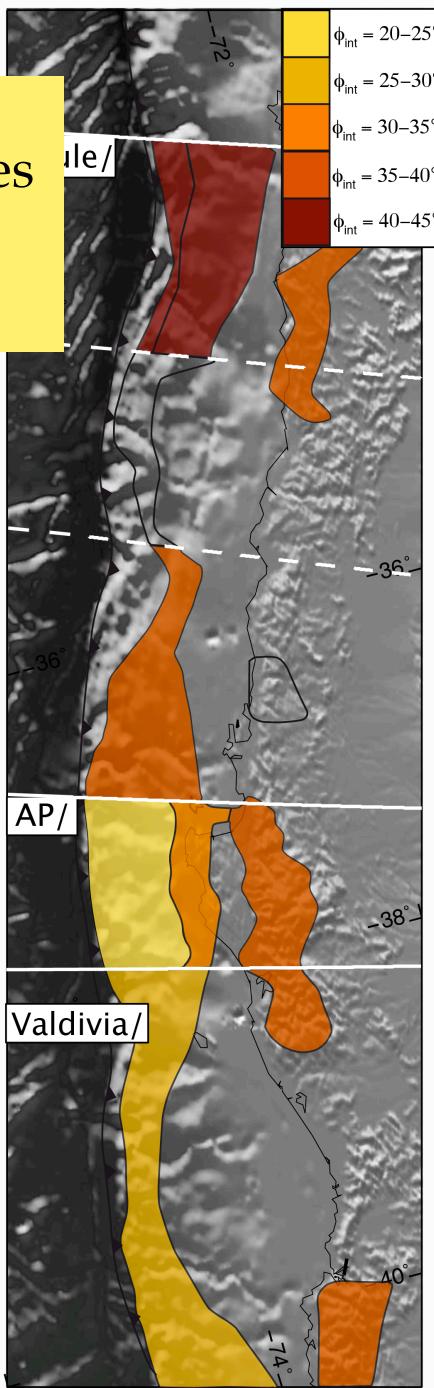
### Bueno segment:

quaternary uplift (Rehak *et al.*, Geom. 2008)



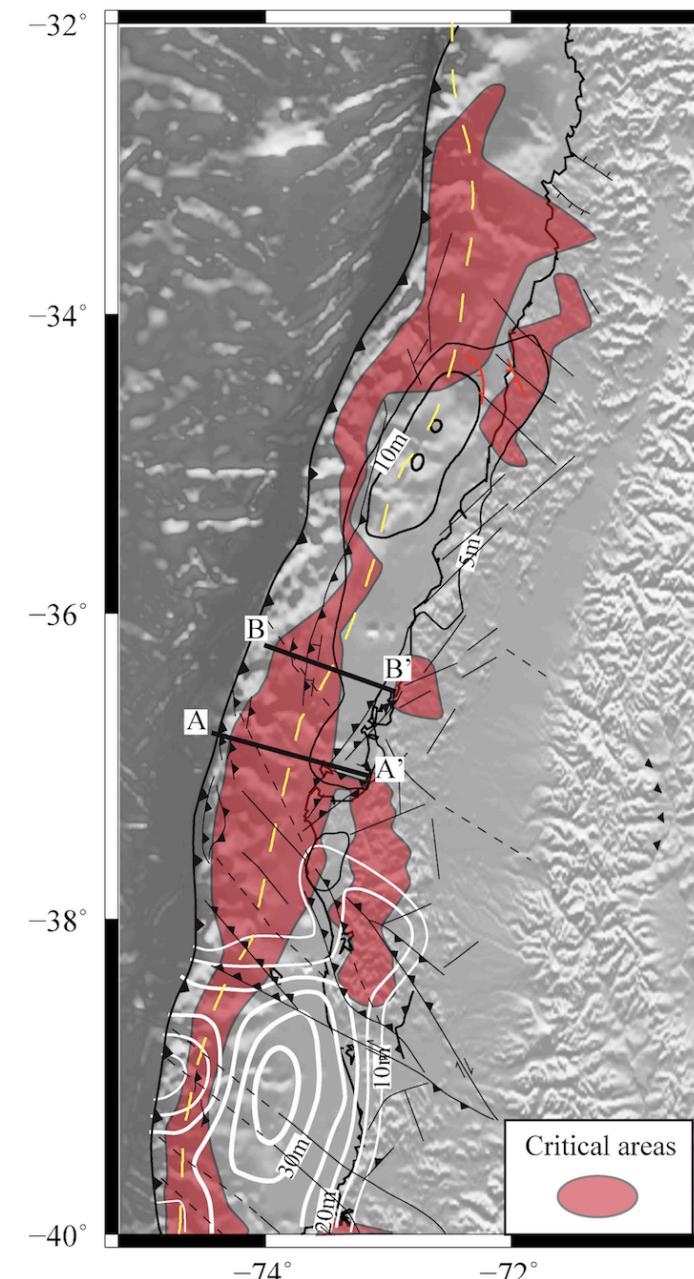
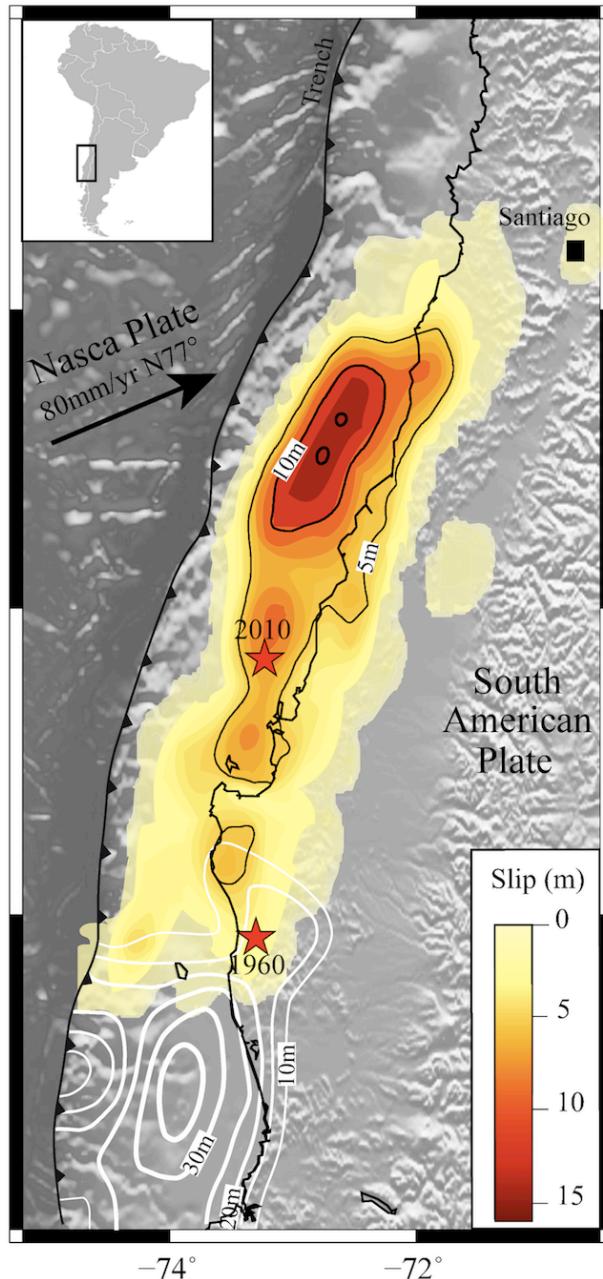
## 2. Critical Taper

a) Forearc:  
Frictional properties  
obtained from  
inversion



## 2. Critical Taper

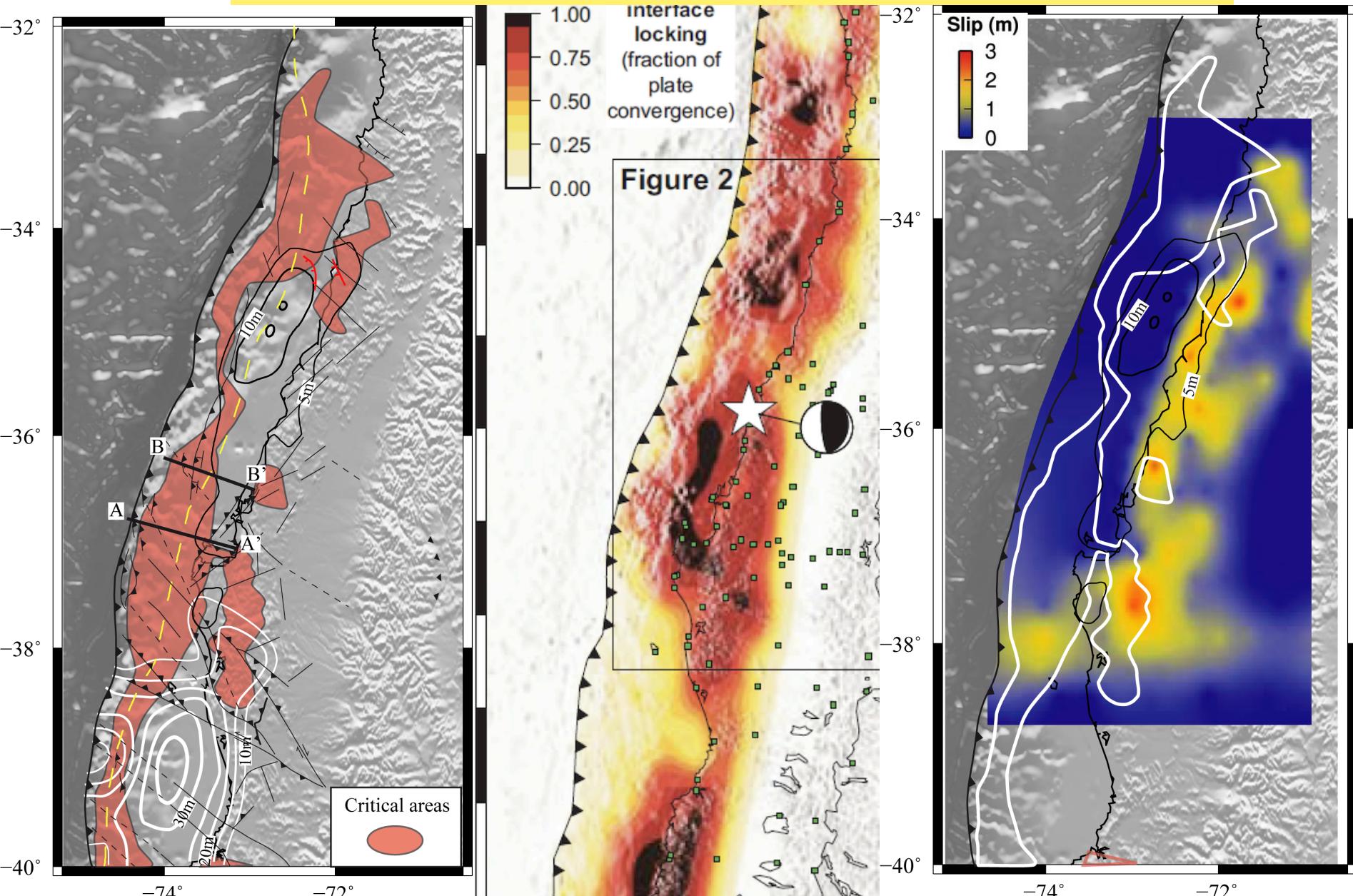
### Comparison with coseismic slip (*Lin et al., JGR in prep.*)



*Moreno et al.,  
GRL 2009*

## 2. Critical Taper

Comparison with interseismic (Moreno *et al.*, *Nature* 2010,  
and postseismic slip (Lin *et al.*, *JGR* in prep.)



# **Megathrust friction in the 2010 Maule earthquake area**

1. Introduction
2. From the Critical Taper Theory
3. From Limit Analysis
4. From Dynamic Simulation of EQ cycle

### 3. Limit analysis

Theory (*Salencon, 1974, 2002*)

Based on:

- Force equilibrium: Theorem of virtual work

$$\mathcal{P}_i(\hat{\mathbf{U}}) = \mathcal{P}_e(\hat{\mathbf{U}}) \quad \forall \hat{\mathbf{U}} \text{ KA}$$

$$\mathcal{P}_e(\hat{\mathbf{U}}) = - \int_{\Omega} \rho g \mathbf{e}_2 \cdot \hat{\mathbf{U}} dV + Q \mathbf{t}_D \cdot \hat{\mathbf{U}}_S$$

Gravity term:      Pushing force:

$$\mathcal{P}_i(\hat{\mathbf{U}}) = \int_{\Sigma_U} \hat{\mathbf{J}} \cdot \mathbf{T} dS$$

Stress vector:

- Theory of maximum rock strength (*Maillet and Leroy, 2006*)

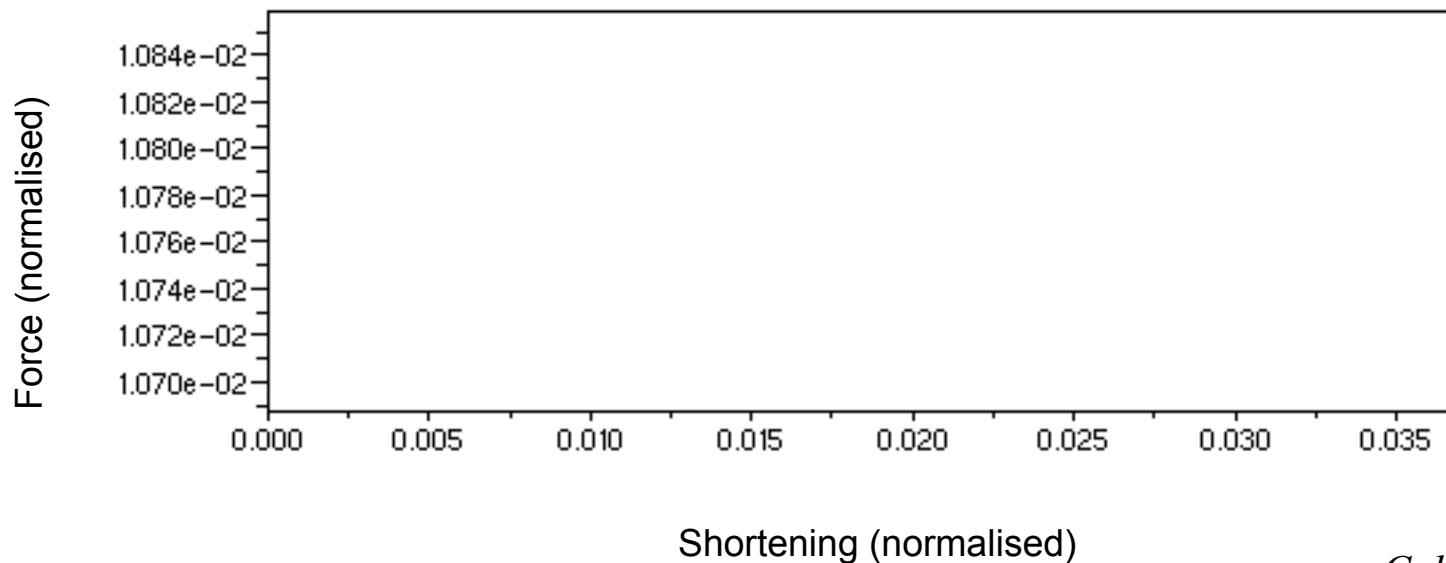
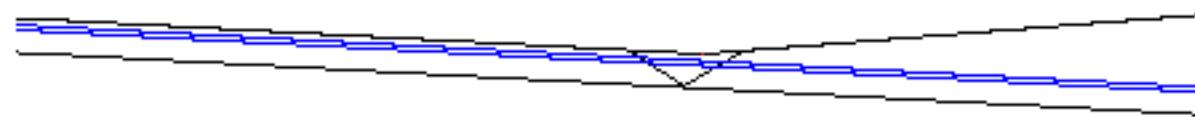
$$Q \mathbf{t}_D \cdot \hat{\mathbf{U}}_S \leq \int_{\Omega} \rho g \mathbf{e}_2 \cdot \hat{\mathbf{U}} dV + \int_{\Sigma_U} \varpi(\hat{\mathbf{J}}) dS$$

### 3. Limit analysis

#### Limit analysis

Based on:

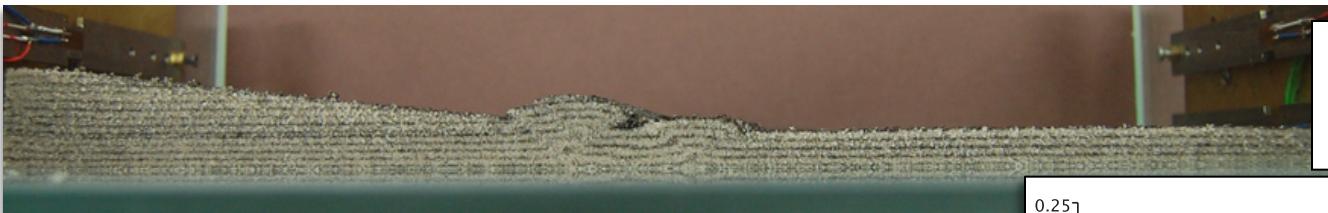
- Force equilibrium
- Theory of maximum rock strength



### 3. Limit analysis

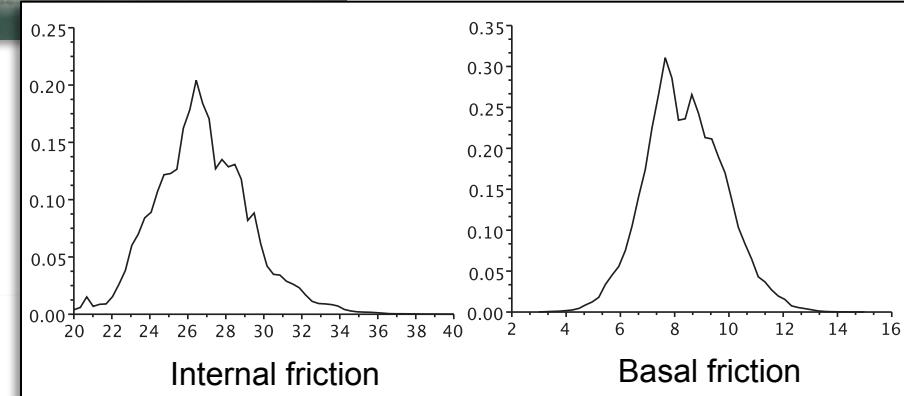
#### Validation

*Analogue experiments:*

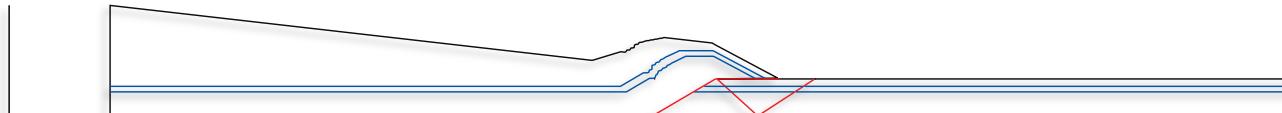


*Probability distributions  
of frictional properties*

*Statistical analysis: observable error bars*



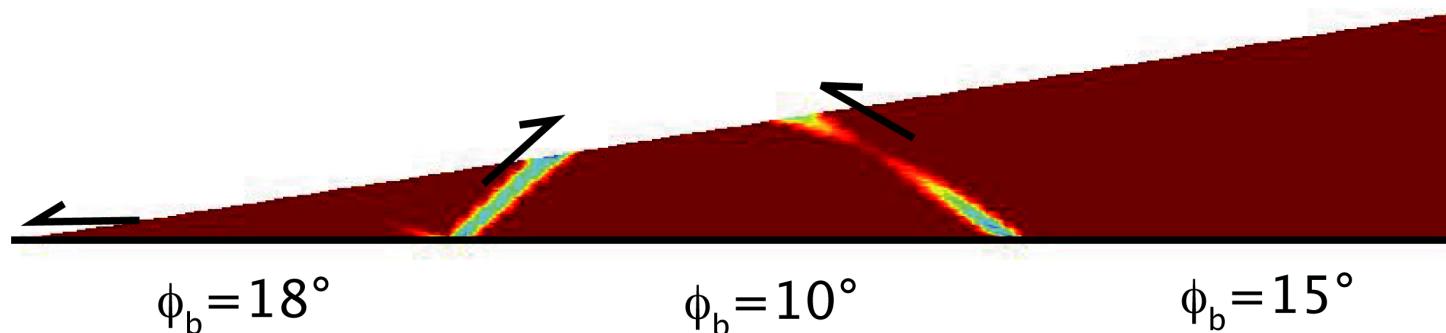
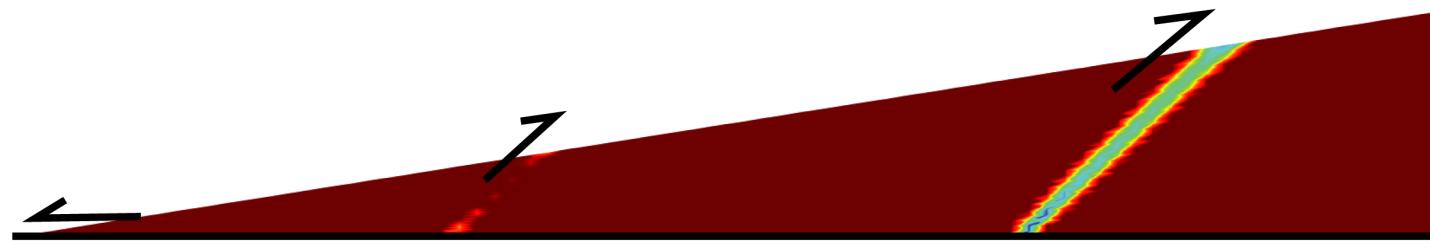
*Mechanical modelisation:*



### 3. Limit analysis

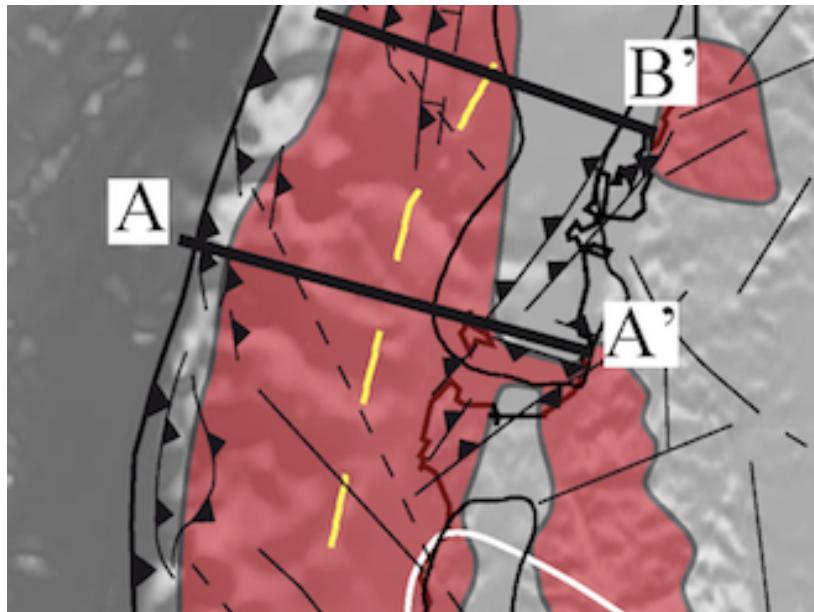
#### Active deformation: Transition of friction

Numerical limit analysis model: Soulaoumiac et al., Comp Geosc. 2010



### 3. Limit analysis

#### Active deformation: Transition of friction?



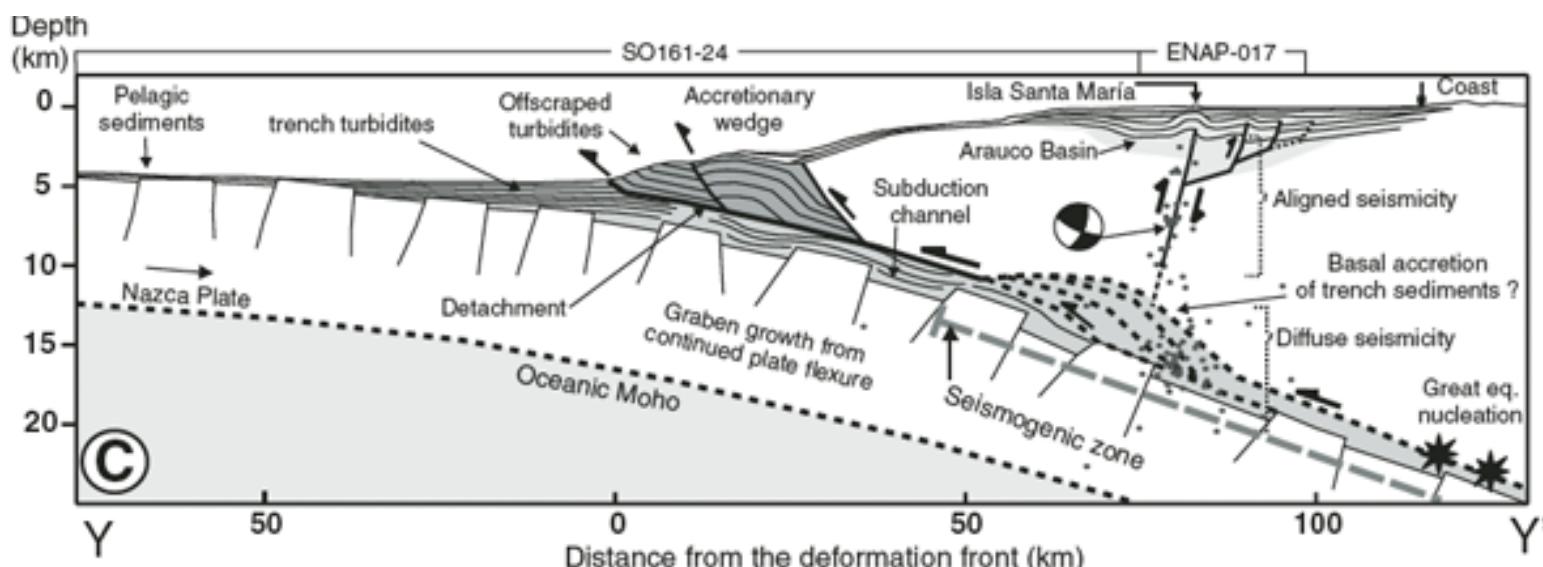
#### Isla Santa Maria:

2010 EQ : 1.4m uplift (Melnick et al., 2012)

1835 EQ : 2.4 - 3m (Darwin, 1839)

1751 EQ : 6m estimated (Melnick et al., 2006)

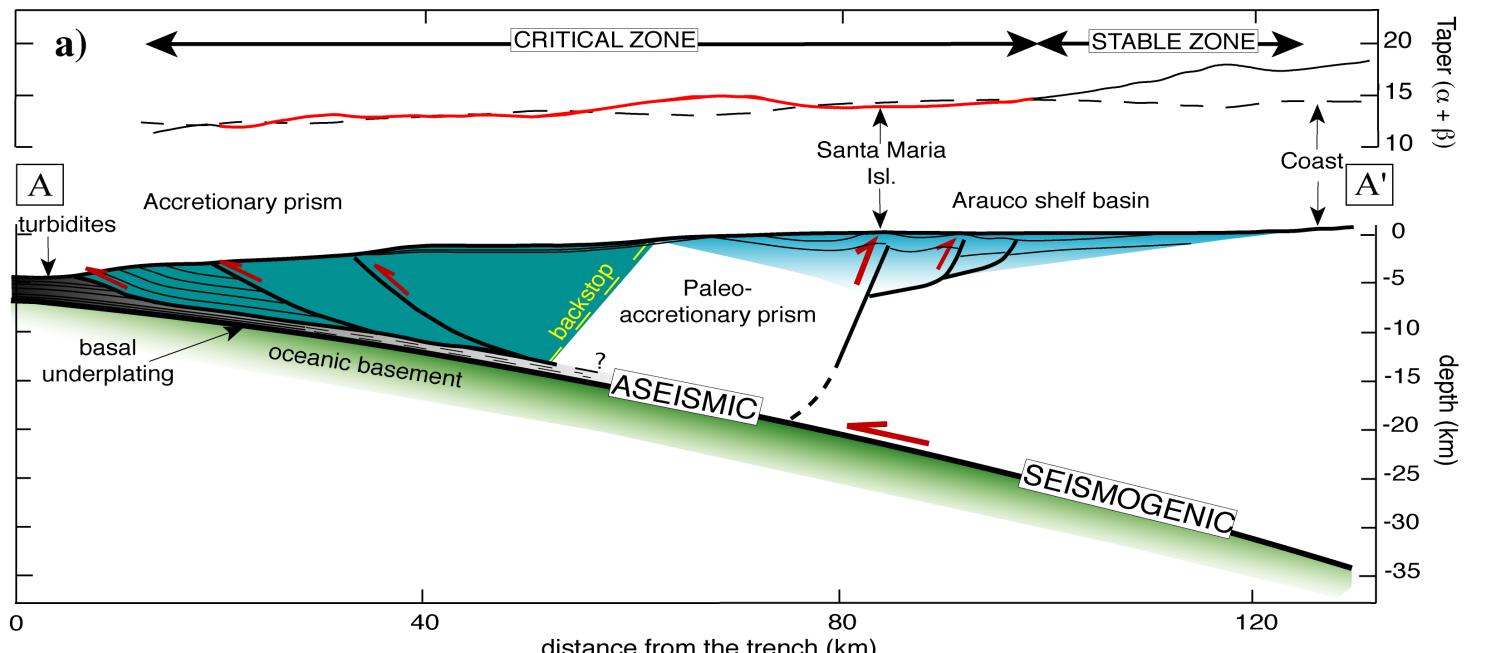
Long-term : 2m / ka since Pleistocene  
(Melnick et al., 2009)



Melnick et al., 2006, 2009

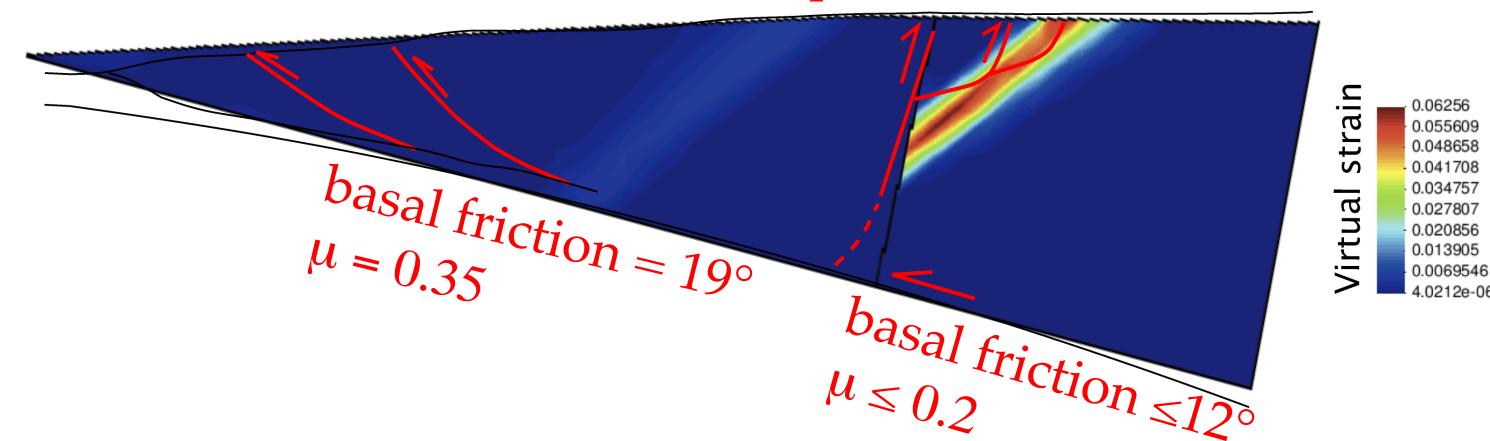
### 3. Limit analysis

#### Application to Santa Maria Island



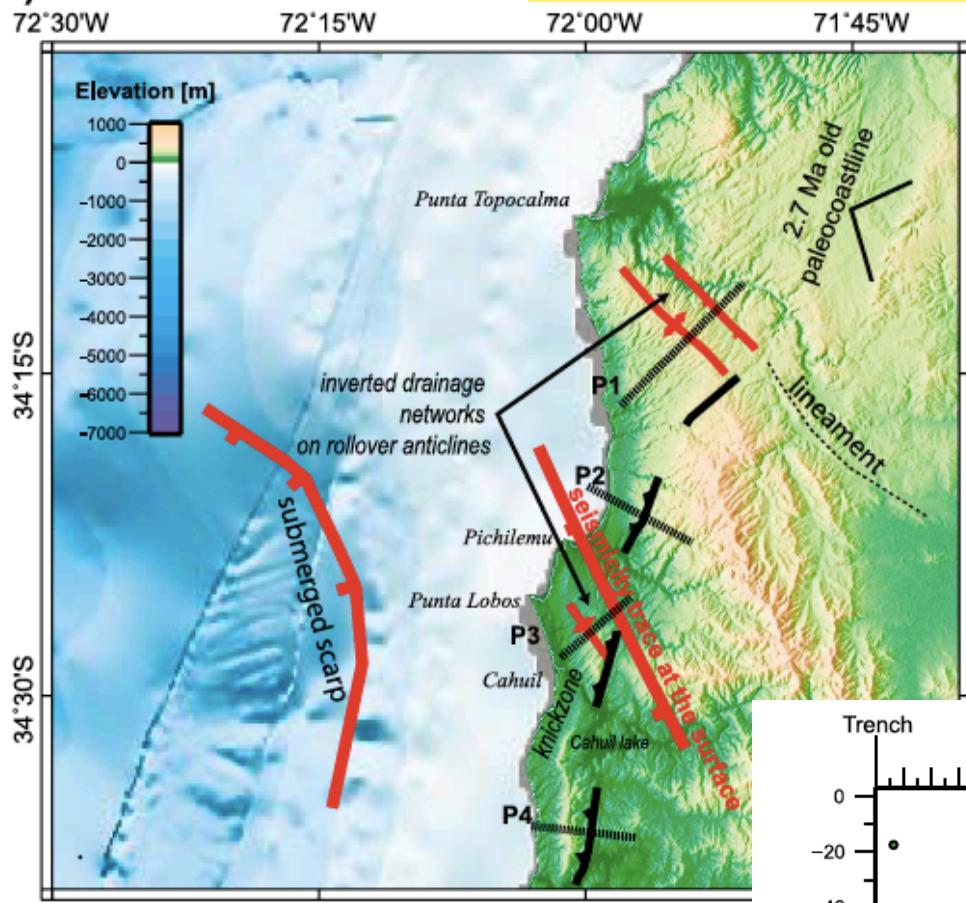
b)

Ramp friction =  $12^\circ$ ,  $\mu = 0.2$



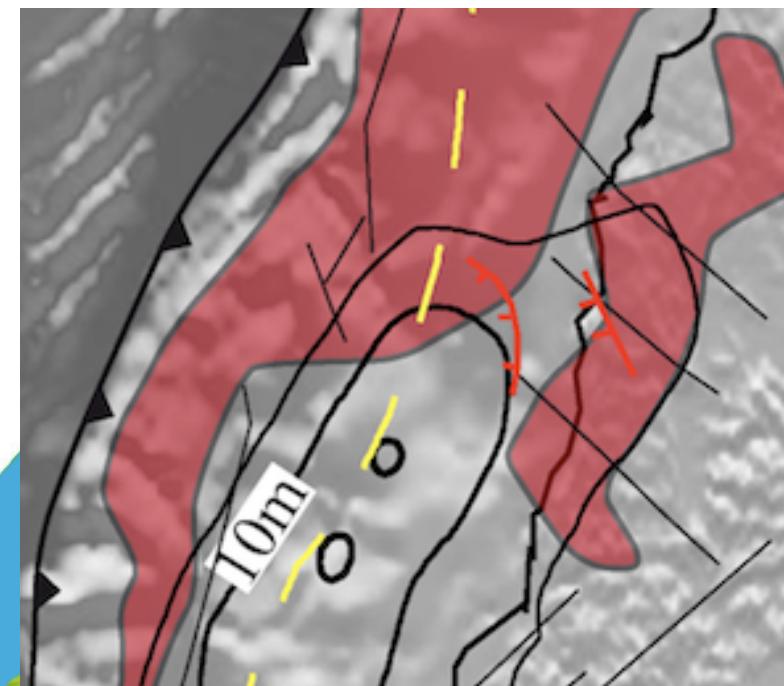
### 3. Limit analysis

a)



### Pichilemu NF, frictional transition?

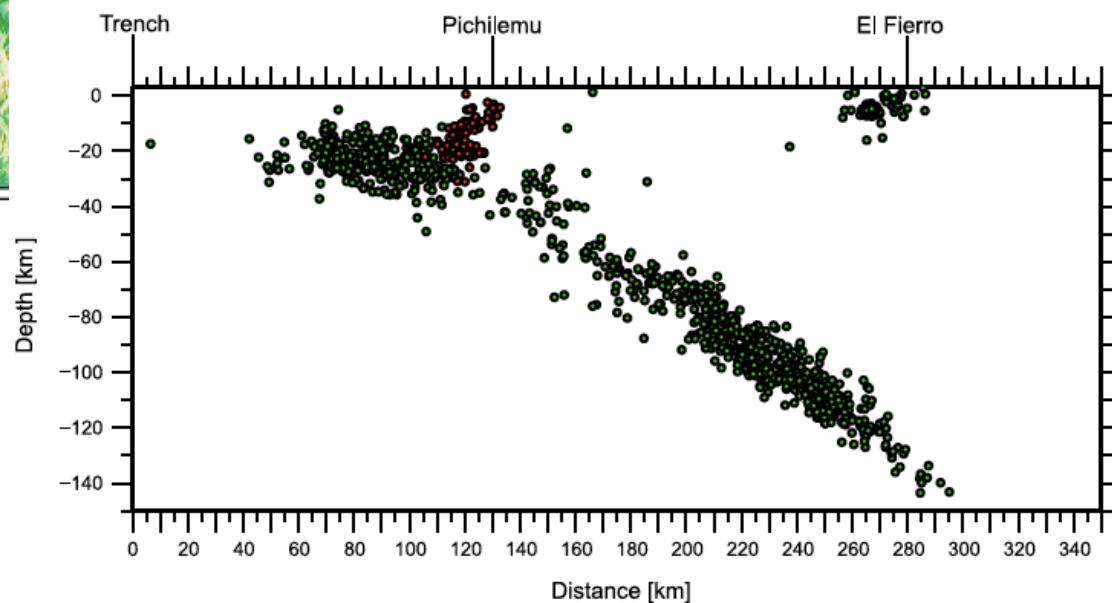
b)



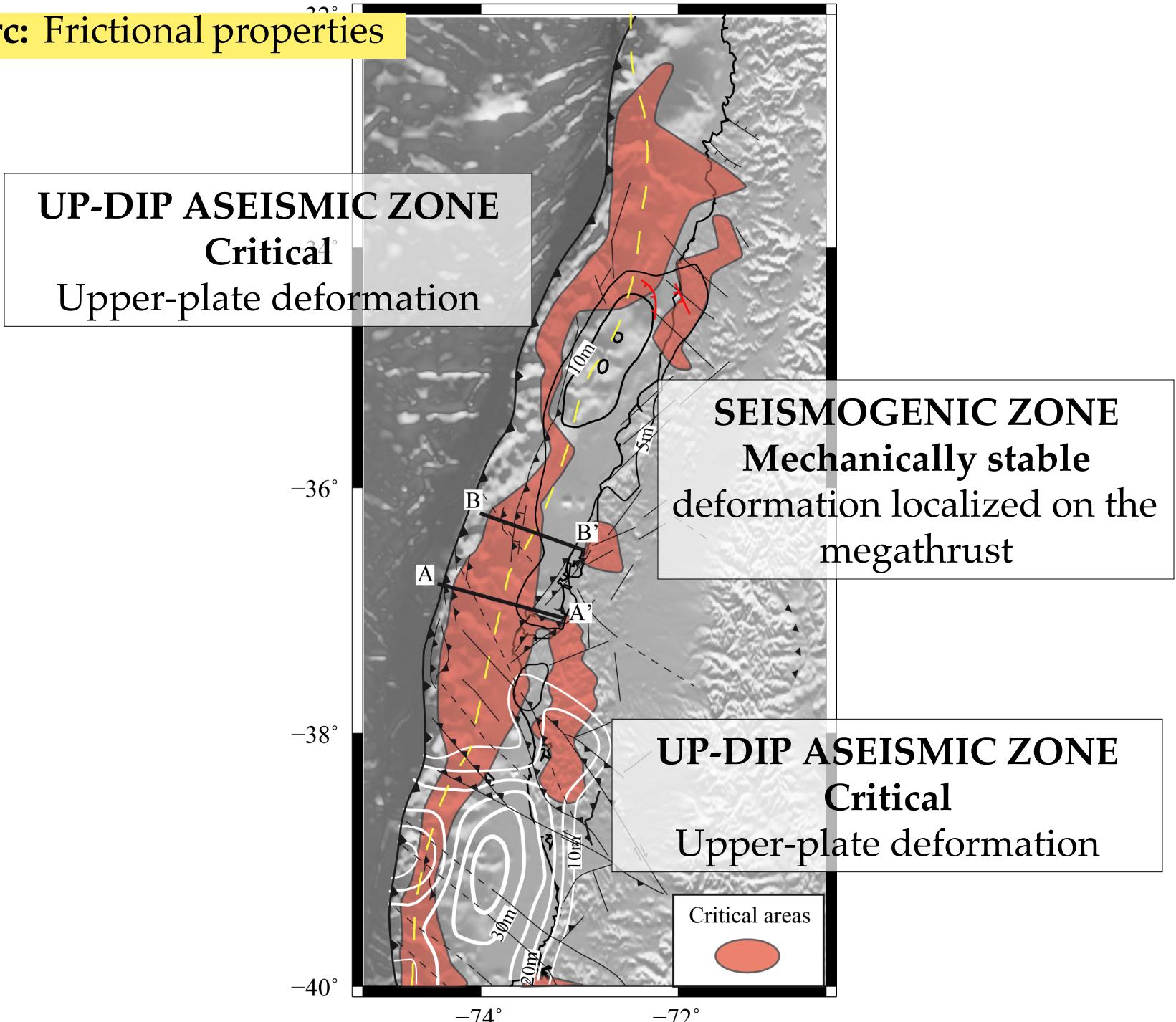
Farias et al., Tectonics 2011

basal friction in SZ  $\leq 5^\circ$

$$\mu \leq 0.1$$



# Forearc: Frictional properties

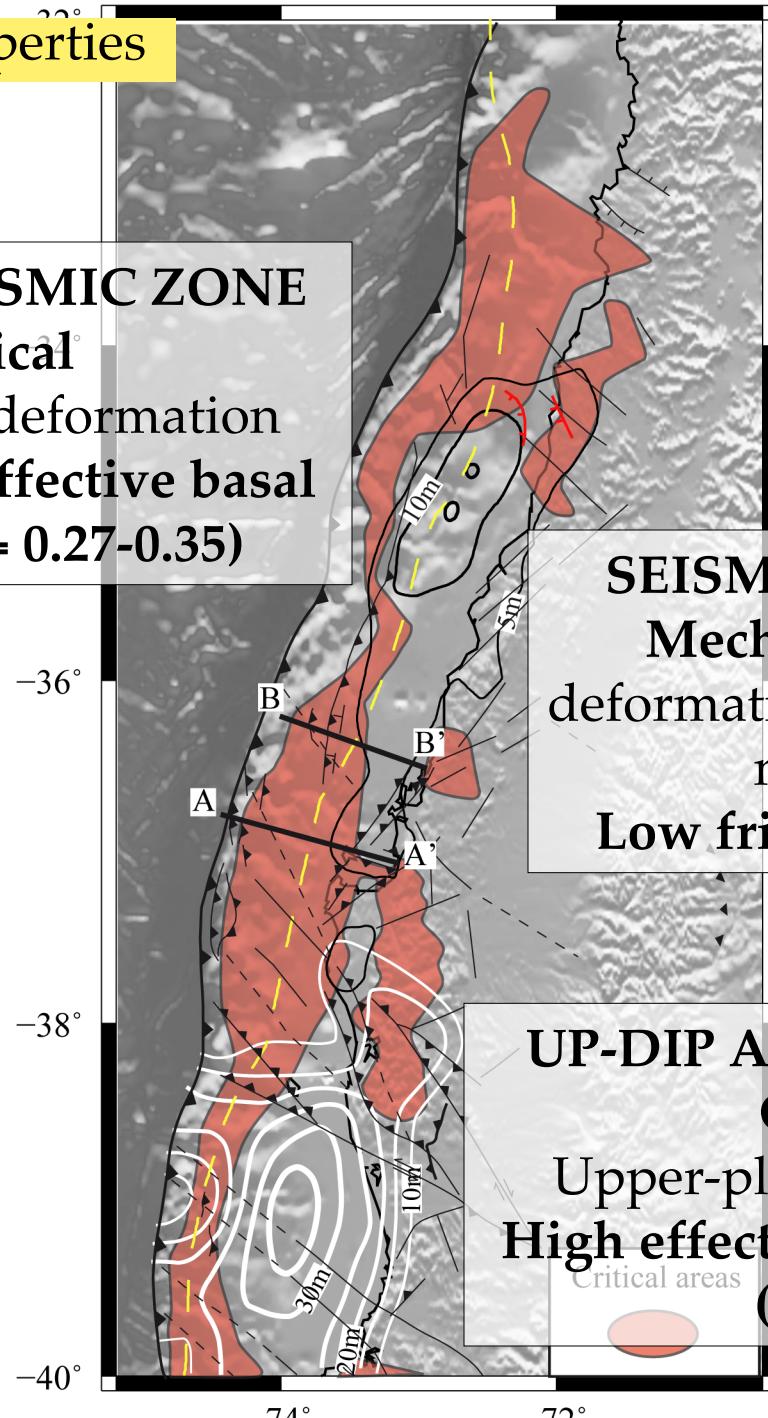


# Forearc: Frictional properties

**UP-DIP ASEISMIC ZONE**  
**Critical**  
Upper-plate deformation  
**Intermediate effective basal friction ( $\mu = 0.27-0.35$ )**

**SEISMOGENIC ZONE**  
Mechanically stable deformation localized on the megathrust  
**Low friction ( $\mu = 0.1-0.2$ )**

**UP-DIP ASEISMIC ZONE**  
**Critical**  
Upper-plate deformation  
**High effective basal friction ( $\mu \geq 0.4$ )**



## Forearc: Arauco Peninsula, a rate-strengthening barrier?

3D dynamic simulation of EQ cycle  
(*Lapusta and Liu, JGR 2009*)

**Based on Rate- and State- laws, laboratory-derived**

(Dieterich, Ruina, Blanpied, Marone, Tullis and others, based on earlier work of Scholz and others) **for slip velocities small** ( $\sim 10^{-9} - 10^{-2}$  m/s) **compared to the seismic range.**

***Unique tool for simulating earthquake cycles*** in their entirety,

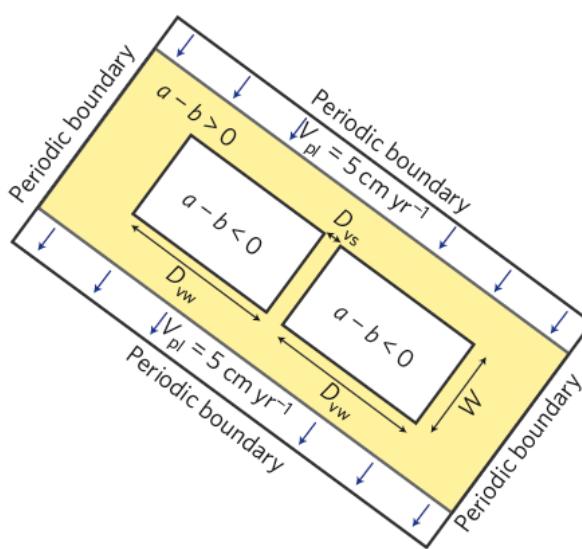
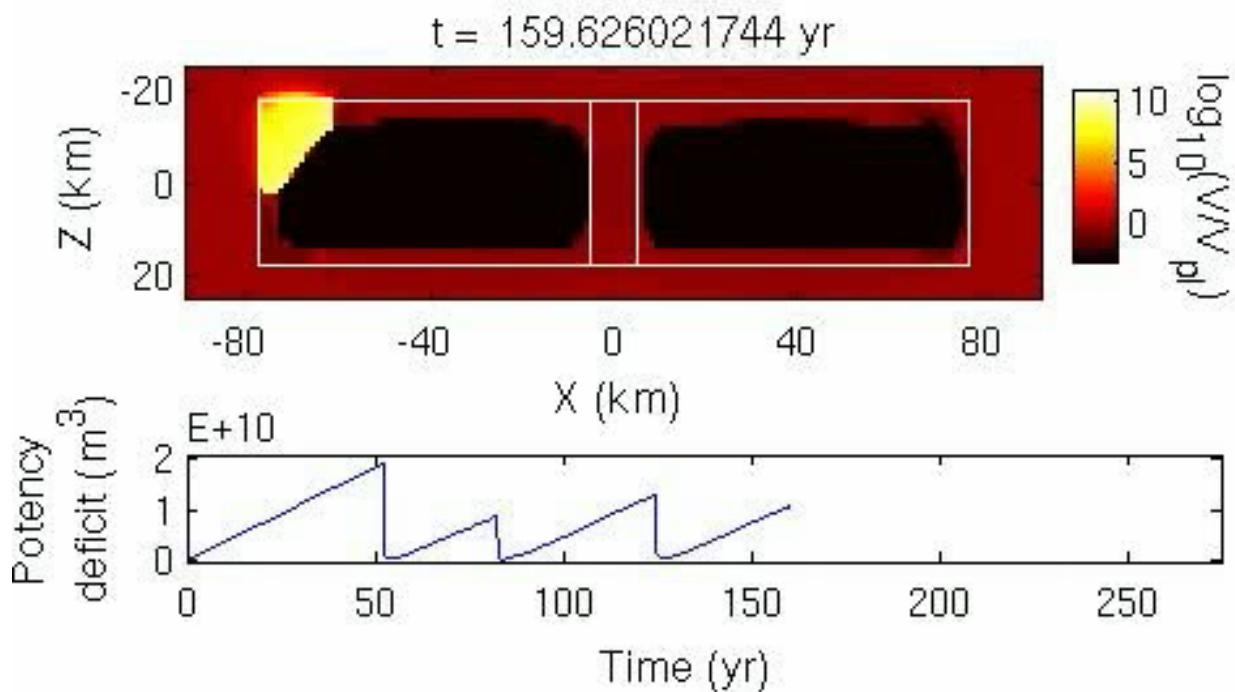
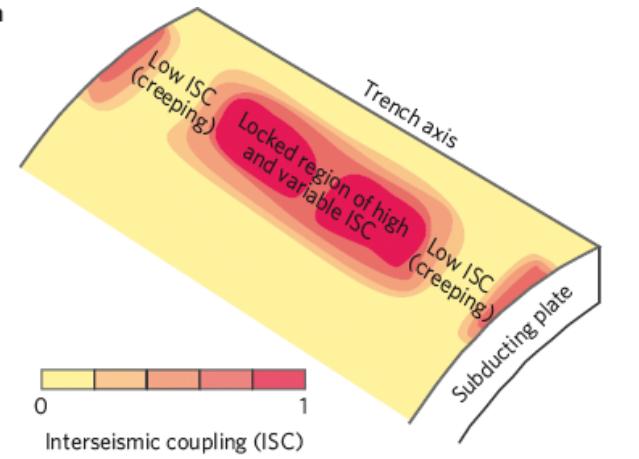
- from accelerating slip in slowly expanding nucleation zones
- to dynamic rupture propagation (*turn into linear slip weakening*)
- to post-seismic slip and interseismic creep
- to fault restrengthening between seismic events.

$$\tau = \bar{\sigma} f = (\sigma - p)[f_o + a \ln \frac{V}{V_o} + b \ln \frac{V_o \theta}{L}]; \quad \frac{d\theta}{dt} = 1 - \frac{V \theta}{L}$$

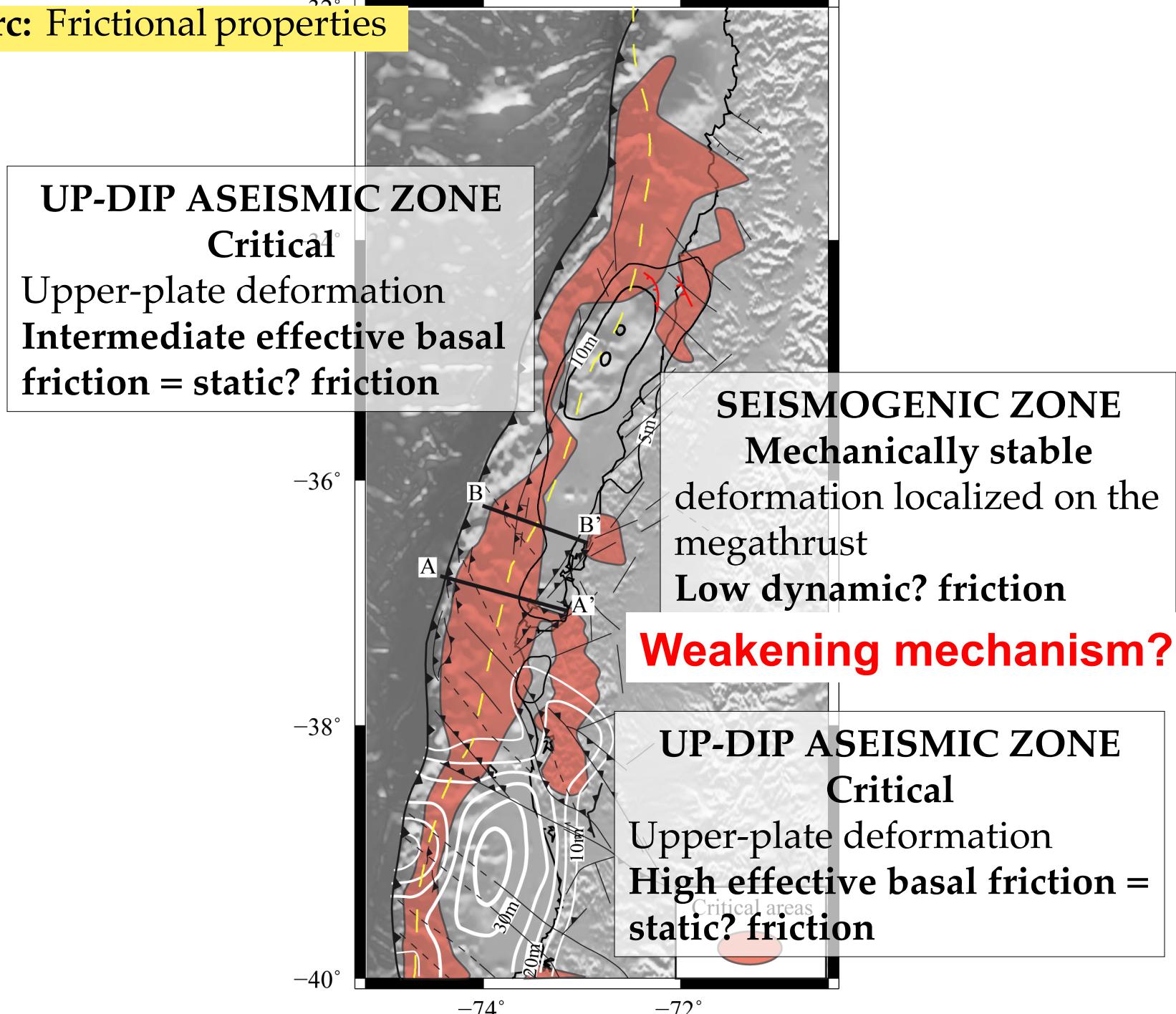
# Forearc: Arauco Peninsula, a rate-strengthening barrier?

3D dynamic simulation of EQ cycle

Kaneko *et al.*, *Nature* 2010



# Forearc: Frictional properties



# **Megathrust friction in the 2010 Maule earthquake area**

1. Introduction
2. From the Critical Taper Theory
3. From Limit Analysis
4. From Dynamic Simulation of EQ cycle

## 4. 2-3D Dynamic simulation

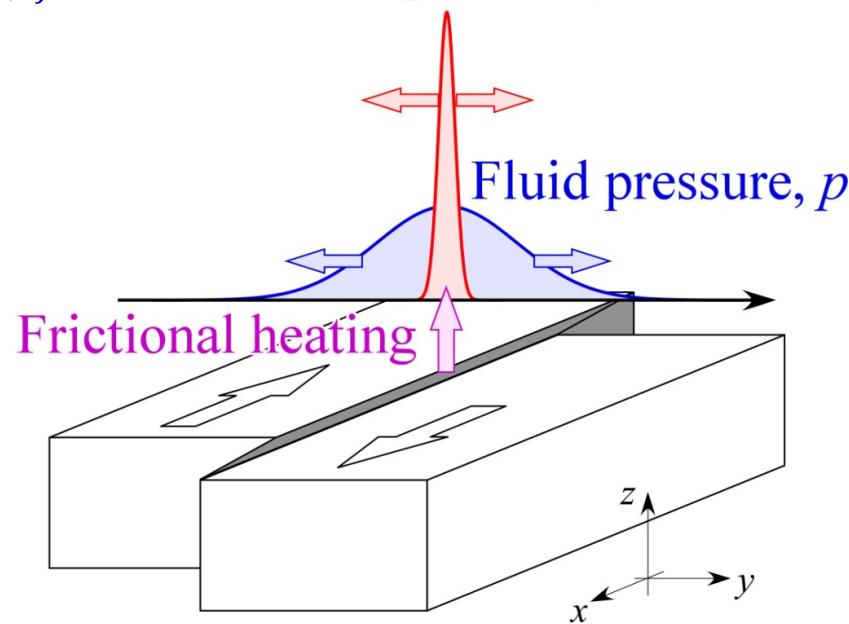
### Weakening mechanisms

#### Hydrothermal effects on frictional resistance (high slip rates)

(Sibson 1973, Lachenbruch 1980, Mase & Smith 1985, Lee & Delaney 1987, Andrews 2002, Wibberley 2002, Noda & Shimamoto 2005, Sulem 2005, Bizarri & Cocco 2006, Rice 2006,...)

Numerical implementation: *Noda and Lapusta, JGR 2010*    Temperature,  $T$

- Rapid shear heating during seismic slip increases fault temperature  $T$ .
- **Thermal pressurization** is one of the potential effects: Since the thermal expansivity of water is much larger than that of rocks, shear heating may increase the pore fluid pressure  $p$ .
- This could lead to **co-seismic fault weakening**, additional to any slow-slip friction behavior.



$$\text{Shear traction } \tau = f \sigma_e = f(\sigma_n - p)$$

Friction coefficient      Effective normal stress      Elastodynamic normal stress

Pore pressure

## 4. 2-3D Dynamic simulation

### Model set-up

**Important length scales to resolve:**

**Nucleation size:**

Seismic slip in large enough regions -  
Estimates of the critical size (Rice and  
Ruina, 1983; Rice, Lapusta, Ranjith, 2001;  
Rubin and Ampuero, 2005):

$$h^* \propto \frac{\text{shear modulus} \times \text{char. slip}}{\text{effective normal stress} \times F(a, b)}$$

$$h_{RR}^* \propto \frac{\mu L}{\bar{\sigma}(b-a)}; \quad h_{RA}^* \propto \frac{\mu L}{\bar{\sigma}(b-a)^2/b}$$

**Characteristic weakening scale at the  
rupture tip due to RS friction**

$$\Lambda = \frac{\mu^* L}{b\sigma}.$$

**Important slip scales to resolve:**

**For adiabatic, undrained conditions  
(Rice 2006):**

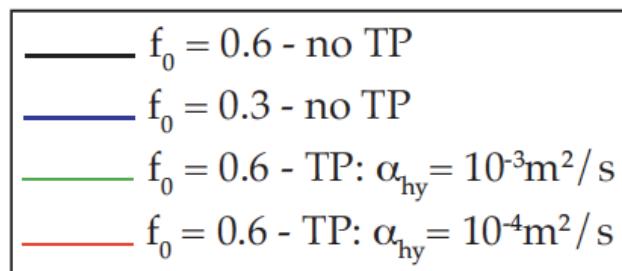
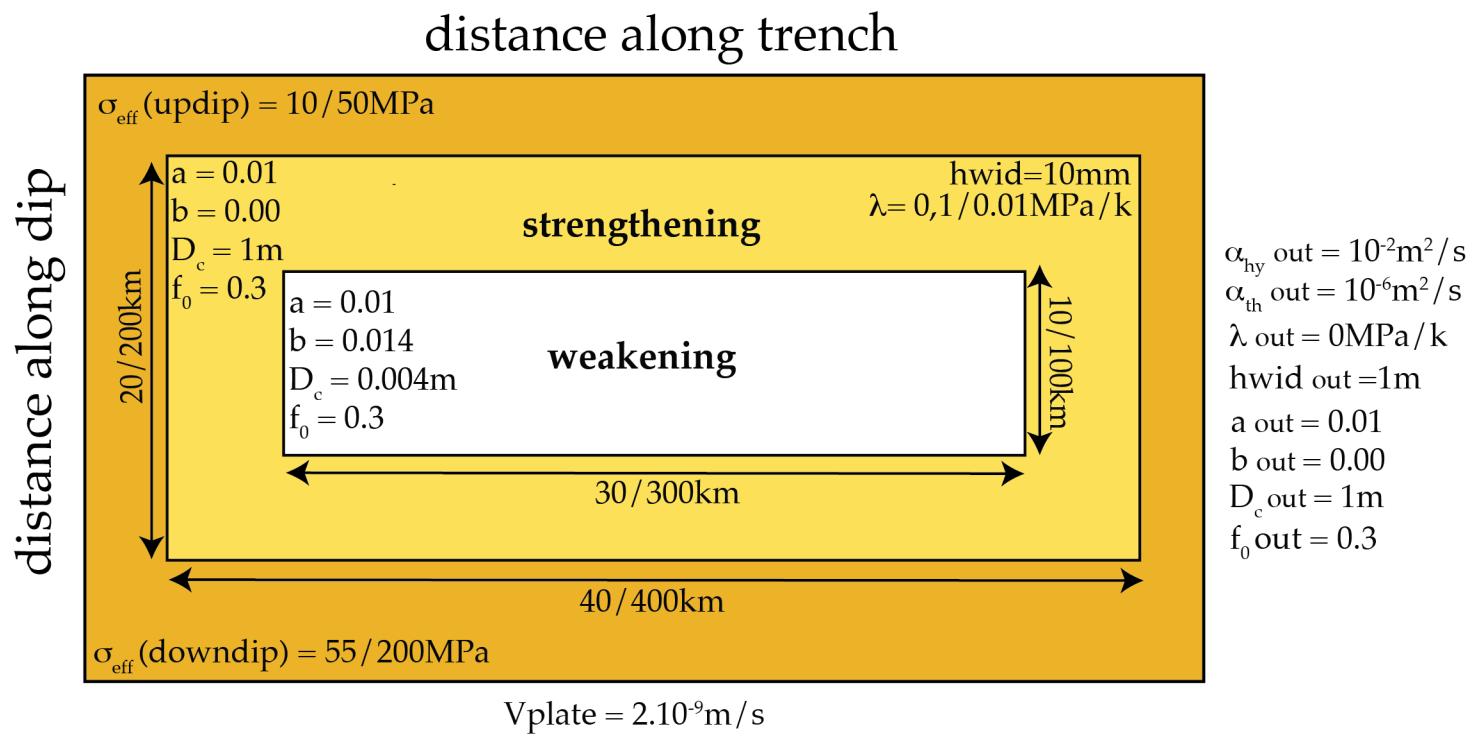
$$La = \frac{\text{specific heat} * \text{layer thickness}}{\text{friction} * \text{undrained press factor}}$$

**At constant friction & slip rate (Rice  
2006):**

$$L^* = \frac{4}{f^2} \left( \frac{\rho c}{\Lambda} \right)^2 \frac{\left( \sqrt{\alpha_{hy}} + \sqrt{\alpha_{th}} \right)^2}{V}.$$

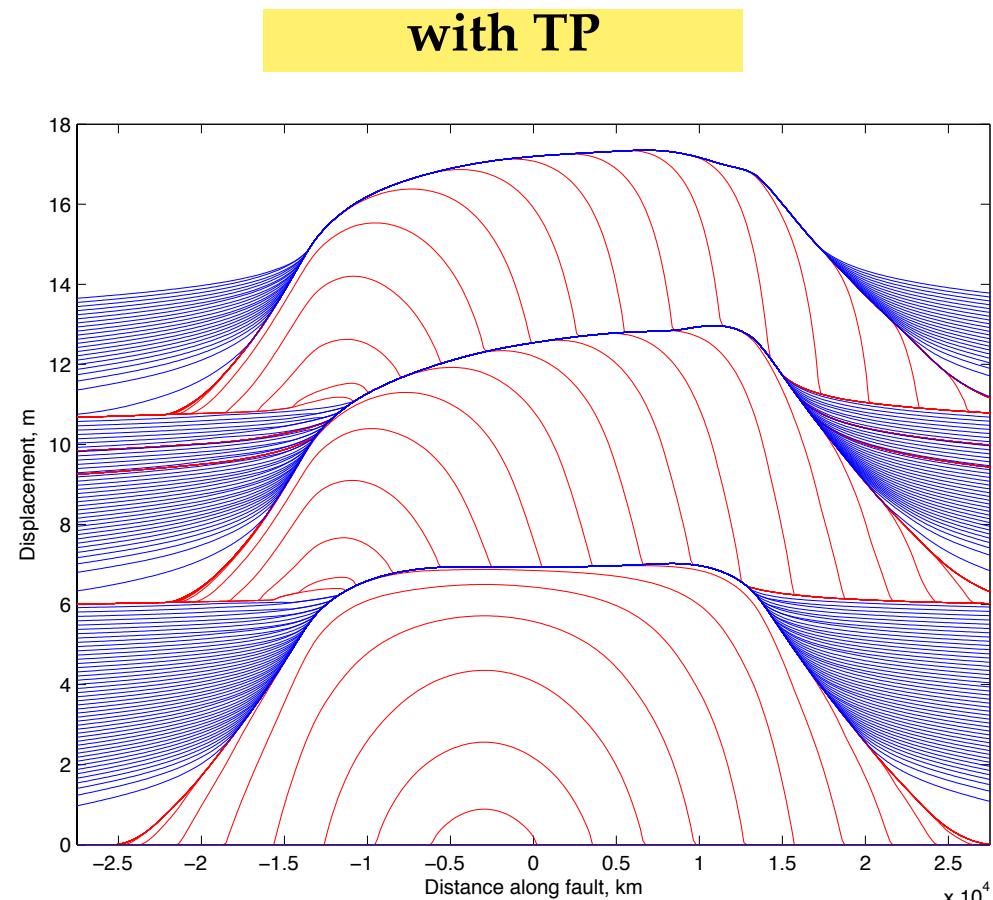
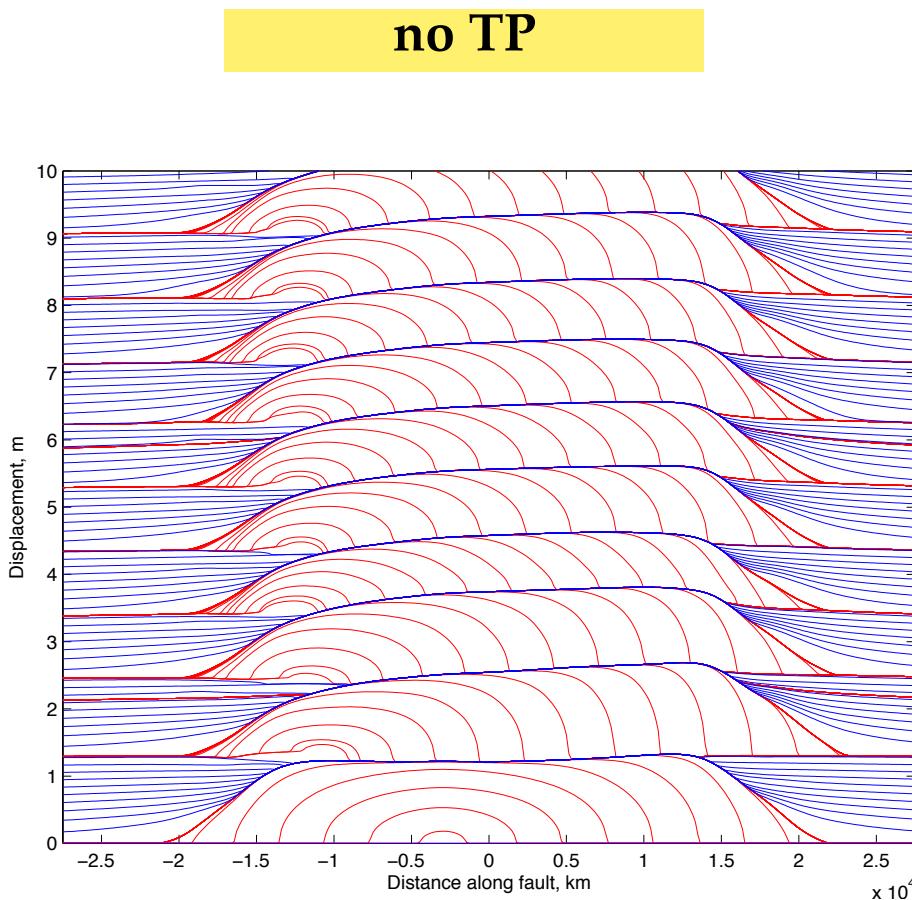
# 4. 2-3D Dynamic simulation

## Model set-up



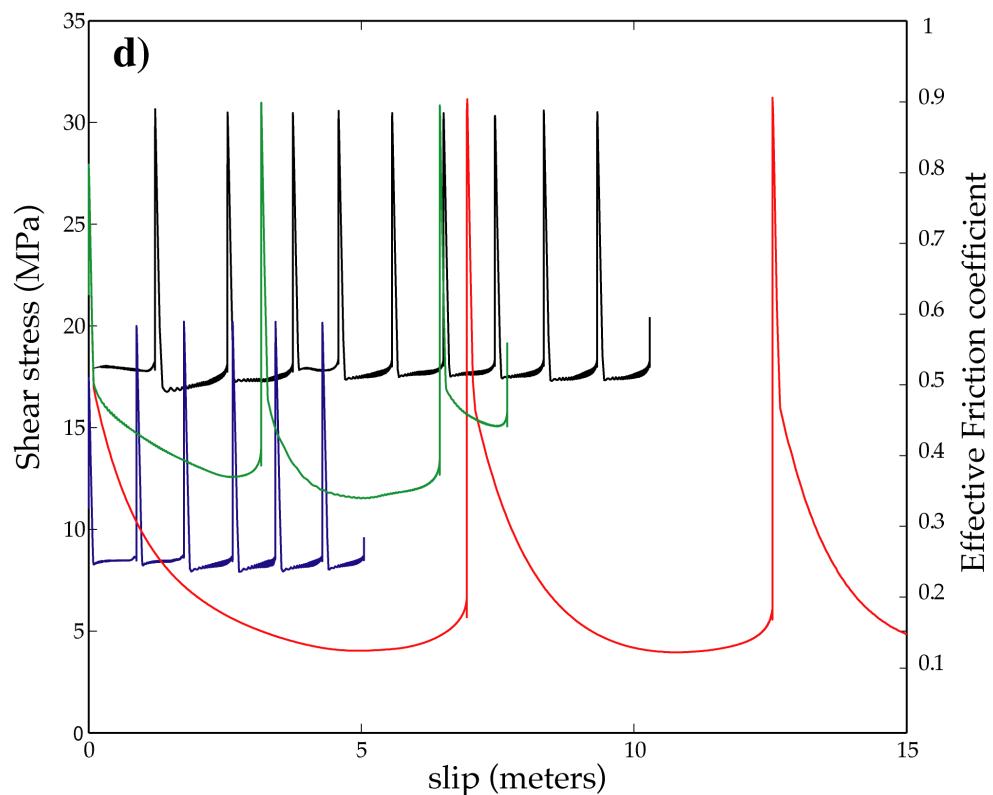
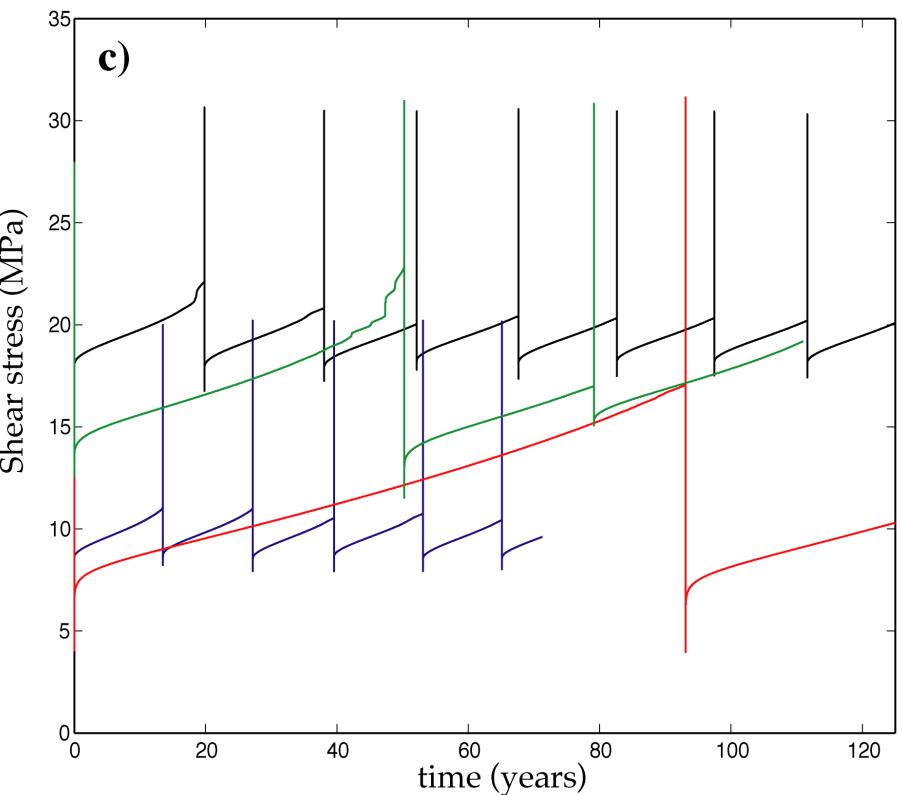
## 4. 2-3D Dynamic simulation

### Dynamic friction, stress drop and recurrence



## 4. 2-3D Dynamic simulation

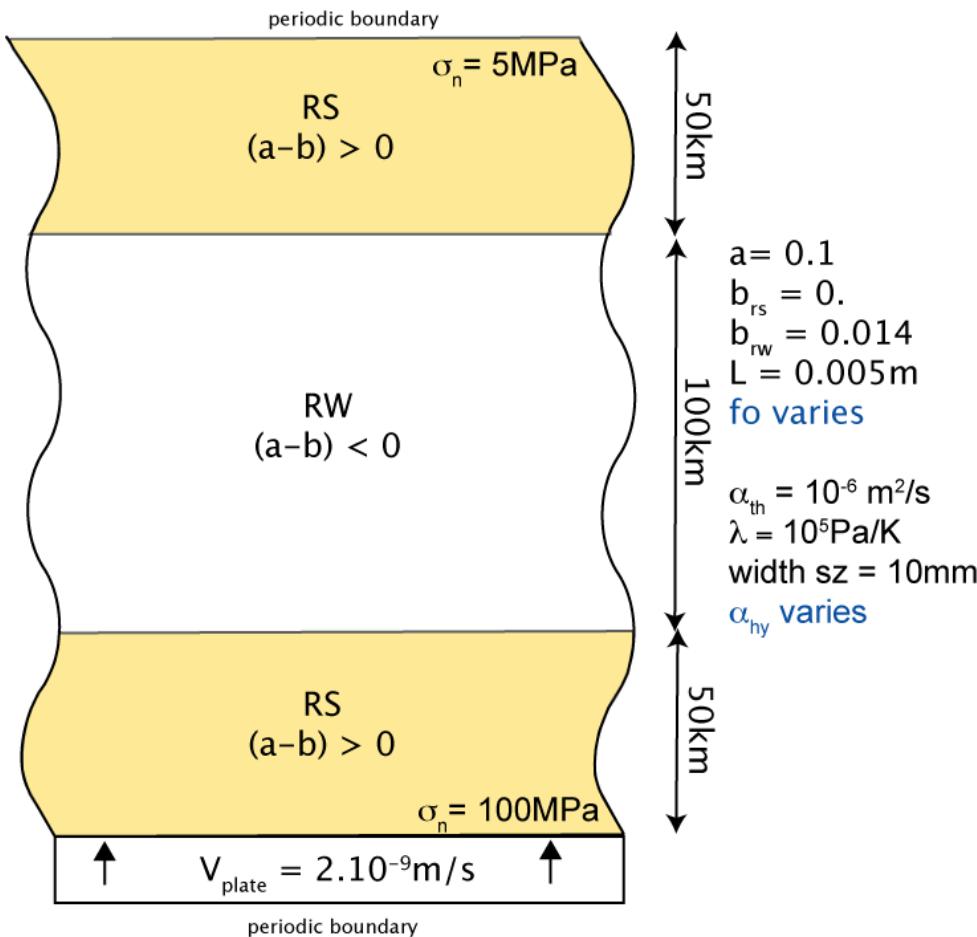
### Dynamic friction, stress drop and recurrence



—	$f_0 = 0.6$ - no TP
—	$f_0 = 0.3$ - no TP
—	$f_0 = 0.6$ - TP: $\alpha_{hy} = 10^{-3} \text{ m}^2/\text{s}$
—	$f_0 = 0.6$ - TP: $\alpha_{hy} = 10^{-4} \text{ m}^2/\text{s}$

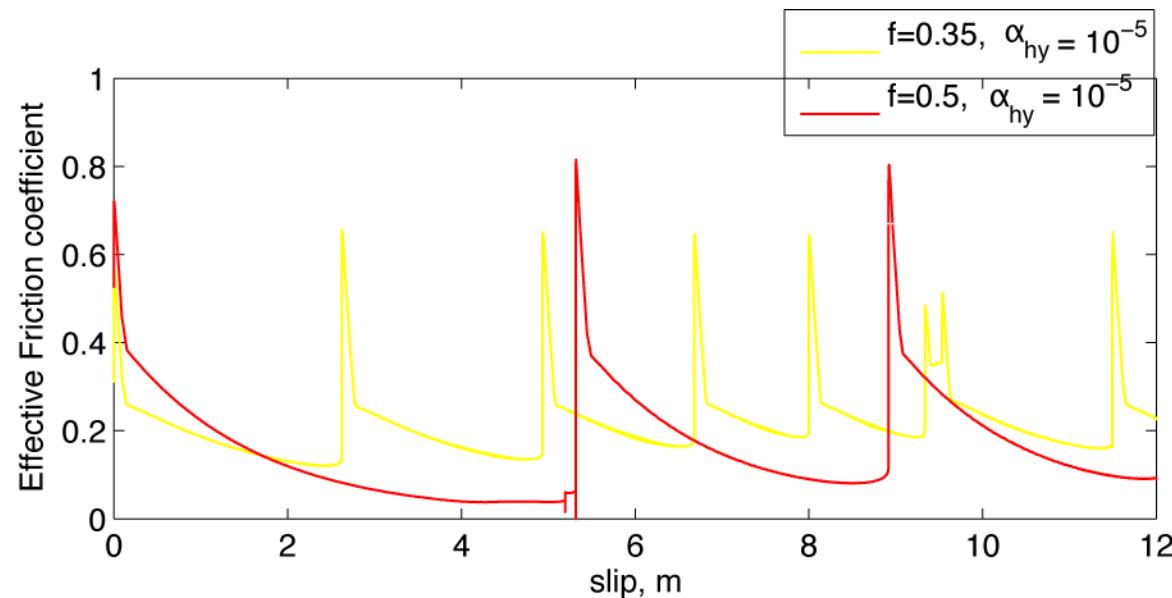
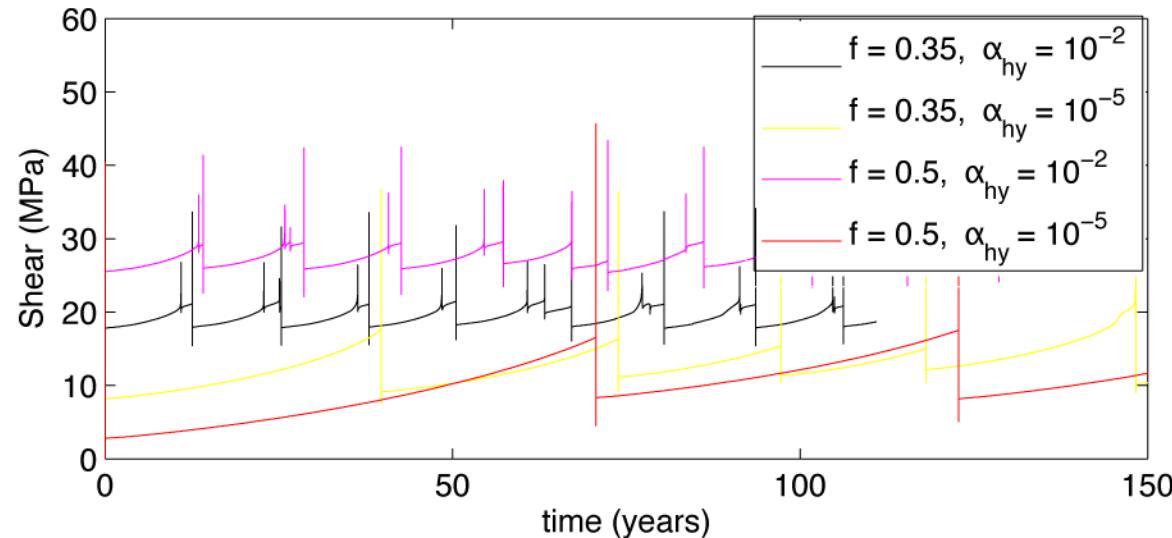
## 4. 2-3D Dynamic simulation

### Model set-up



## 4. 2-3D Dynamic simulation

### Dynamic friction, stress drop and recurrence



# Conclusion

