

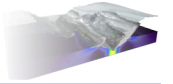
AuScope & Lagrangian-Eulerian consistent AMR

Steve Quenette

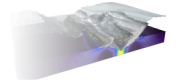
Louis Moresi,

Luke Hodgkinson & Dave May

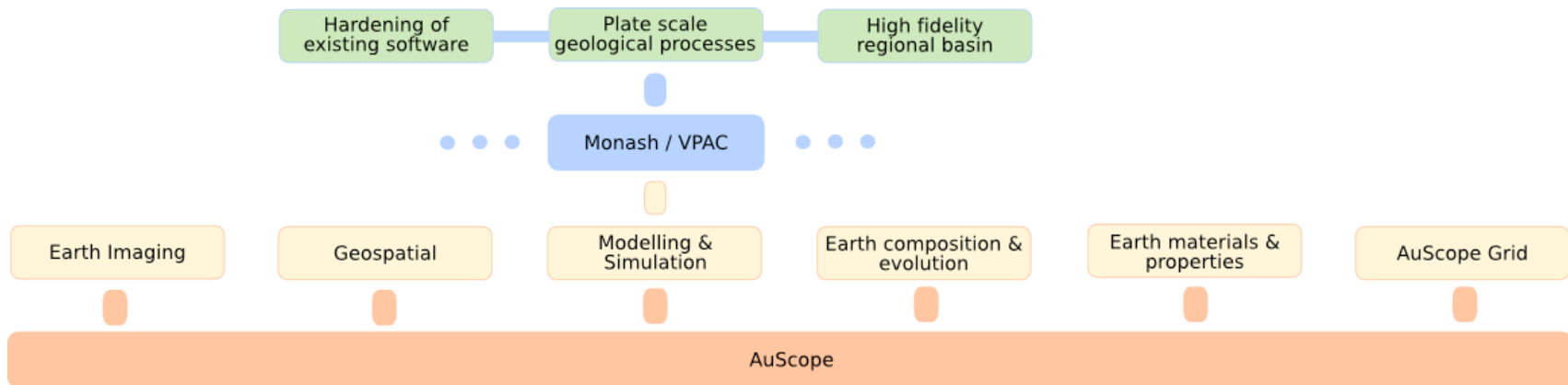
CIG - AMR Workshop October 2007



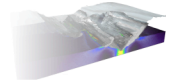
- *About us & motivations*
- *Lagrangian - Eulerian consistent AMR*



- *Provide the capability of:*
“Structure and Evolution of the Australian Continent”



- *With respect to us:*
 - *Software as infrastructure*
 - *Fabricating numerical and geophysics research*



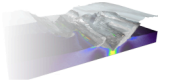
Existing: *Underworld*

- **Aspect:** geophysics
 - Isolated toolbox of rheologies and workflow revolving about Stokes flow
 - Long-term geodynamics - large deformation
- **Target models:**
 - Mantle, slab, basin, plumes, lithospheric, ...
- **Targeted numerics:**
 - FEM
 - material point history (PIC)
 - Multigrid

Bleeding-edge: *Mayhem*

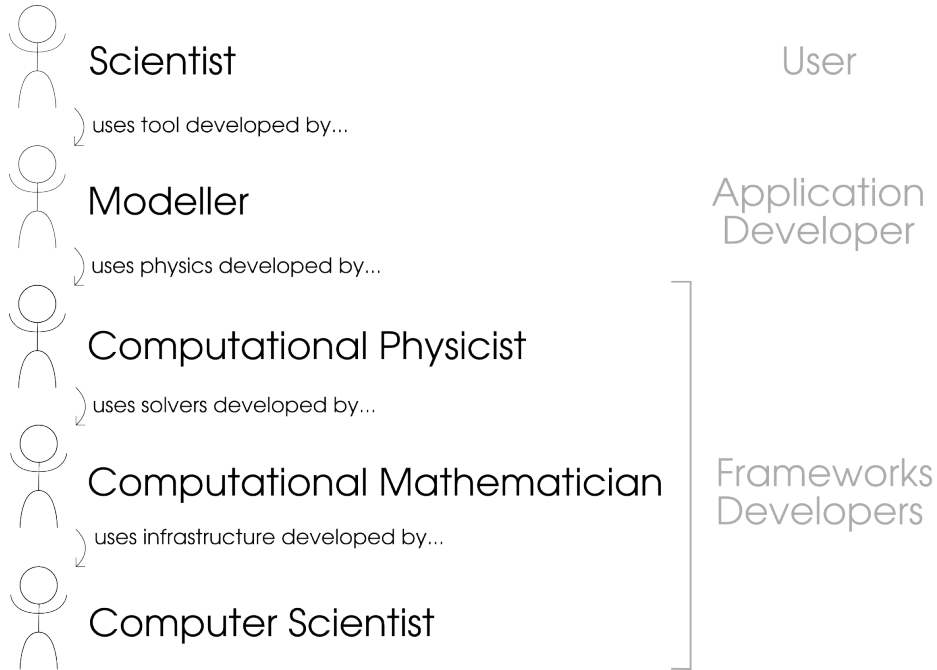
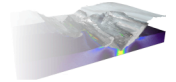
Dave May - dave.mayhem23@gmail.com

- **Aspect:** numerics
 - Research into AMR techniques optimised for Stokes and FEM with material point methods (Lagrangian-Eulerian consistent AMR)
- **Origin:** isolated research code
 - Serial
 - Not applied to involved geophysical problem
- **Objective:**
 - Consolidate into framework
 - plugin into existing phenomena models



- *We're interested in an environment where:*
 - *Numerical schemes & physics can change with minimal impact on existing phenomena models*
 - *Hardware proofing (bandwidth, memory models)*
 - *Enabling multiphysics*
 - *Enabling scaling*

- *Our solution:*
 - *StGermain*
 - *Aspect oriented*
 - *“Composition” of phenomena models by isolated numerics and physics*
 - *Enables layered frameworks & expectation alignment*



- *Spans C & XML*

- *Abstraction of concepts at all levels*

- *CP: MoresiMulhous*

- *CM: Field*

- *CS: Component*

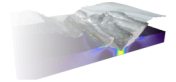
- ...

- *Interchangability*

```

<struct name="components" mergeType="merge">
  <struct name="mantleShape">
    <param name="Type">Box</param>
    <param name="startX"> minX </param>
    <param name="startY"> 0.0 </param>
    <param name="startZ"> minZ </param>
  </struct>
  <struct name="mantleShape2">
    <param name="Type">Union</param>
    <list name="shapes">
      <param>mantleShape</param>
      <param>weakZoneShape</param>
    </list>
  </struct>
</struct>

```



- *Domain & Discretisation*

- *Meshing*

- *Structured - 1 to 3d decomposition*
- *Unstructured - less mature*
- *Incidence graph technique*
- *Render out to flat arrays (Fortran like FEM)*

- *Particles*

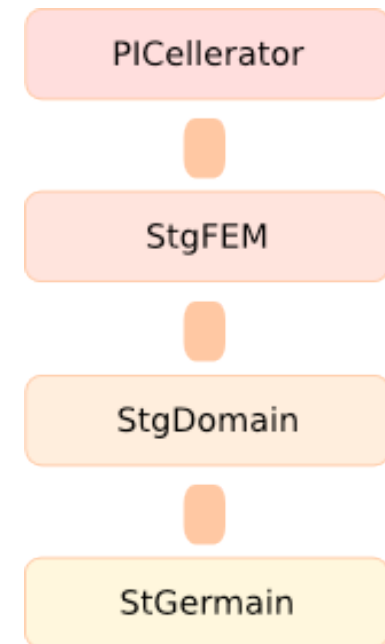
- *Complicated to optimise*

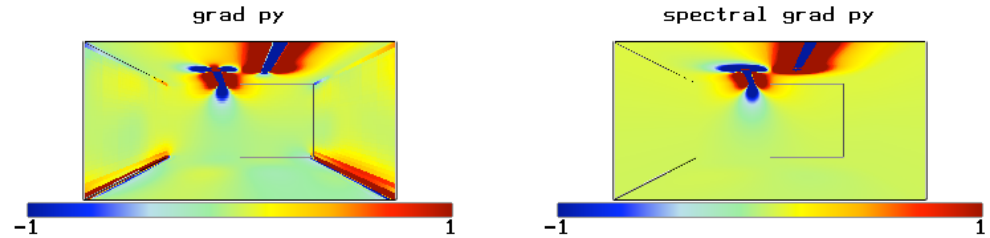
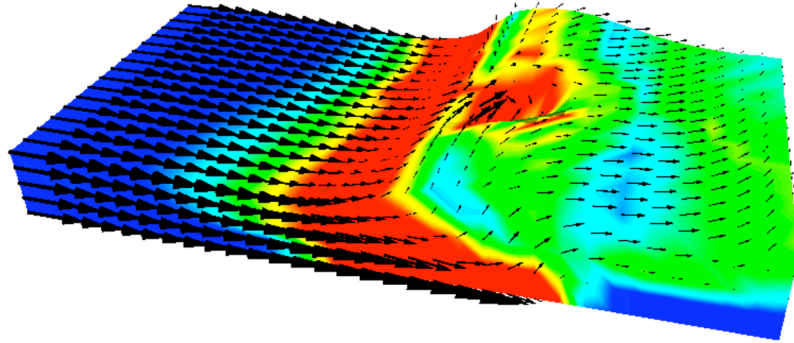
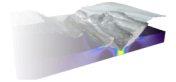
- *FEM*

- *Abstract out fields (bundles)*
- *(have had versions with optimal numbering)*

- *Summary*

- *Expensive to develop.*
- *Years of use.*
- *Its all book keeping!*



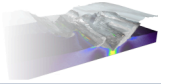


Existing: *GALE*

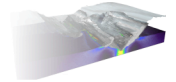
- GALE solves the Stokes and heat transport equations with a large selection of viscous and plastic rheologies.
- *Target models:*
 - orogenesis, rifting, and subduction, ...
- *Targeted numerics:*
 - Underworld (FEM,PIC) + free surface + ...

Bleeding-edge: *MADDs*

- Explore how magma dynamics interacts with mantle convection and/or long-term tectonics
- *Target models:*
 - *mor*, ...
- *Targeted numerics:*
 - Present thinking... Mixed FEM(PIC)-FV, \geq quadratic

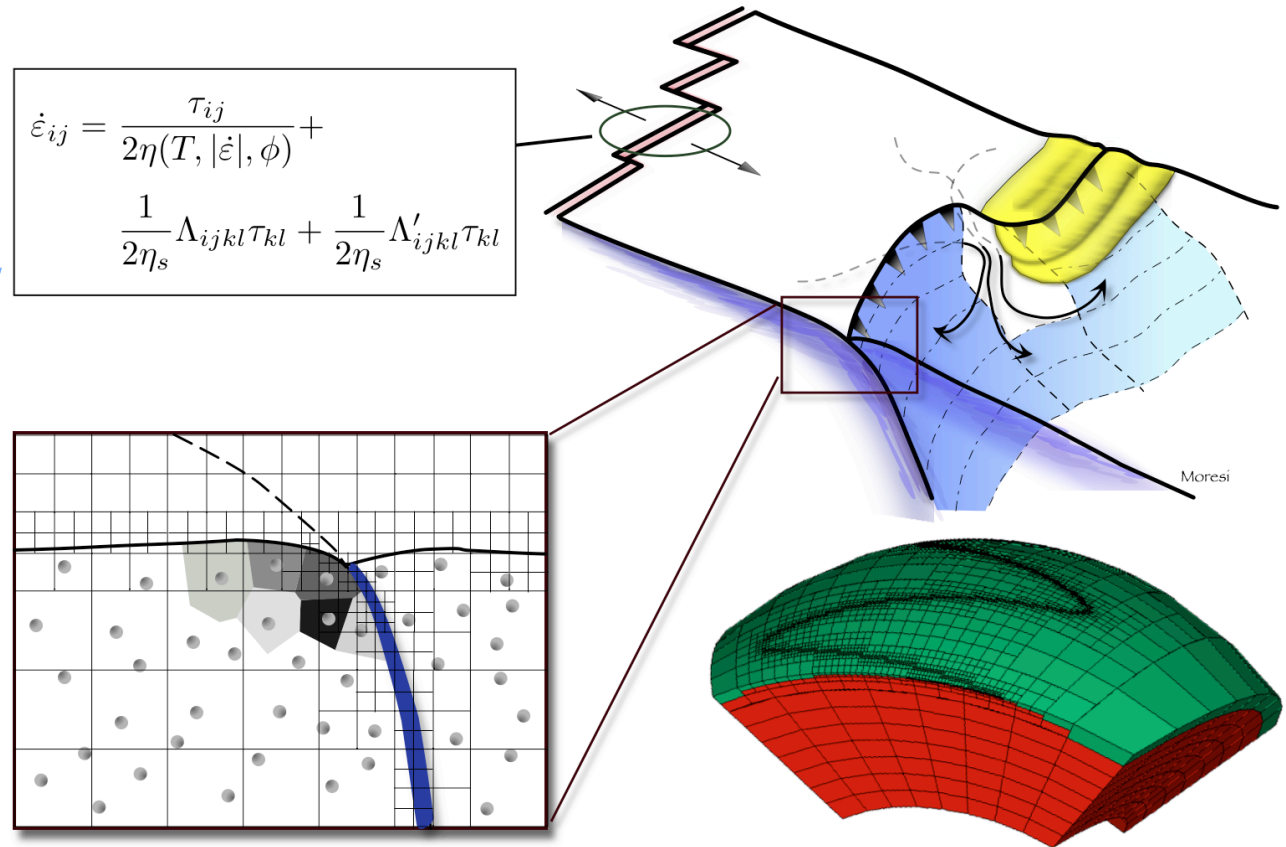


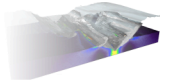
Ok, ok, but what about AMR?



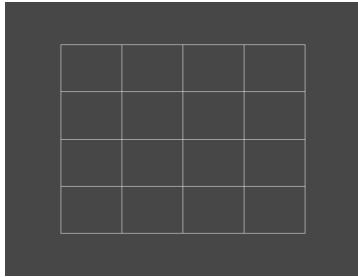
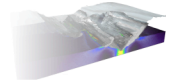
- *Either at the scale of:*
 - *Rifting & subduction*
 - *Graven*
- *Embedded within a greater lithospheric & mantle context*
- *Material point vs mesh density at a given point*

$$\dot{\epsilon}_{ij} = \frac{\tau_{ij}}{2\eta(T, |\dot{\epsilon}|, \phi)} + \frac{1}{2\eta_s} \Lambda_{ijkl} \tau_{kl} + \frac{1}{2\eta_s} \Lambda'_{ijkl} \tau_{kl}$$





1. *Distributed memory parallel meshing infrastructure*
 - *Mixed tree & flat array based system*
2. *AMR aware FEM book-keeping*
 - *Refinement models*
3. *AMR aware PIC*
 - *Global Voronoi*
4. *AMR aware Multigrid, levelsets, ...*

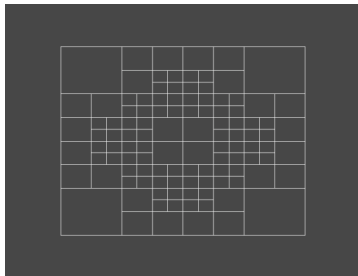


- *Implemented the distributed memory parallel meshing infrastructure*

- *C example...*

```
int newCells[4];
AdjTopology* topo;
AdjSet* coords;

topo = AdjTopology_New();
newCells[0] = AdjTopology_MakeQuad( topo );
AdjTopology_RefineQuad( topo, newCells[0], newCells );
AdjTopology_RefineQuad( topo, newCells[0], newCells );
```

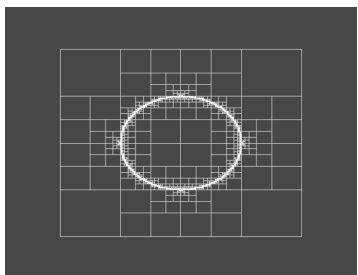
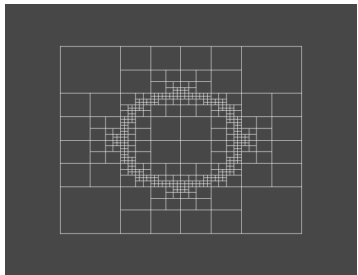


- *From an API that looks like...*

```
int MakeVertex( void* self );
void KillVertex( void* self, int id );
int Lift( void* self, int dim, int nSubCells, int* subCells );
void Unlift( void* self, int dim, int id );
int Join( void* self, int dim, int leftID, int rightID );
```

```
void RefineHexa( void* self, int cell, int *newCells );
void RefineQuad( void* self, int cell, int *newCells );
void RefineEdge( void* self, int cell, int *newCells );
```

```
void Update( void* self );
```



Desired outcome...

