

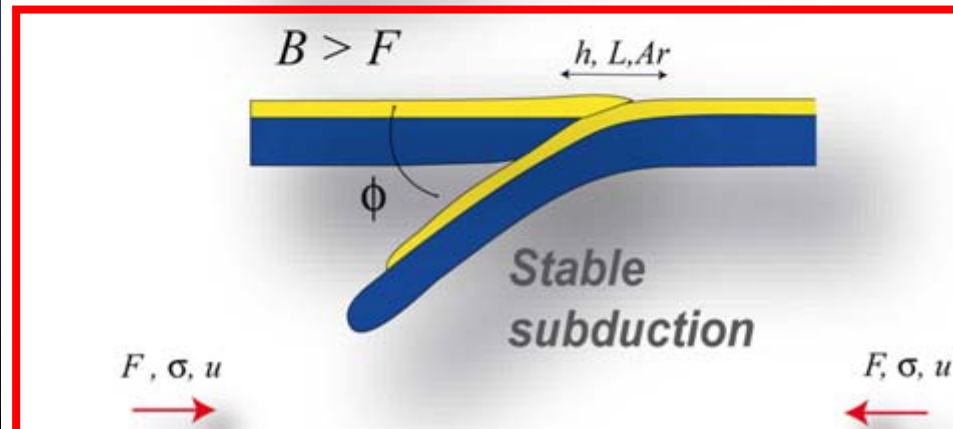
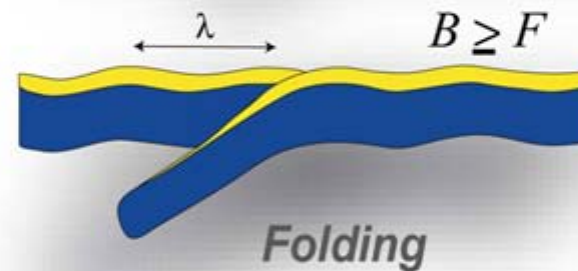
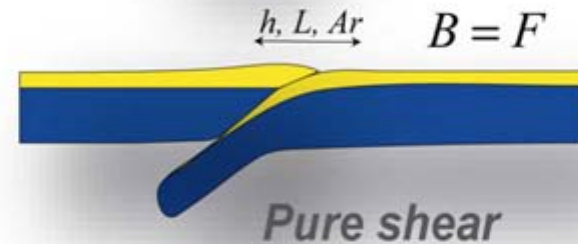
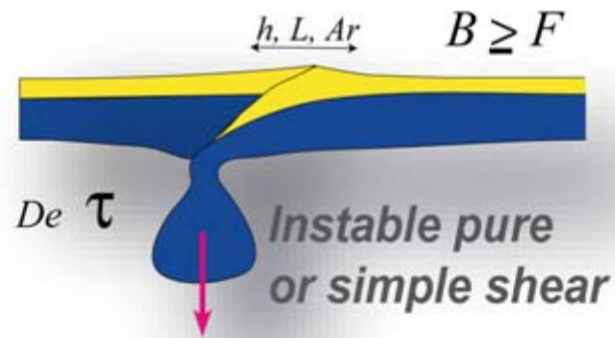


*Convergent margins
processes*

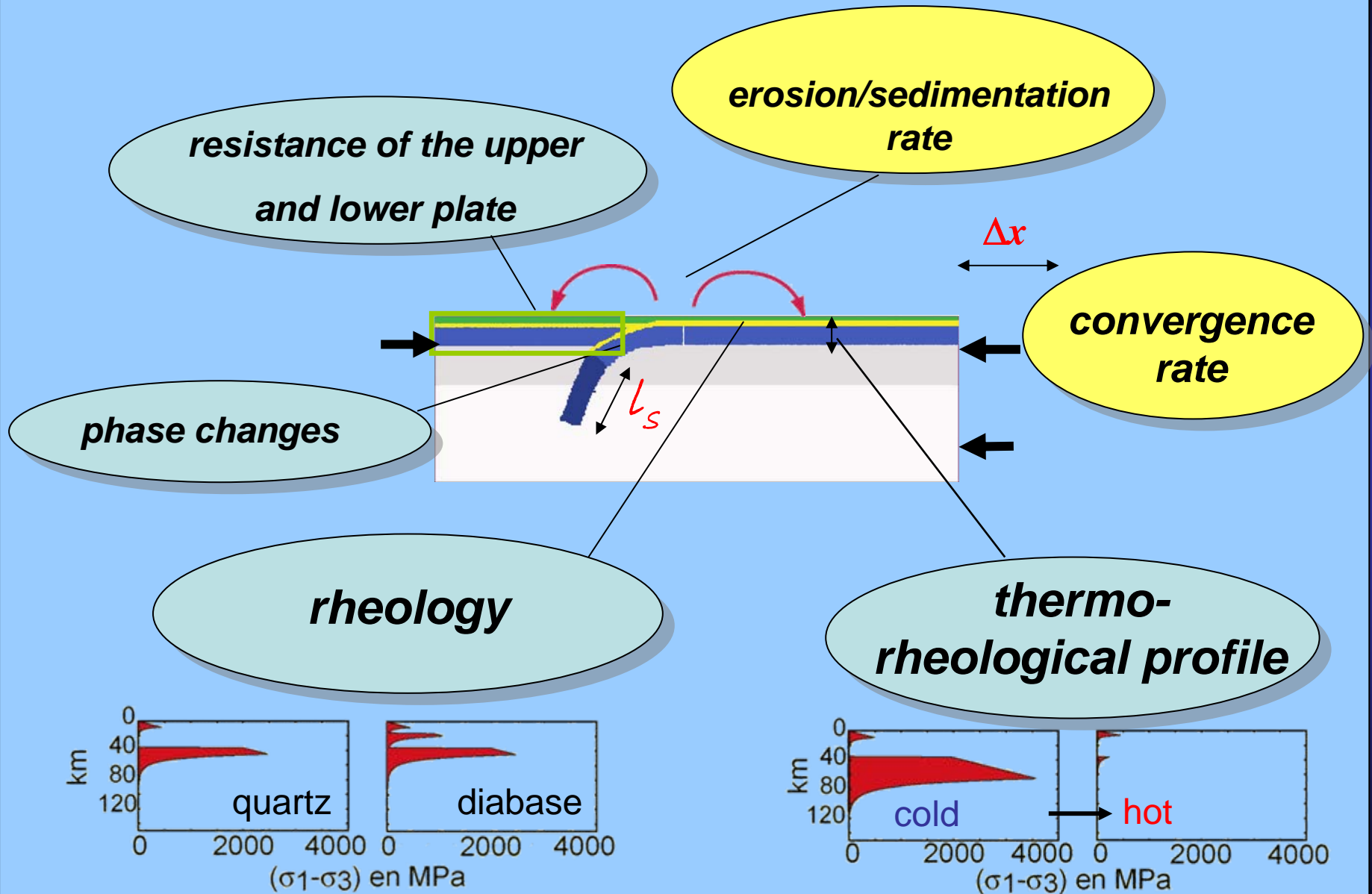
E. Burov

University of Pierre et Marie Curie

four possible collision modes



important controlling parameters of subduction



SUBDUCTION NUMBER:

$$S = \frac{\Delta x}{L_s}$$

(subduction length)

SUBDUCTION FEASIBILITY:

Peclet number $\gg 1$

$$Pe = \frac{\text{advection rate}}{\text{diffusion rate}}$$

Numerical method

$$\Rightarrow \rho g_i + \frac{\partial \sigma_{ij}}{\partial x_j} = \rho \frac{\partial V_i}{\partial t}$$

Newton's 2nd law of motion

$$\Rightarrow \frac{DT}{Dt} = \frac{\partial}{\partial x_i} \left(\chi \frac{\partial T}{\partial x_i} \right) + \frac{H_r}{\rho C_p} - V_i \frac{\partial T}{\partial x_i}$$

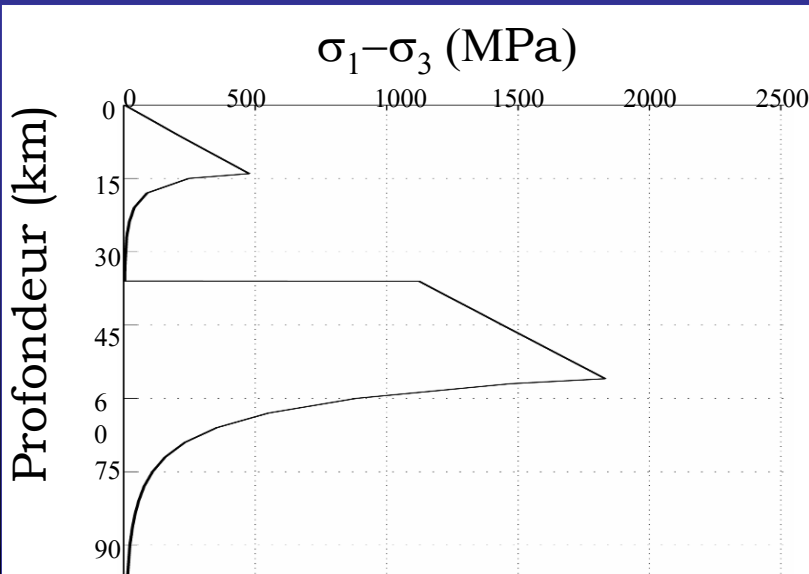
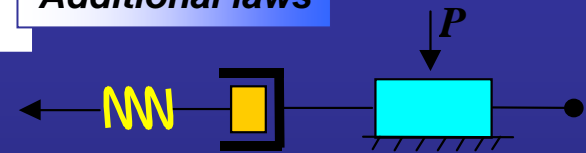
Heat Diffusion, Production, Advection

$$\Rightarrow \frac{D\sigma}{Dt} = F(\sigma, \mathbf{u}, \mathbf{V}, \nabla \mathbf{V}, \dots, T, \dots)$$

Constitutive laws

$$\Rightarrow \rho = f(P, T) \quad \Rightarrow \partial h_s / \partial t - \nabla(k_e (\nabla h)^m \nabla h_s) = 0$$

Additional laws



Viscous

$$\dot{\epsilon} = A \exp\left(-\frac{E}{RT}\right) \sigma^n$$

Elastic

$$\sigma_{ij} = \lambda \delta_{ij} \sum_k \epsilon_{kk} + 2\mu \epsilon_{ij}$$

Plastic

$$\tau = (\tan \varphi) \sigma_n + C_0$$

Gaussian difference equations for polygonal elements (Malvern, 1969)

$$\int_s n_i f ds = \int_A \frac{\partial f}{\partial x_i} dA$$

where \int_s is the integral around the boundary of a closed surface;

n_i is the unit normal to the surface, s ;

f is a scalar, vector or tensor;

x_i are position vectors;

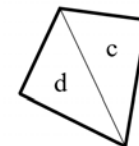
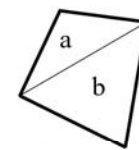
ds is an incremental arc length; and

\int_A is the integral over the surface area,

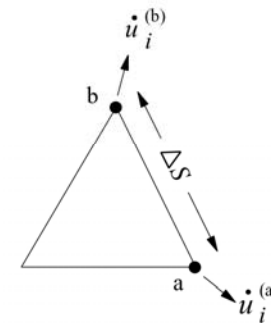
$$\left\langle \frac{\partial f}{\partial x_i} \right\rangle = \frac{1}{A} \int_A \frac{\partial f}{\partial x_i} dA$$

$$\left\langle \frac{\partial f}{\partial x_i} \right\rangle = \frac{1}{A} \int_S n_i f ds$$

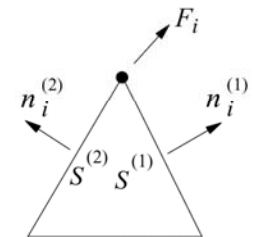
The grid



(a)



(b)



(c)

Strain - stress - force - velocity increments

$$\Delta \varepsilon_{ij}^{(e)} = \frac{1}{2} \left(\frac{\partial v_i^{(e)}}{\partial x_j} + \frac{\partial v_j^{(e)}}{\partial x_i} \right) \Delta t$$

$$\frac{\partial v_i^{(e)}}{\partial x_1} = \sum_{k=1}^3 v_i^{(k)} \cdot \beta_k, \quad \frac{\partial v_i^{(e)}}{\partial x_2} = \sum_{k=1}^3 v_i^{(k)} \cdot \gamma_k.$$

$$\sigma_{ij}^{(e)} = M(\sigma_{ij}^{(e)}, \Delta e_{ij}^{(e)}, S_i)$$

$$F_i^{(n)} = - \sum \frac{1}{2} \sigma_{ij}^{(e)} (n_j^{(1)} \Delta l^{(1)} + n_j^{(2)} \Delta l^{(2)})$$

$$v_i^{(n)}(t + \Delta t) = v_i^{(n)}(t) + [F_i^{(n)} - \alpha |F_i^{(n)}| \text{sign}(v_i)] \frac{\Delta t}{m_{inert}}$$

The damping term

Large strain formulation
(Jaumann's correction)

$$dt_{crit} = \min \left(\frac{\Delta x}{\sqrt{K/\rho_{inert}}}, \frac{\eta}{G} \right)$$

$$Re = \frac{\rho_{inert} V L}{\eta}$$

$$\sigma_{ij} := \sigma_{ij} + (\omega_{ik} \sigma_{kj} - \sigma_{ik} \omega_{kj}) \Delta t$$

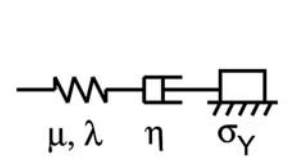
where

$$\omega_{ij} = \frac{1}{2} \left\{ \frac{\partial \dot{u}_i}{\partial x_j} - \frac{\partial \dot{u}_j}{\partial x_i} \right\}$$

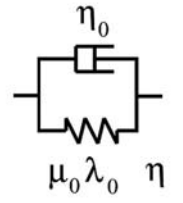
$$\left. \begin{aligned} \bar{e} &= \dot{\epsilon}_{ii} / 3 \\ e_{ij} &= \dot{\epsilon}_{ij} - \delta_{ij} \bar{e} \\ \bar{\sigma} &= \sigma_{ii} / 3 \\ \tau_{ij} &= \sigma_{ij} - \delta_{ij} \bar{\sigma} \end{aligned} \right\}$$

$$\left\{ \begin{aligned} \epsilon^{\text{elas}} + \epsilon^{\text{vis}} + \epsilon^{\text{plast}} - \epsilon &= 0 \\ e^{\text{elas}} &= \dot{\tau} / 2G \quad \text{elastic part} \\ e^{\text{vis}} &= \tau / 2\eta \quad \text{viscous part} \\ F &= \tau^* + \sin \phi \sigma^* - \cos \phi C_0 \\ \tau^* &= \sqrt{(\tau_{11} - \tau_{22})^2 / 4 + \tau_{12}^2} \\ \sigma^* &= (\sigma_{11} + \sigma_{22}) / 2 = (\tau_{11} + \tau_{22}) / 2 + \bar{\sigma} \\ \frac{F(\lambda) - F^{\text{old}}}{dt} &= 0 \\ Q &= \tau^* + \sin \psi \sigma^* \\ \dot{\bar{\sigma}} &= 3K(\bar{e} - \lambda \sin \psi / 3) \\ \dot{\epsilon}_{ij}^{\text{plas}} &= \lambda \frac{\partial Q}{\partial \sigma_{ij}} \end{aligned} \right\} \text{plastic part}$$

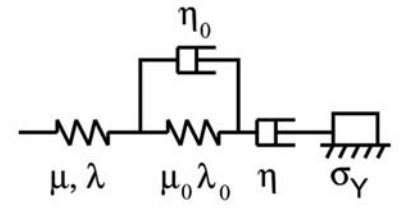
Extended Maxwell solid



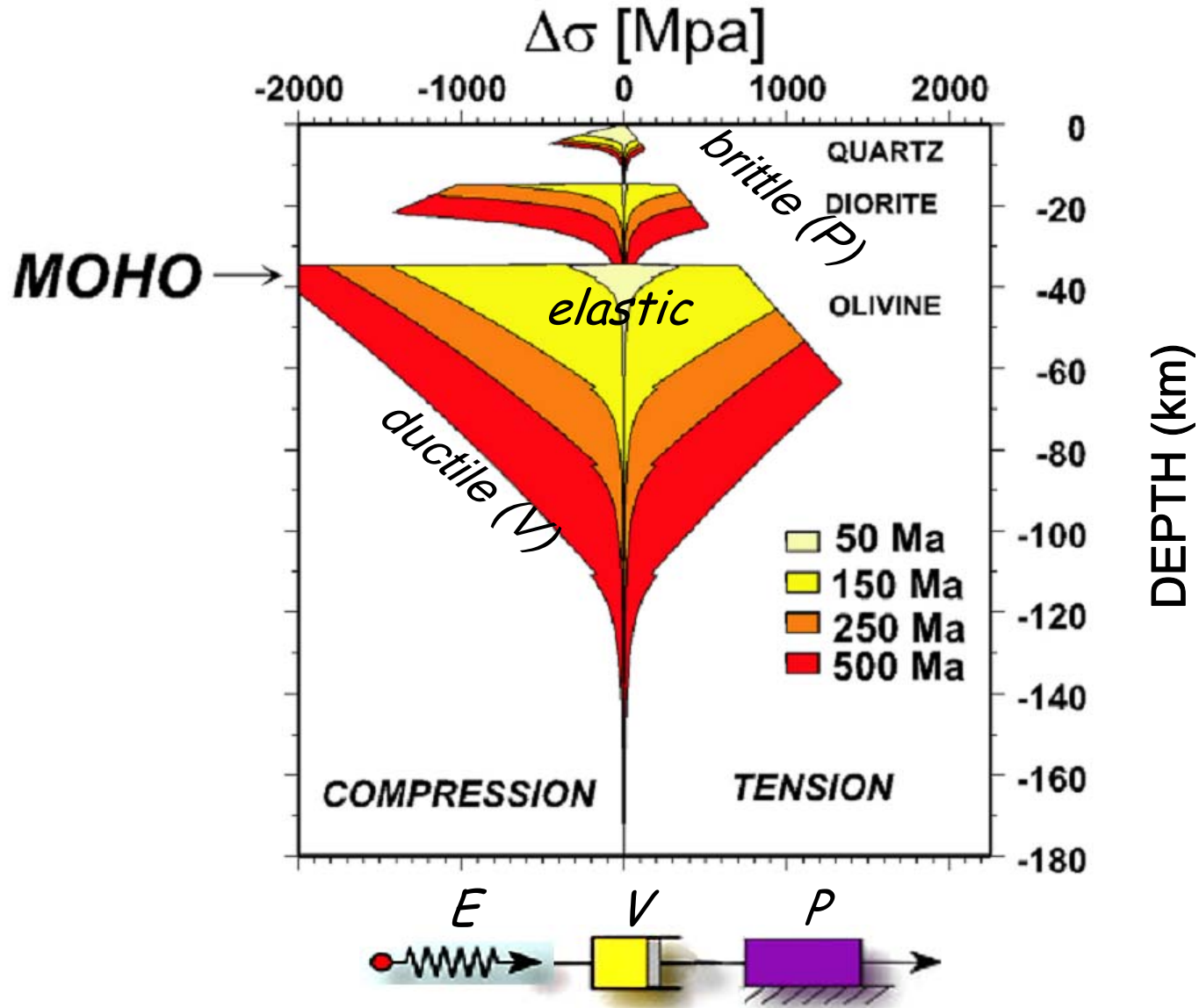
Kelvin solid



Burgers' solid



Continental Lithosphere: THICK MULTI-LAYER with EVP rheology



⇒ Erosion - sedimentation

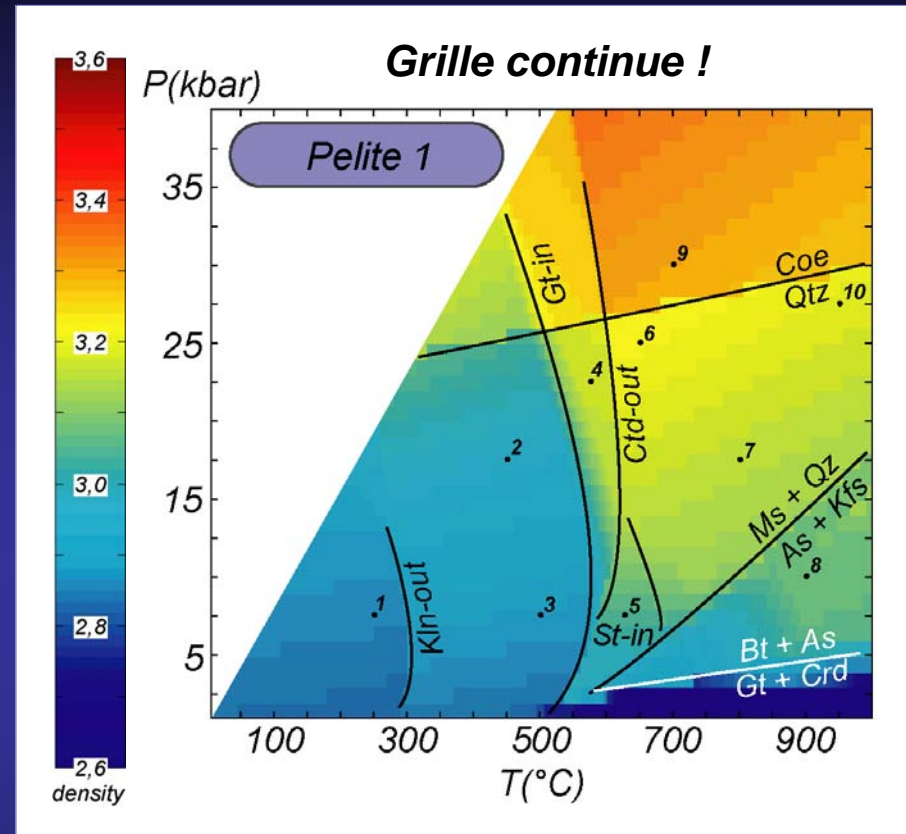
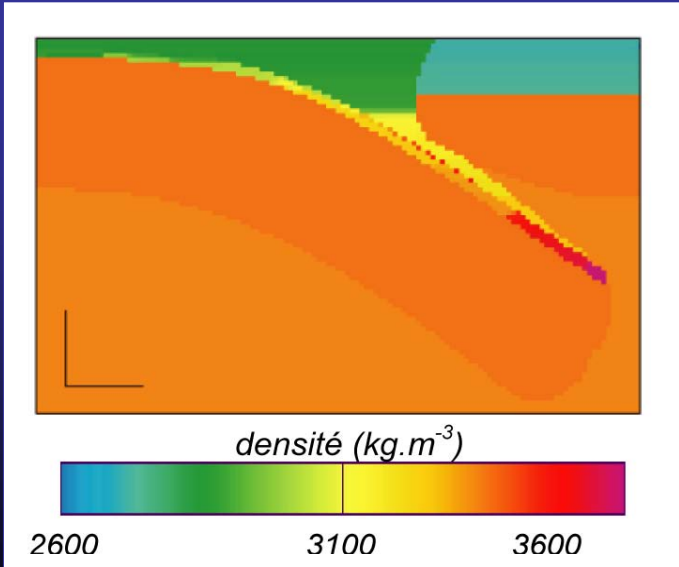
⇒ Progressive phase changes

Thermodynamic processes
(THERIAK ; PERPLEX)

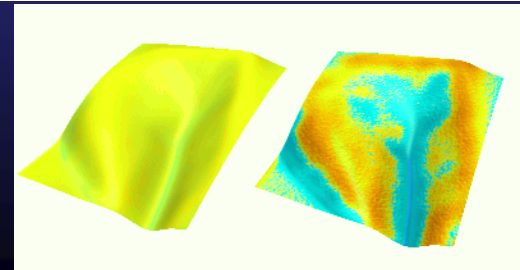
$$\rho = f(P, T)$$



$$G = \sum_{i=1}^n \mu_i N_i$$

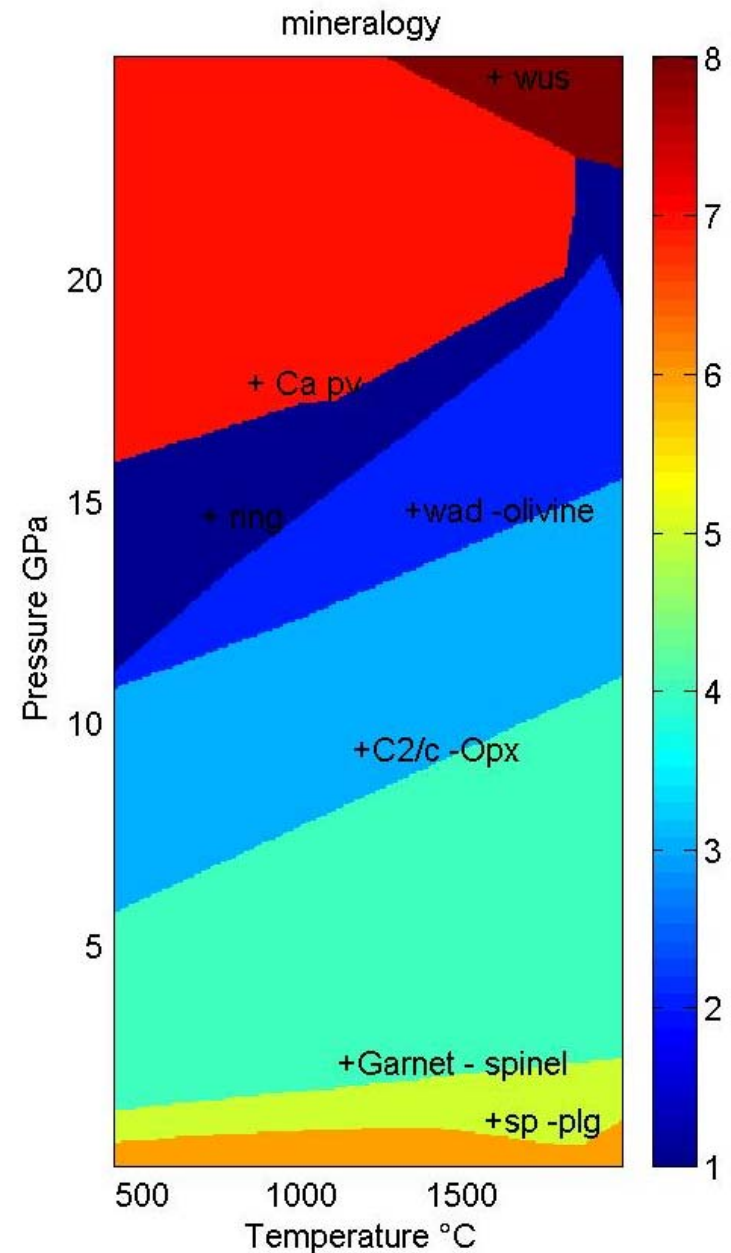
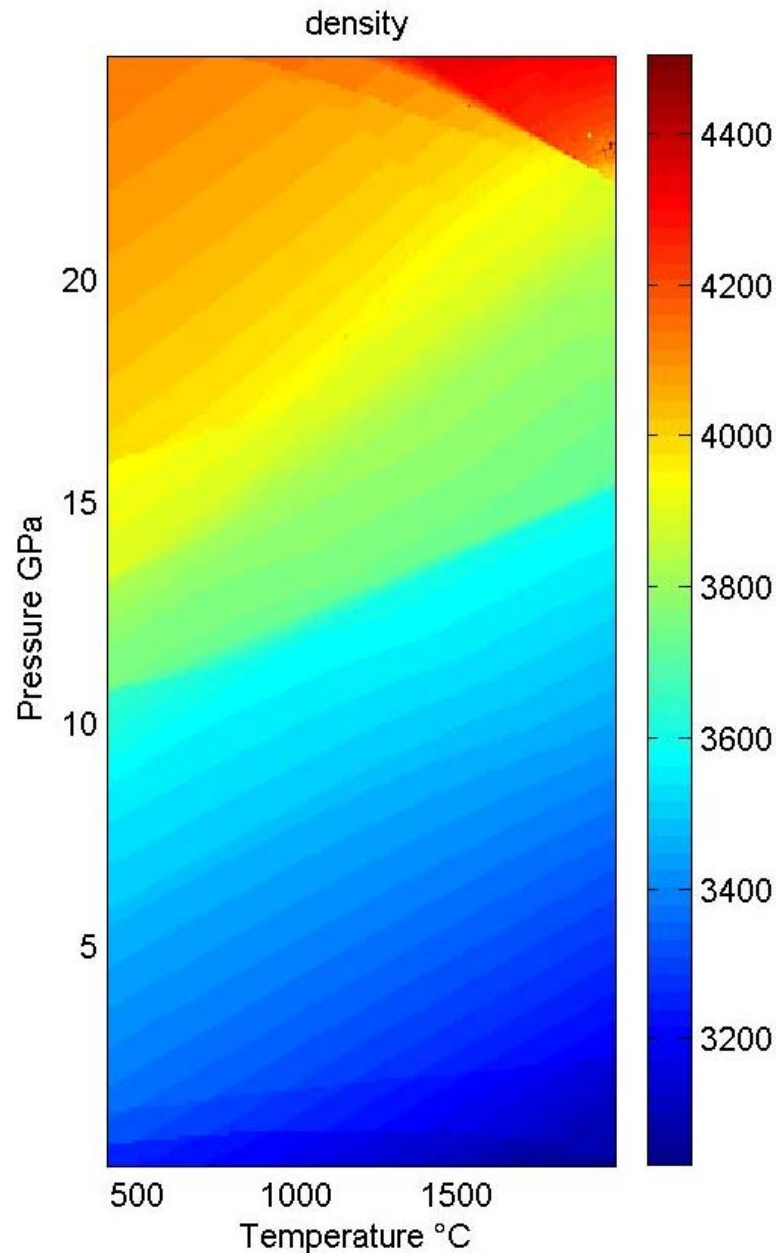


$$\partial h_s / \partial t - \nabla \cdot (k_e (\nabla h)^m \nabla h_s) = 0$$



density versus P-T for the mantle part

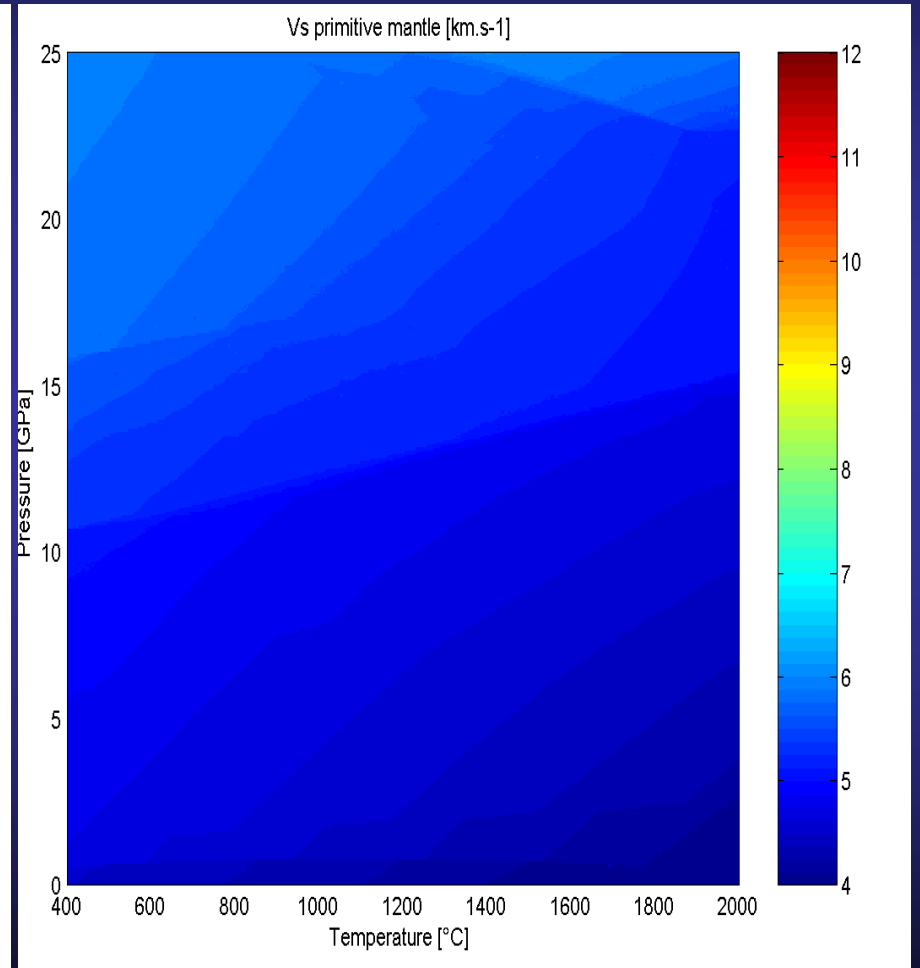
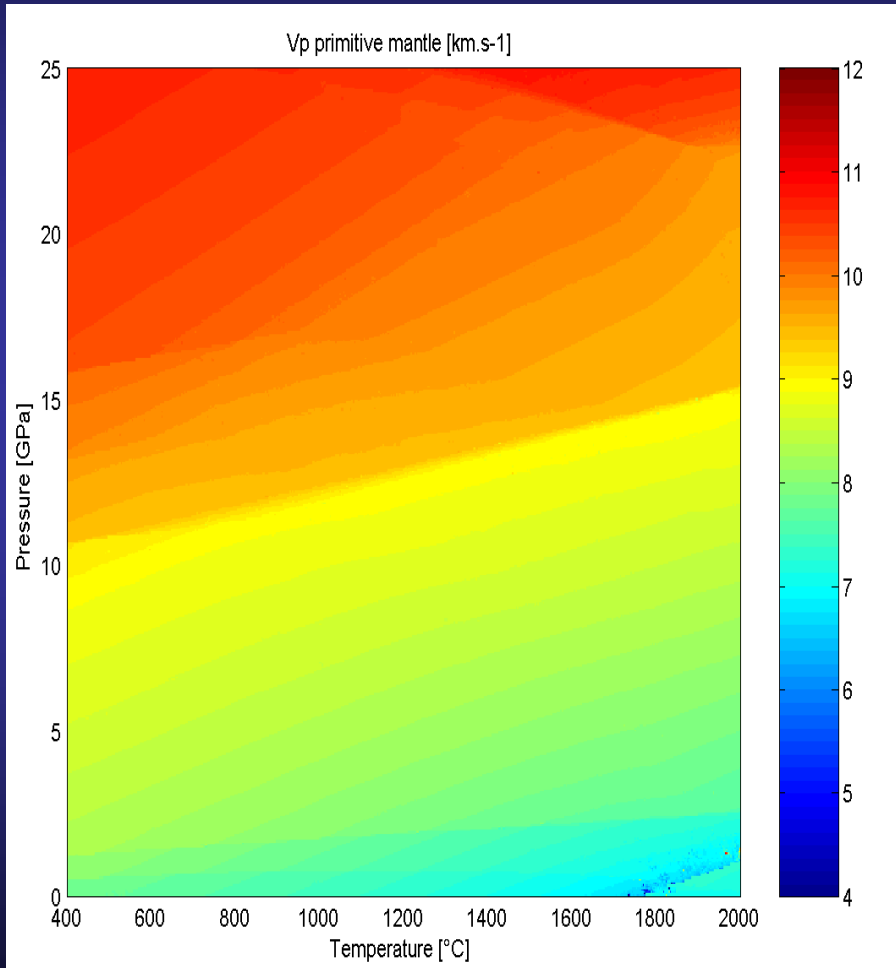
PerpleX (G. Connolly) data base

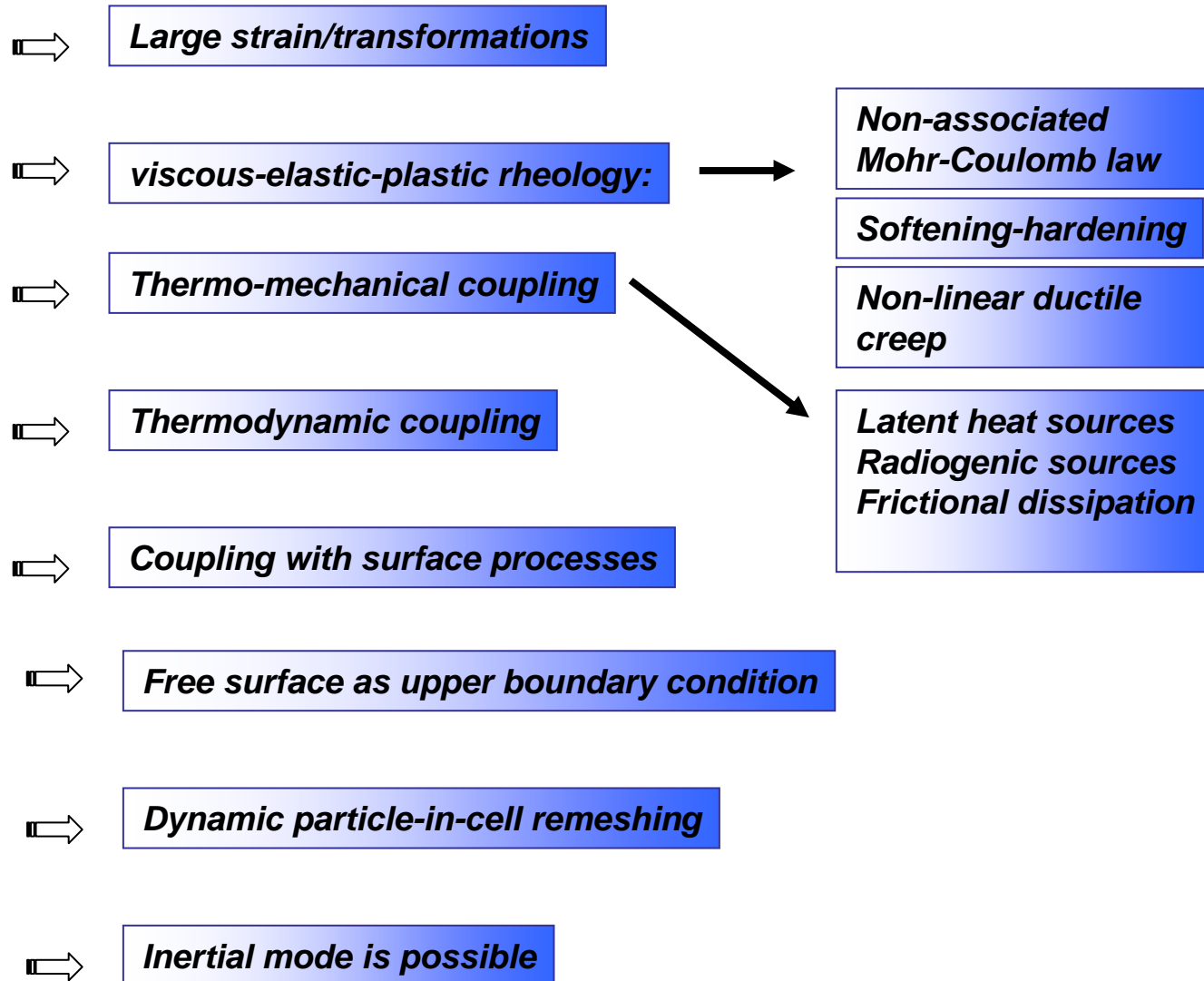


Predicted seismic velocities (m/s)

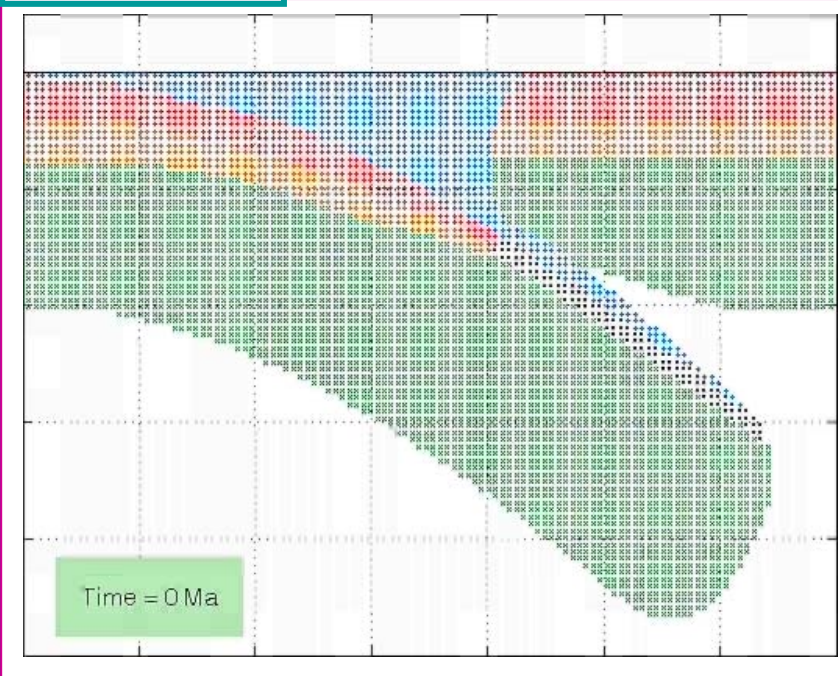
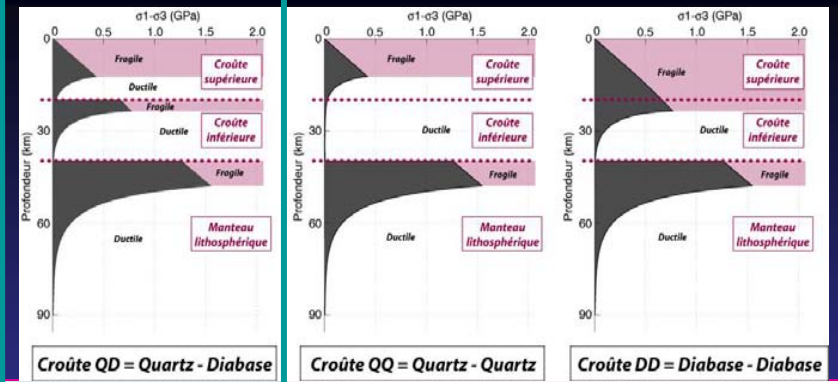
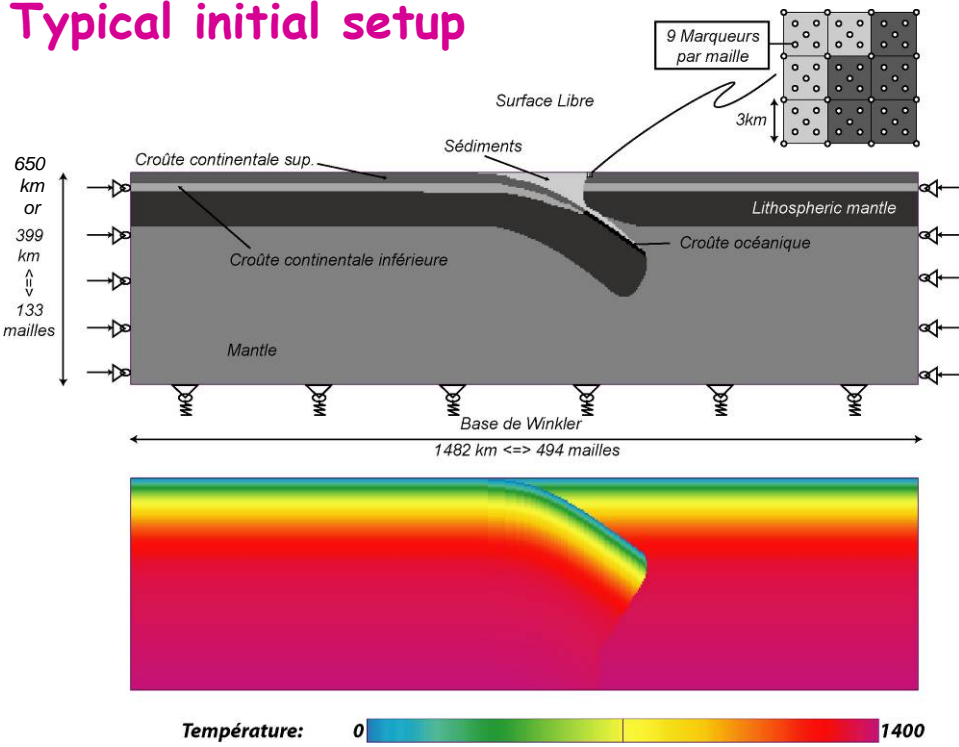
V_p

V_s

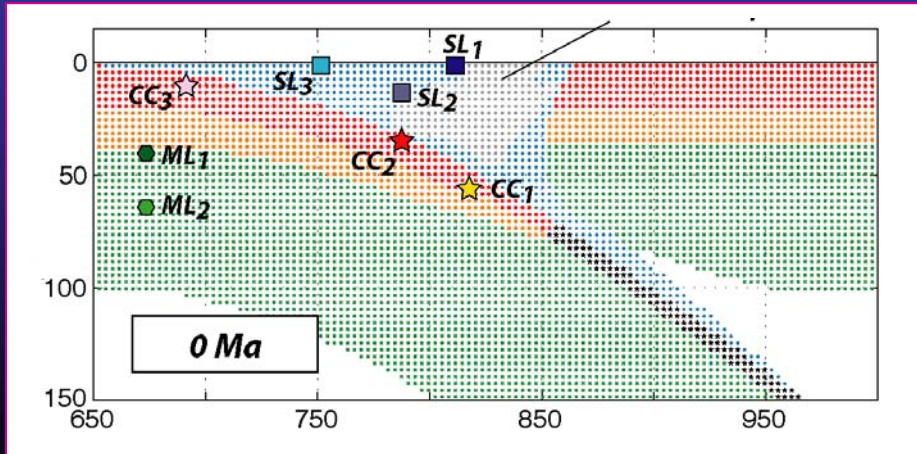




Typical initial setup



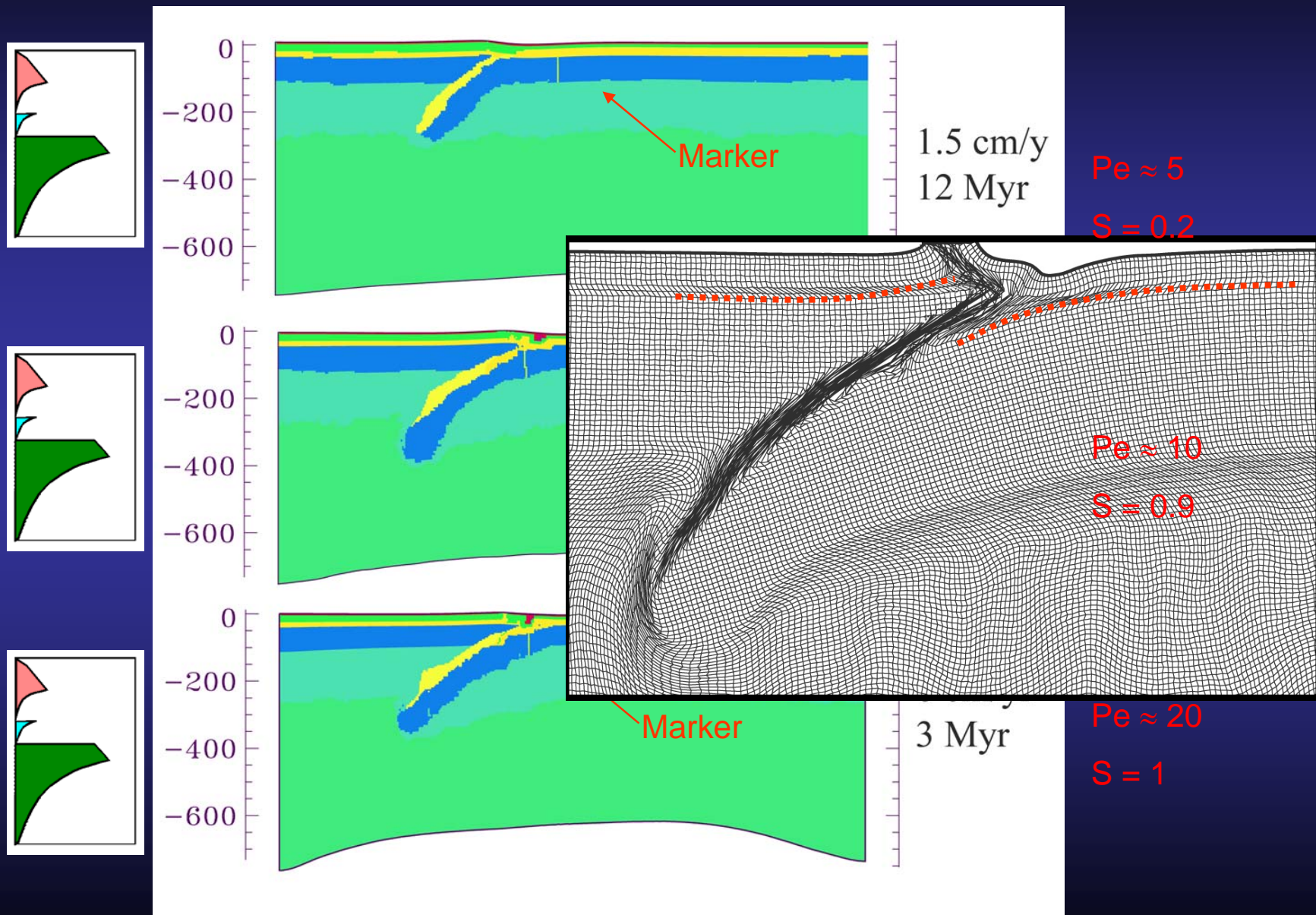
Reference experiment



Collision/Subduction experiments:

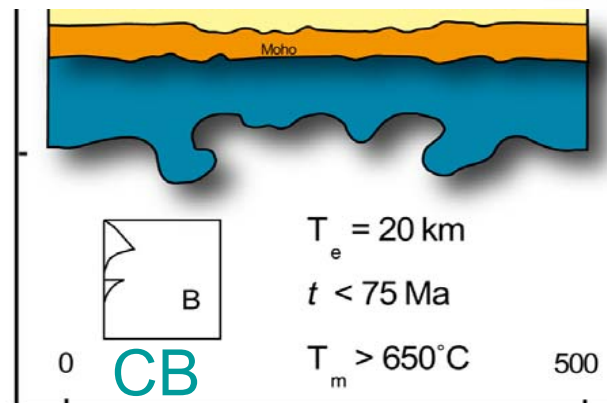
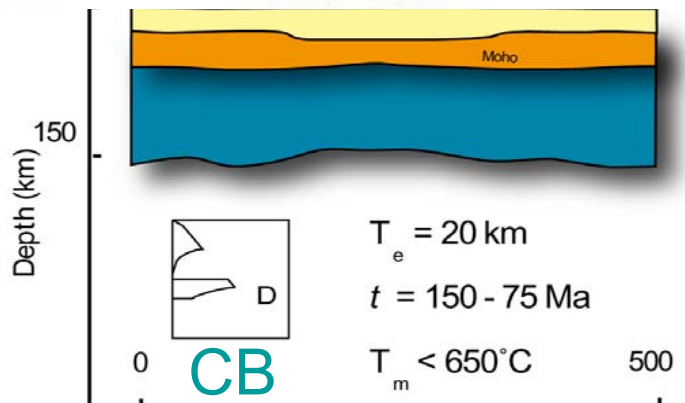
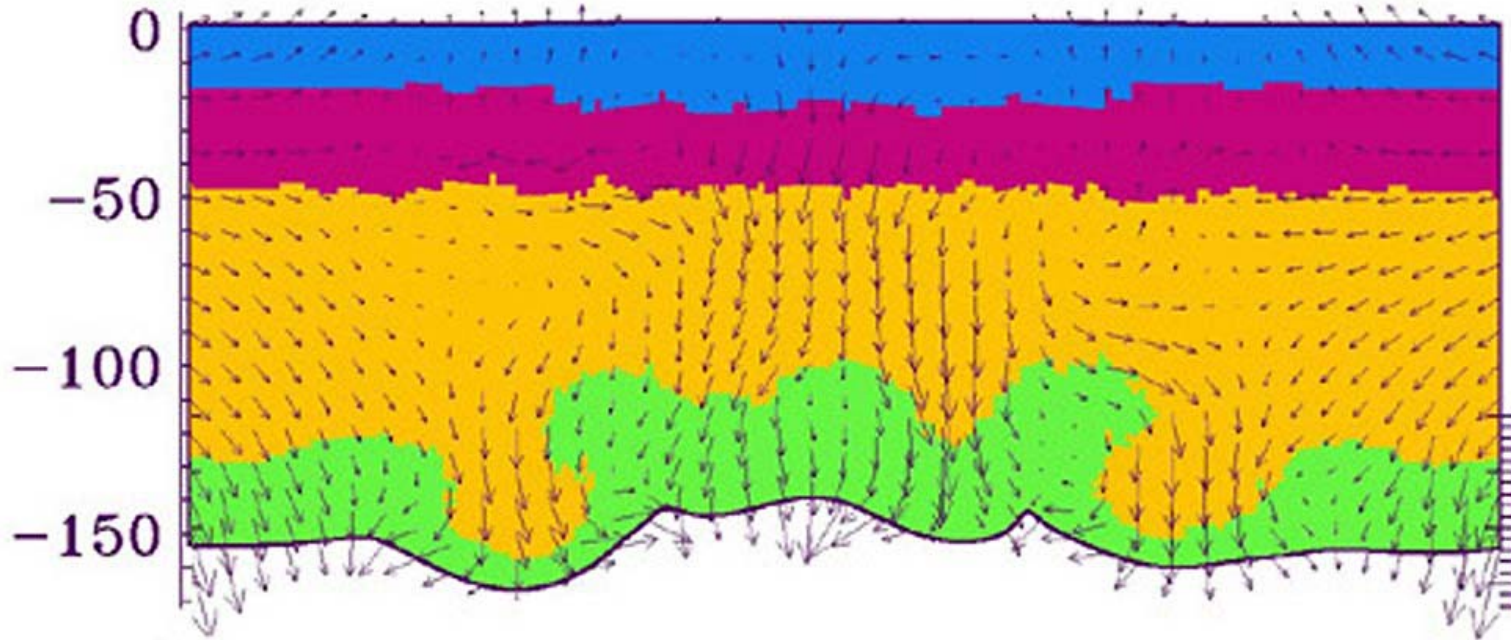
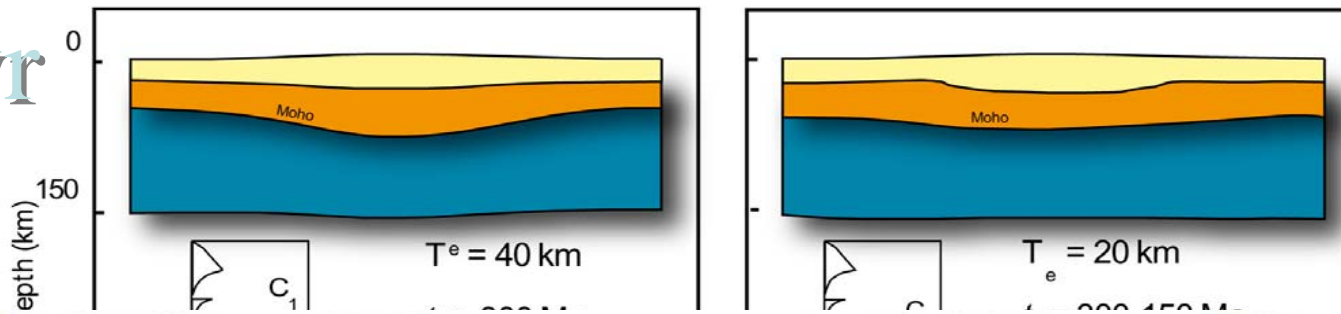
1. Influence of the convergence rate

Dependence on shortening rate. Snapshot at $\Delta x = 180$ km

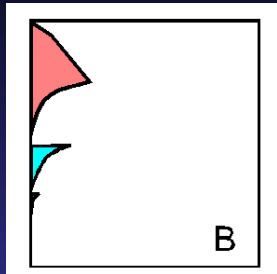


2. Influence of thermo-rheological profile

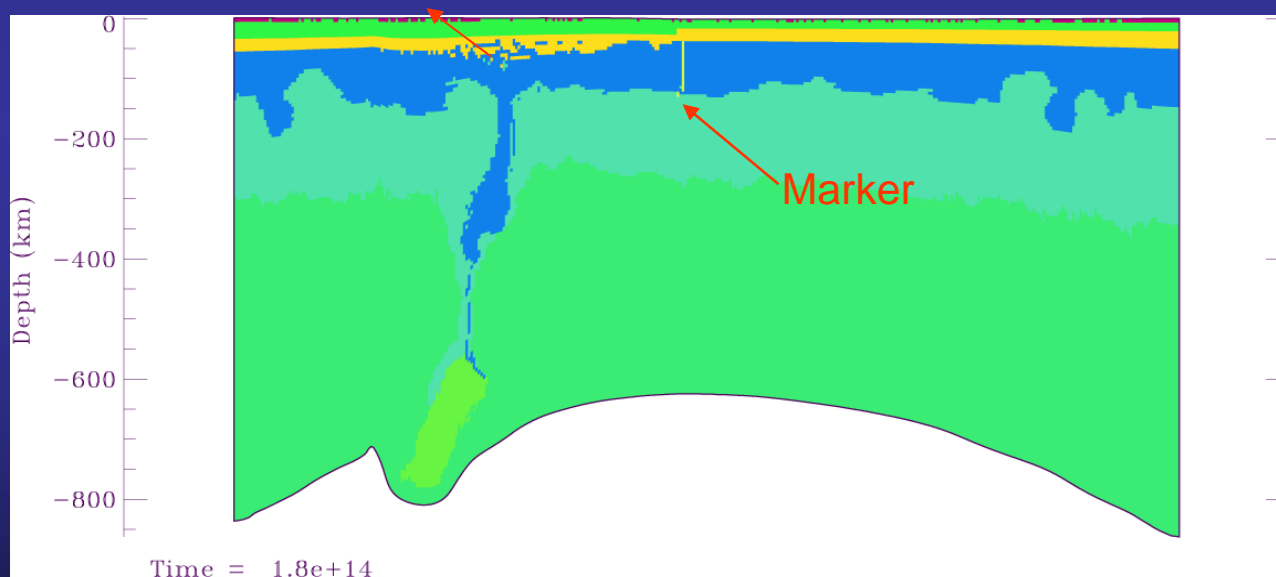
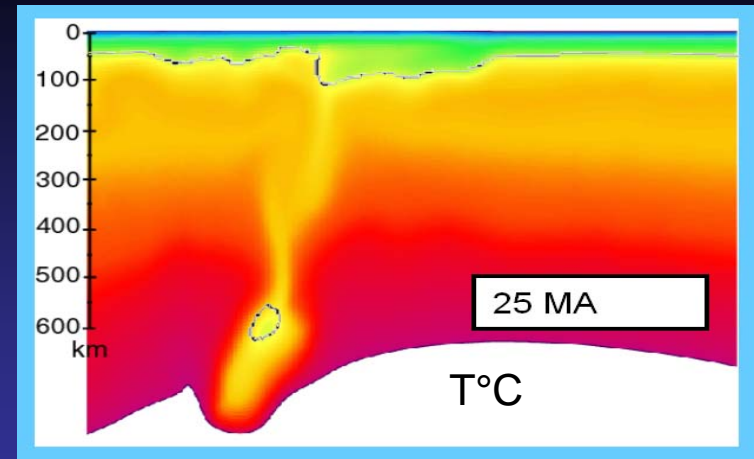
10 Myr



Influence of thermo-rheological age - A1: CREME - BRULEE RHEOLOGY (SOFT)



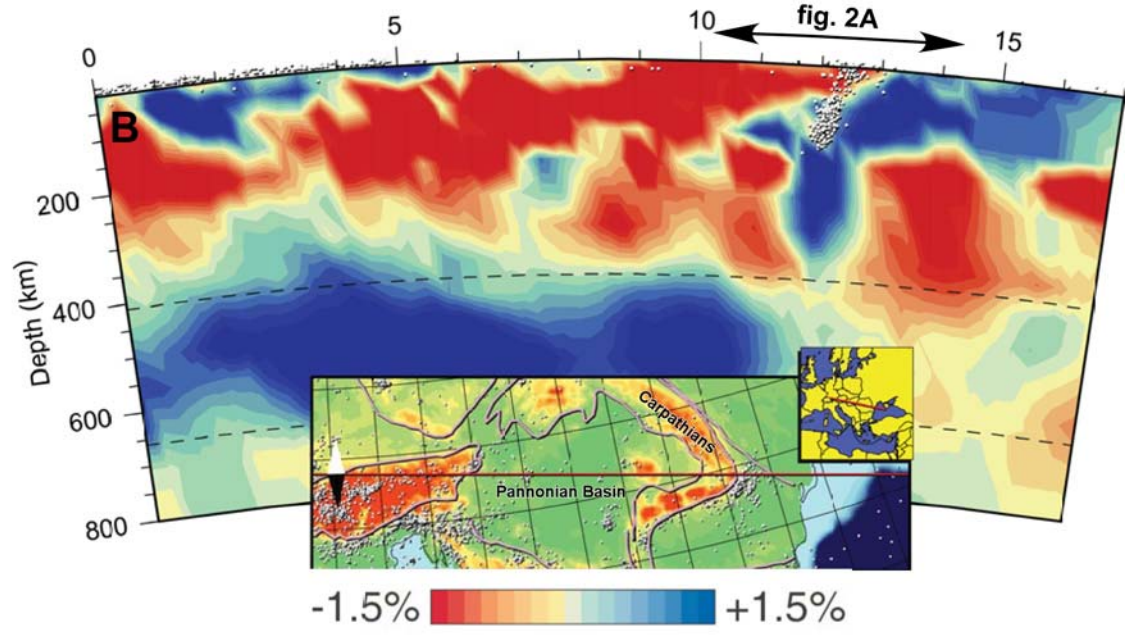
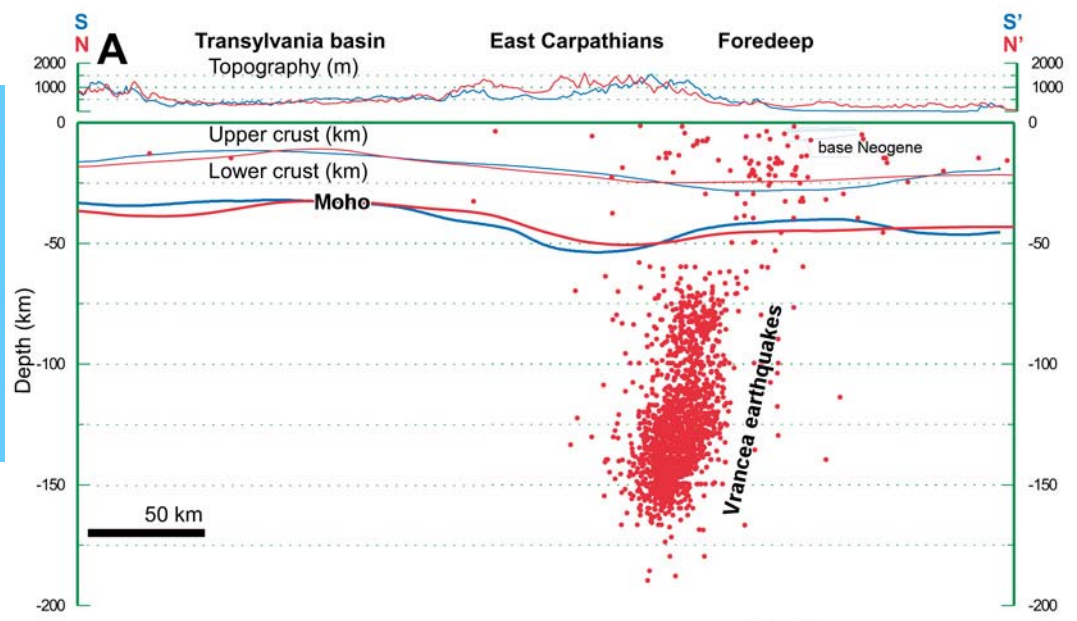
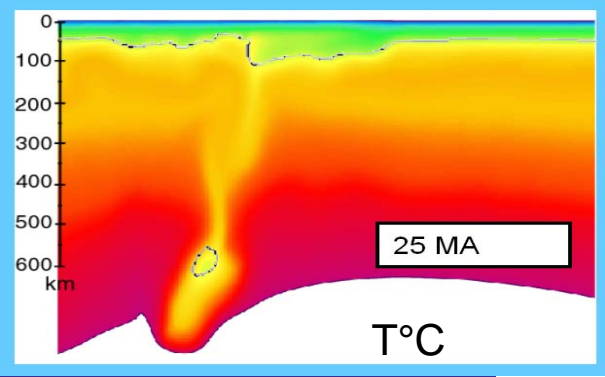
$$S < 0.1$$



Thermal age of 25 Ma $T_m = 850^\circ\text{C}$, $dx = 330$ km, $t = 5,5$ Ma, 2×3 cm/yr

wait ...

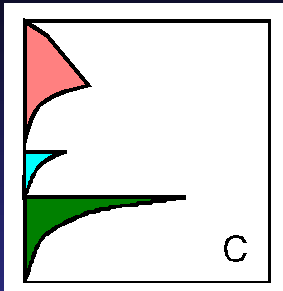
Example: Pannonian Basin / Carpathians



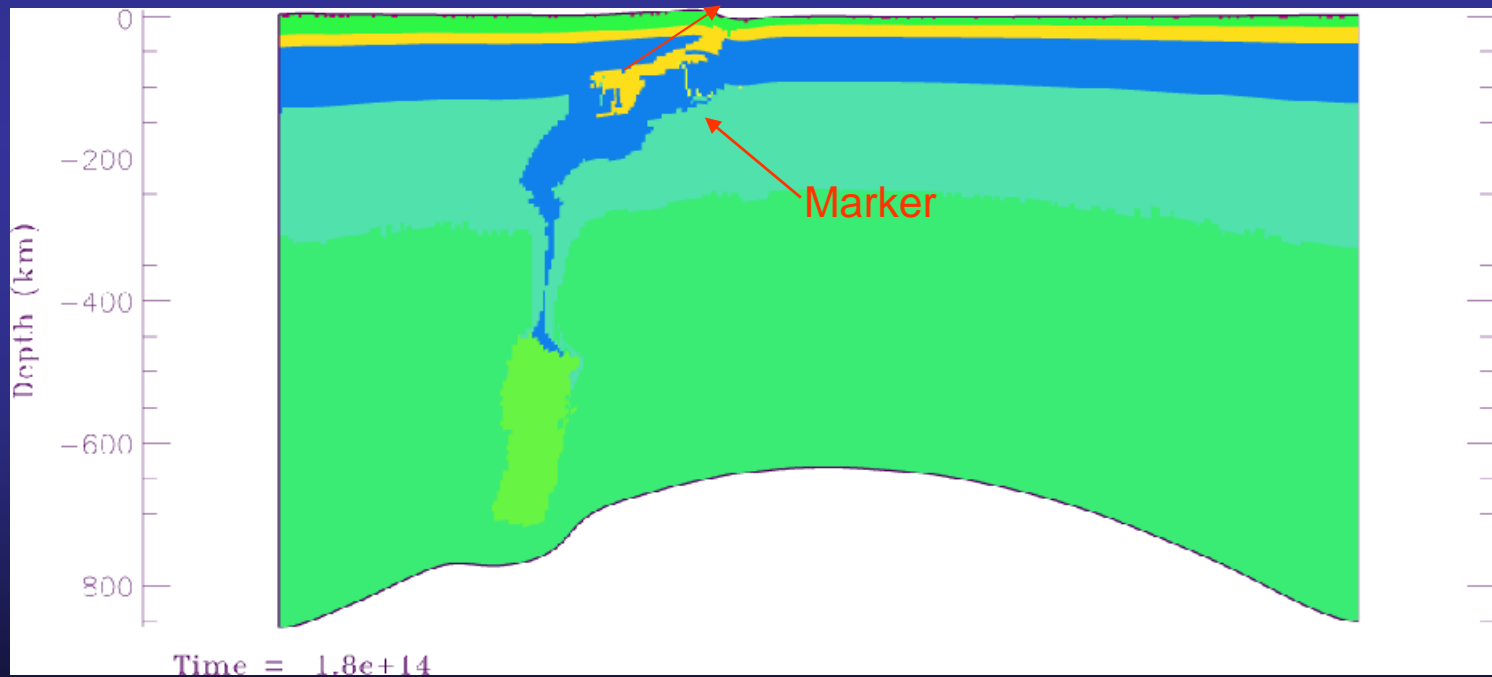
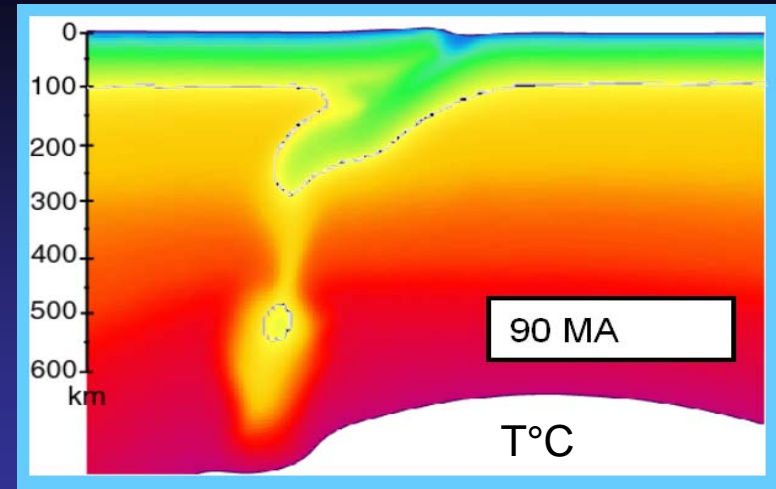
Burov et al, 2007

Figure: Spakman

Influence of thermo-rheological age - A2 JELLY SANDWICH (MIDIUM)



$S < 0.3$



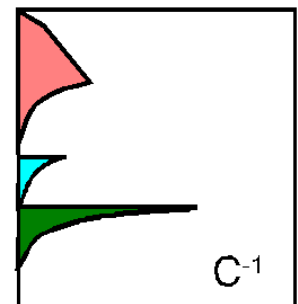
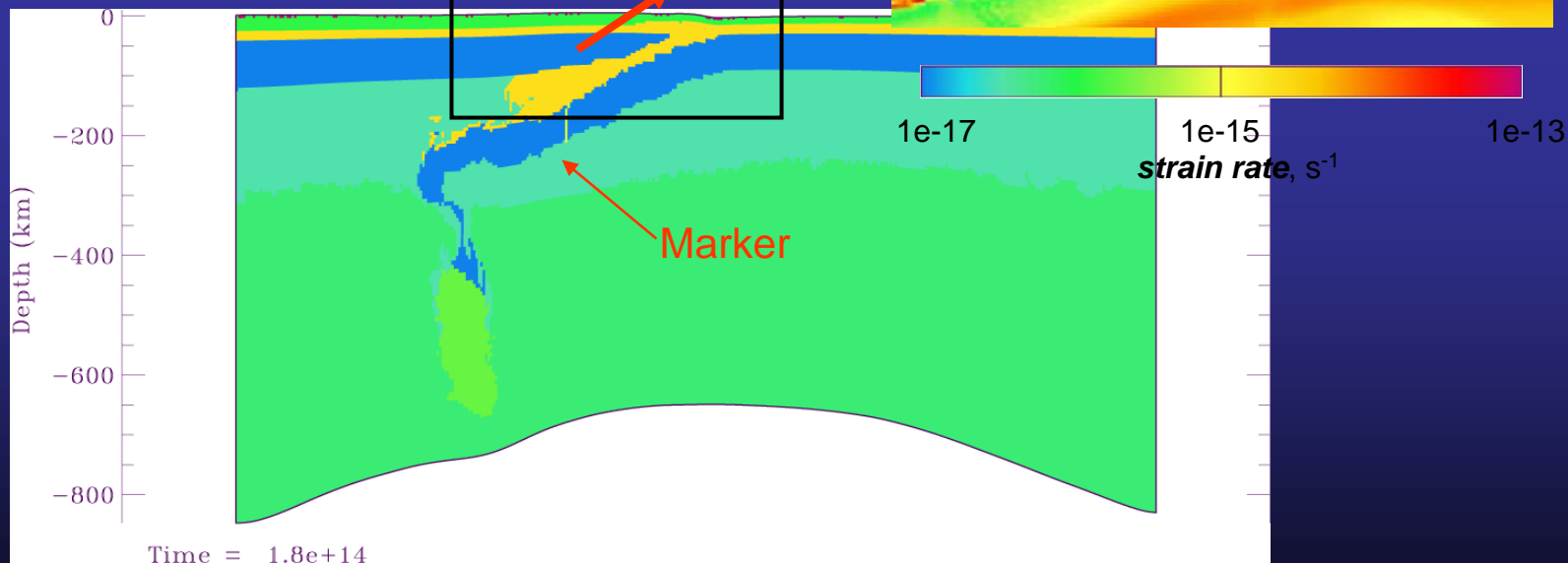
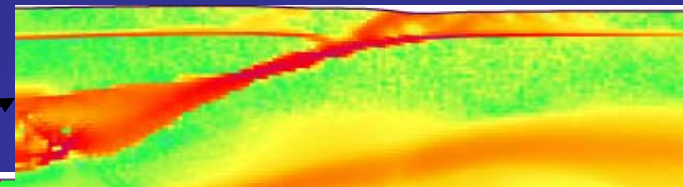
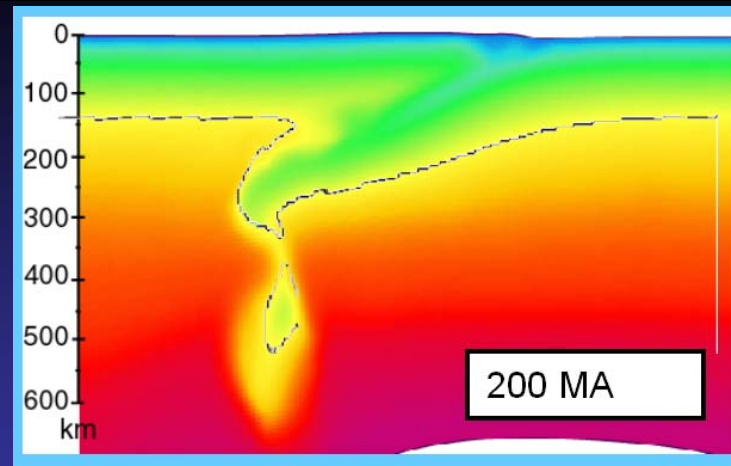
Thermal age of 90 MA, $T_m = 600^{\circ}\text{C}$, $dx = 330$ km, $t = 5,5$ Ma, 2×3 cm/yr

wait ...

Influence of thermo-rheological age - B1 JELLY SANDWICH RHEOLOGY

$S \sim 0.7$

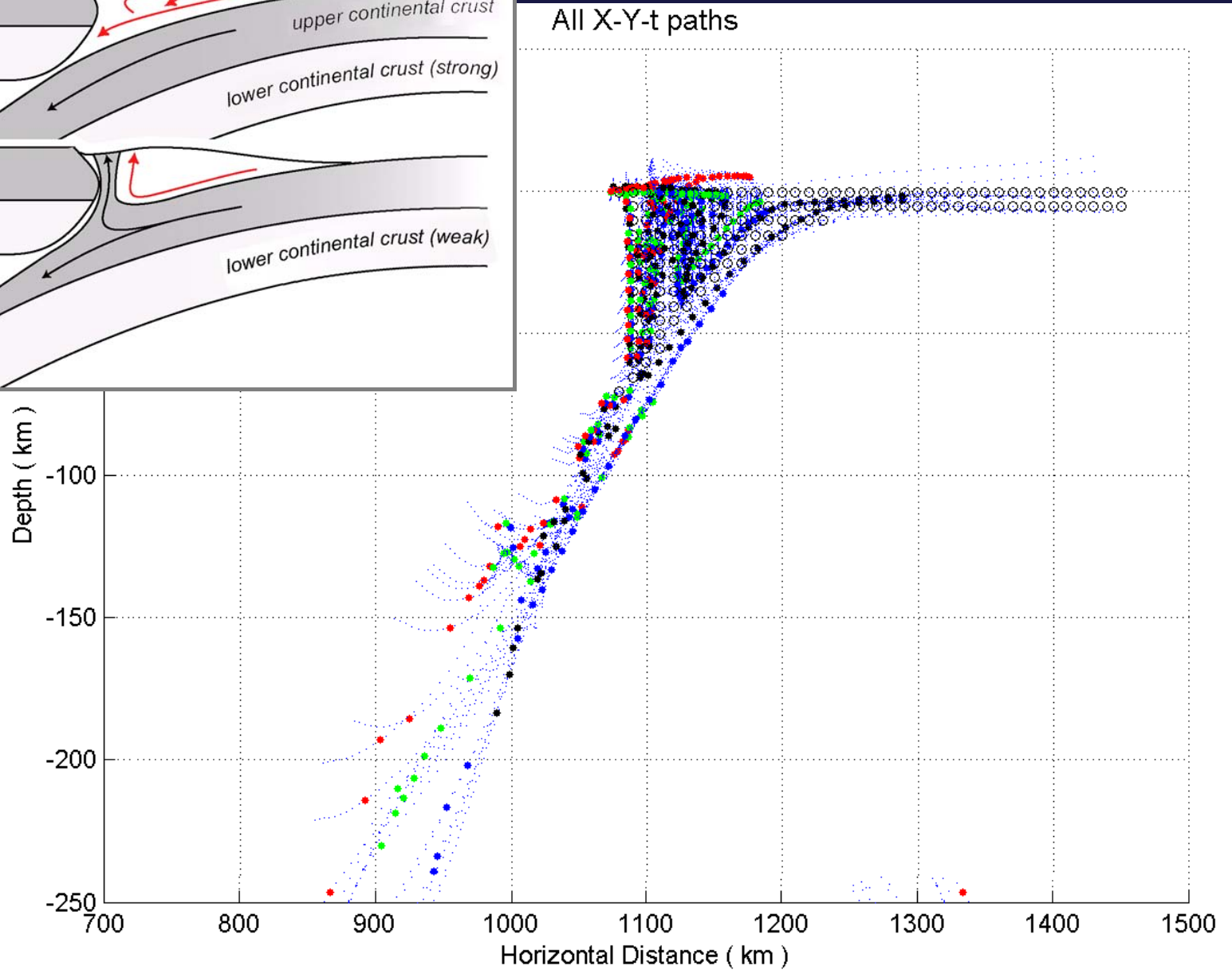
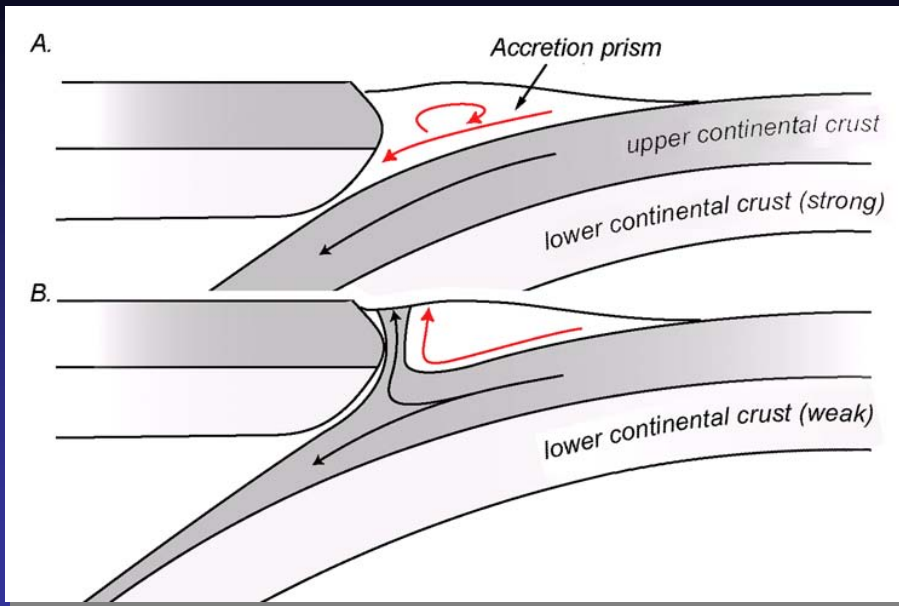
T°C

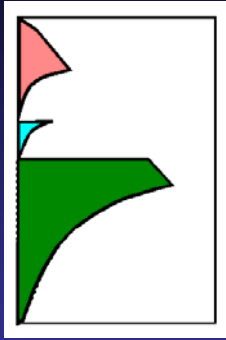


Thermal age of 200MA, $T_m = 500^\circ\text{C}$, $dx = 330 \text{ km}$, $t = 5,5 \text{ Ma}$, $2 \times 3 \text{ cm/yr}$

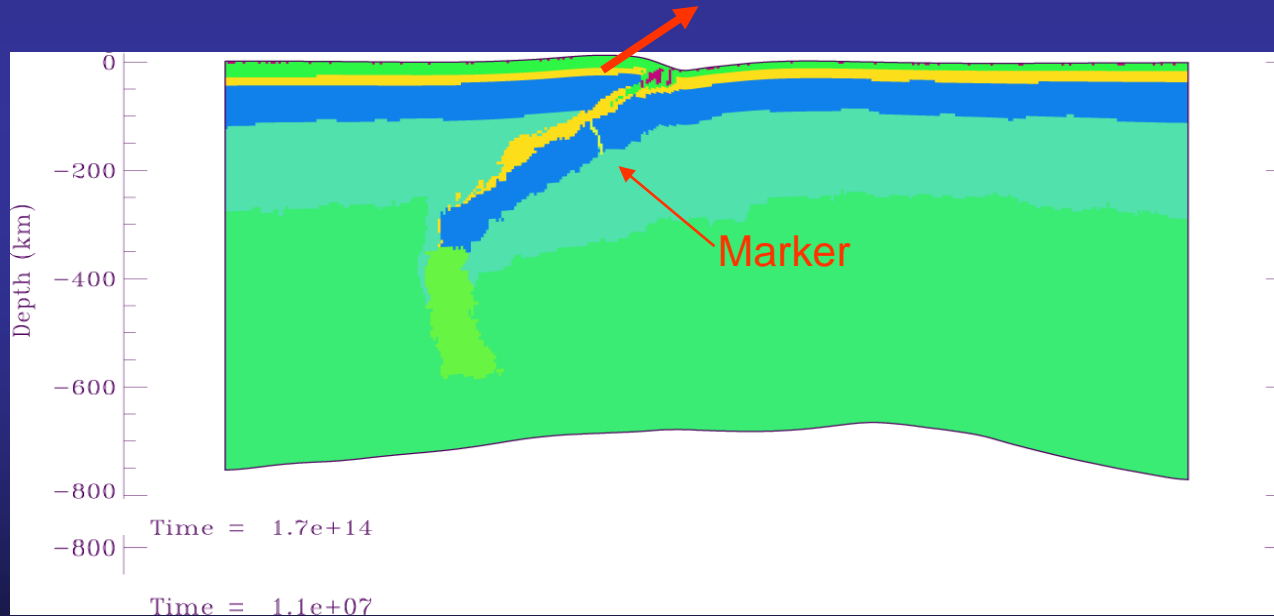
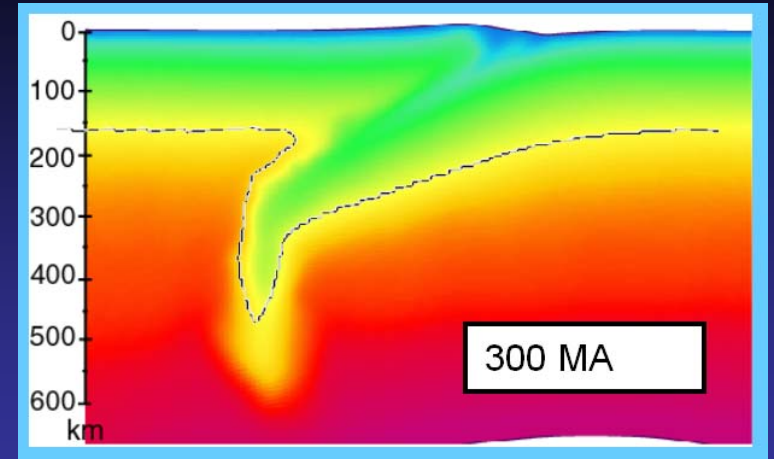
wait ...

P-T-t PATHS VIA PASSIVE MARKERS





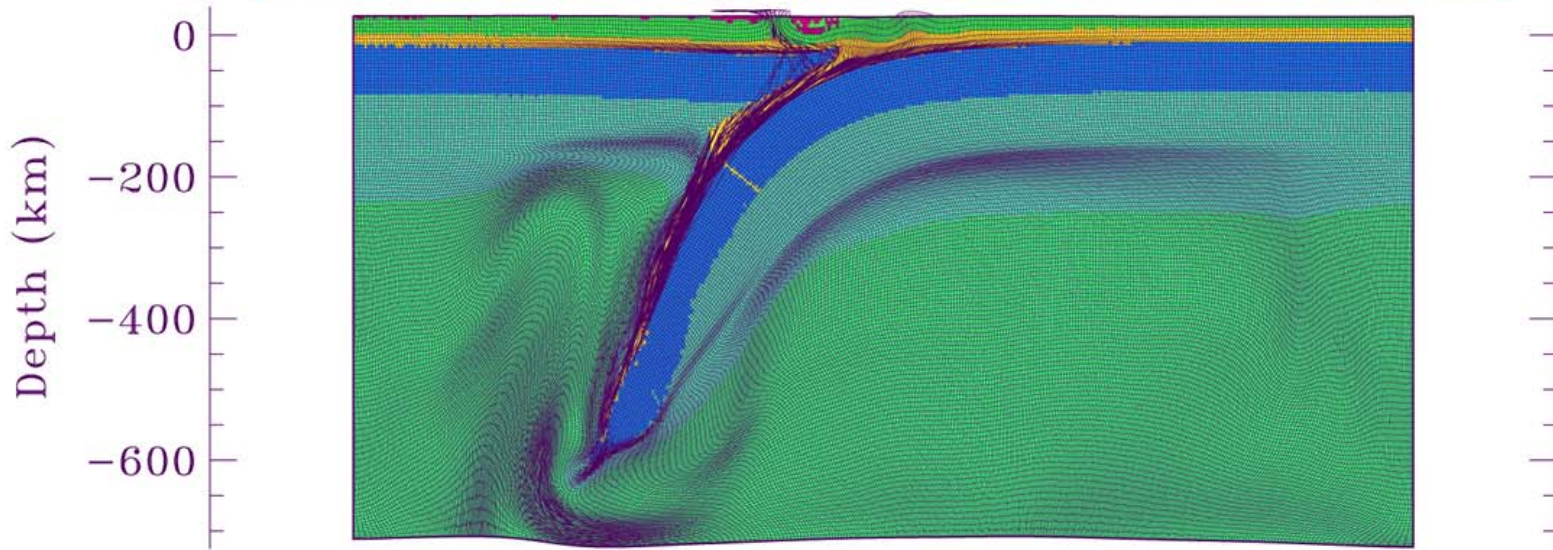
$S \sim 1.$



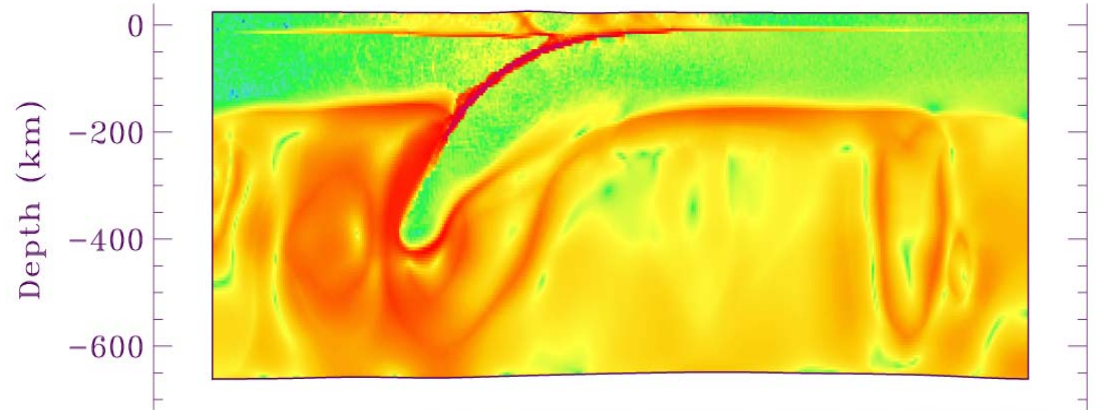
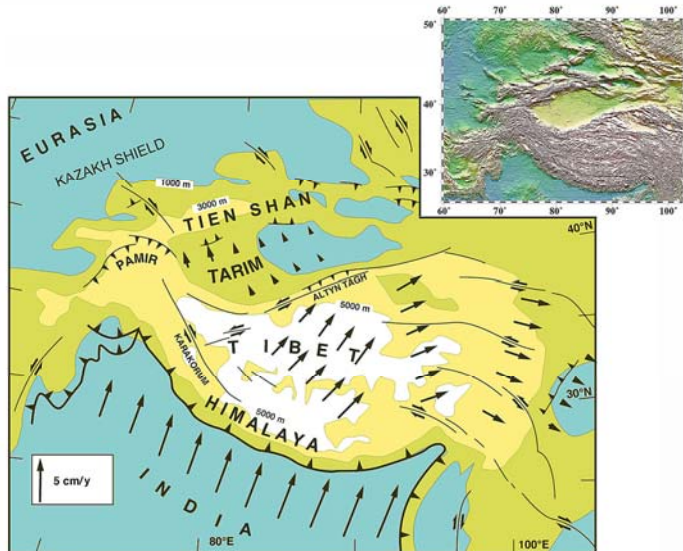
Thermal age of 300MA, $T_m = 450^\circ\text{C}$, $dx = 330 \text{ km}$, $t = 5,5 \text{ Ma}$, $2 \times 3 \text{ cm/yr}$

wait ...

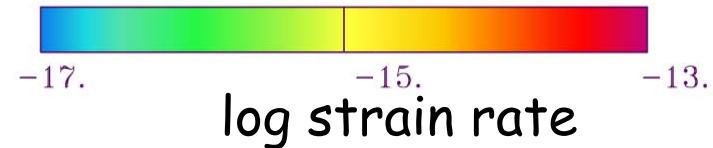
STRONG ($T_e > 60$ km) lithosphere, FAST collision (India-Asia > 5 cm/y)

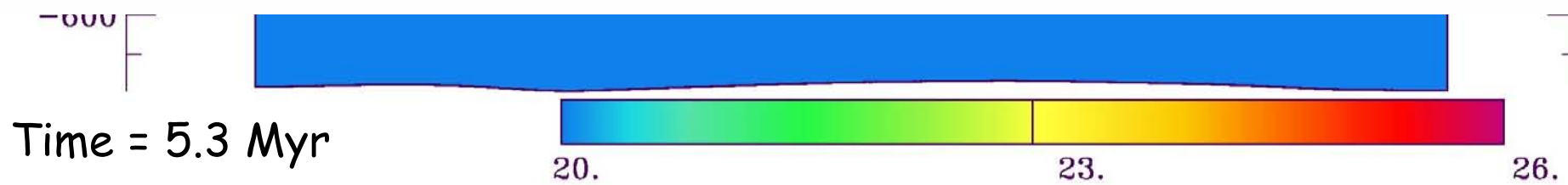
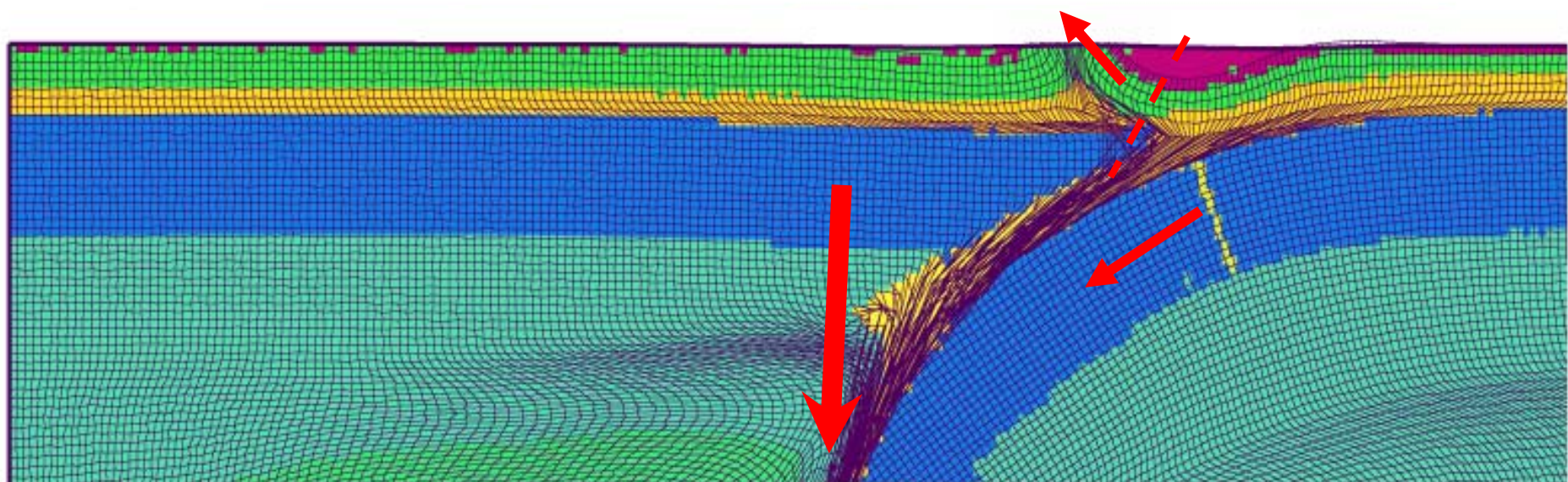
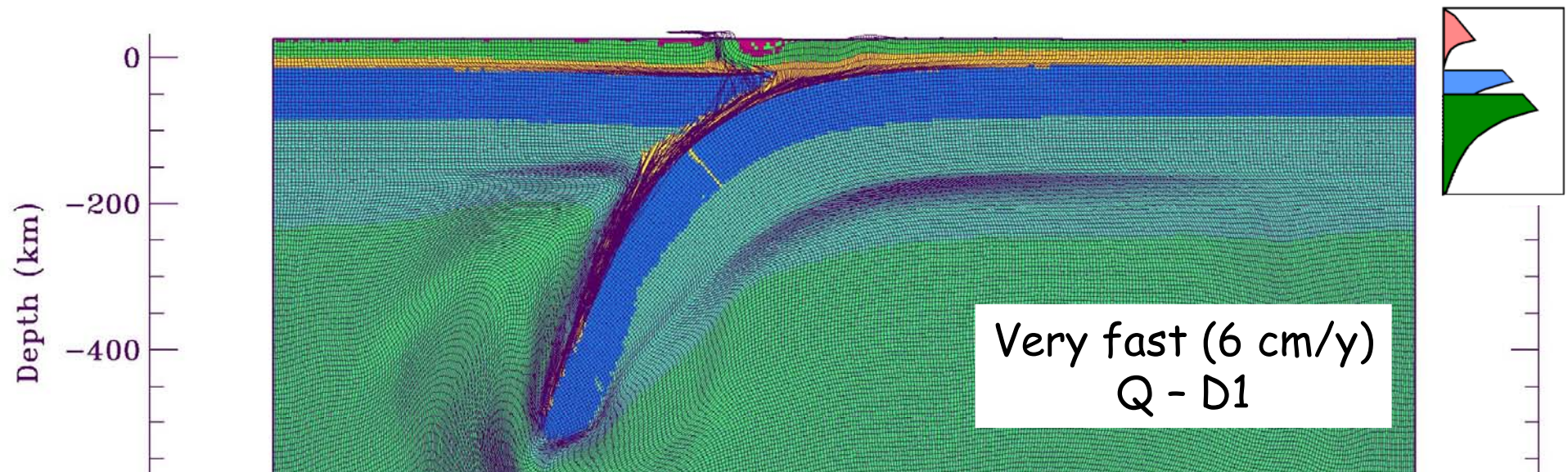


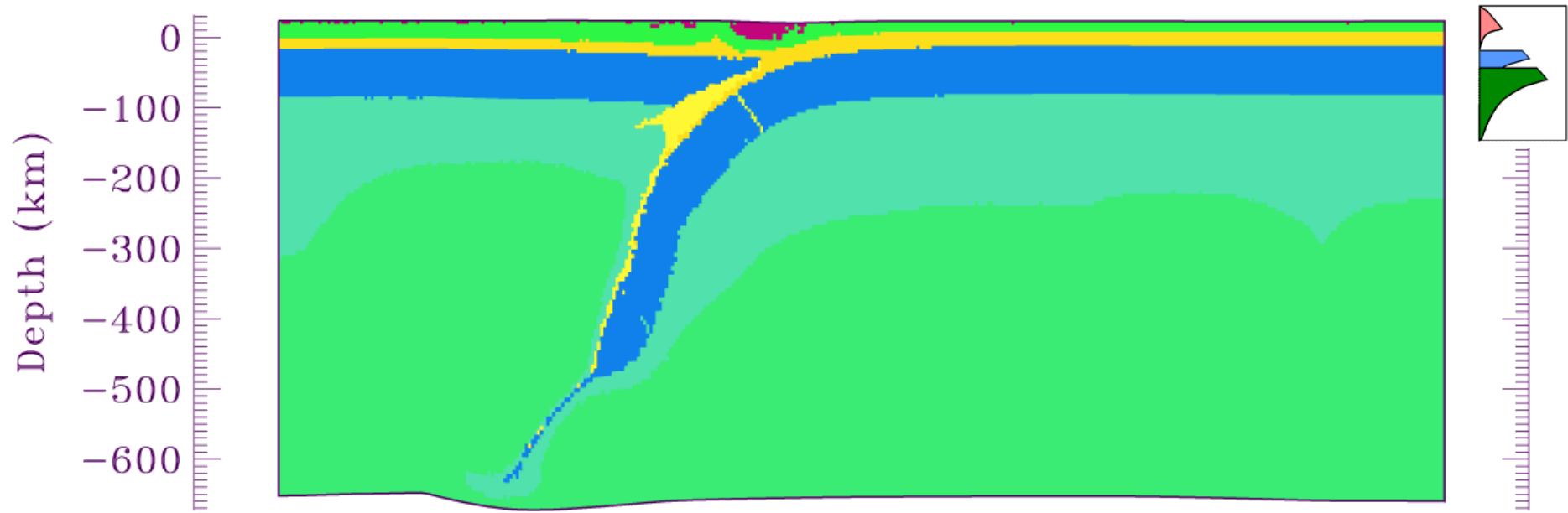
Time = 6.41398 Myr



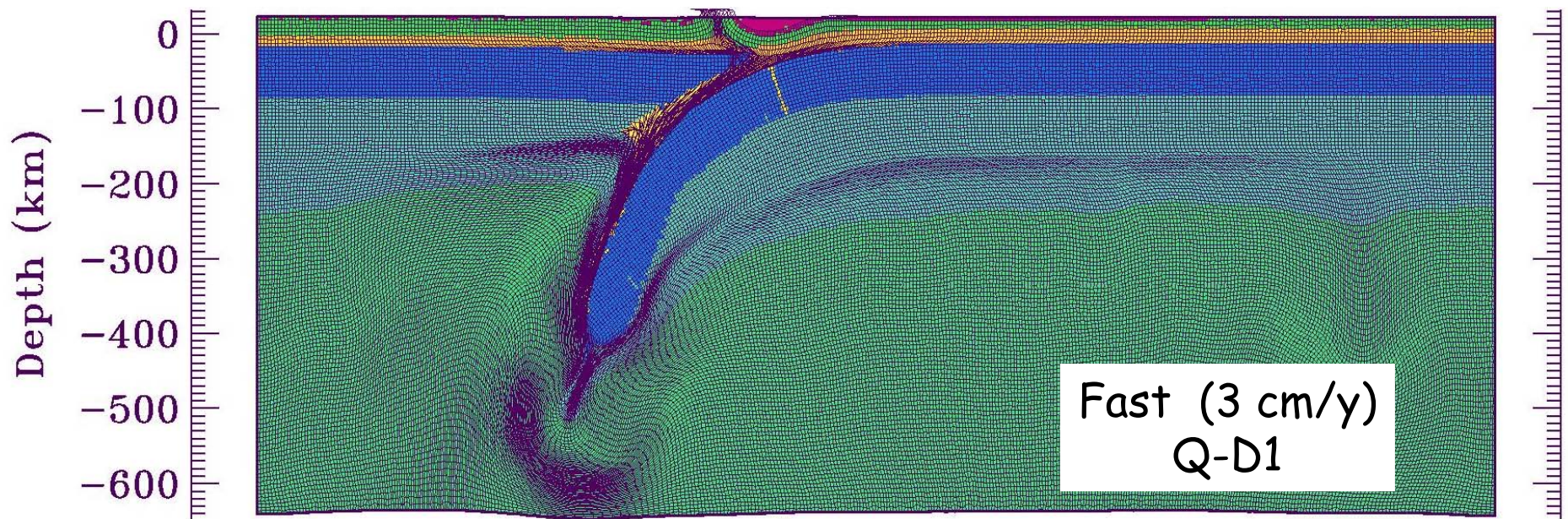
Time = 3.79319 Myr





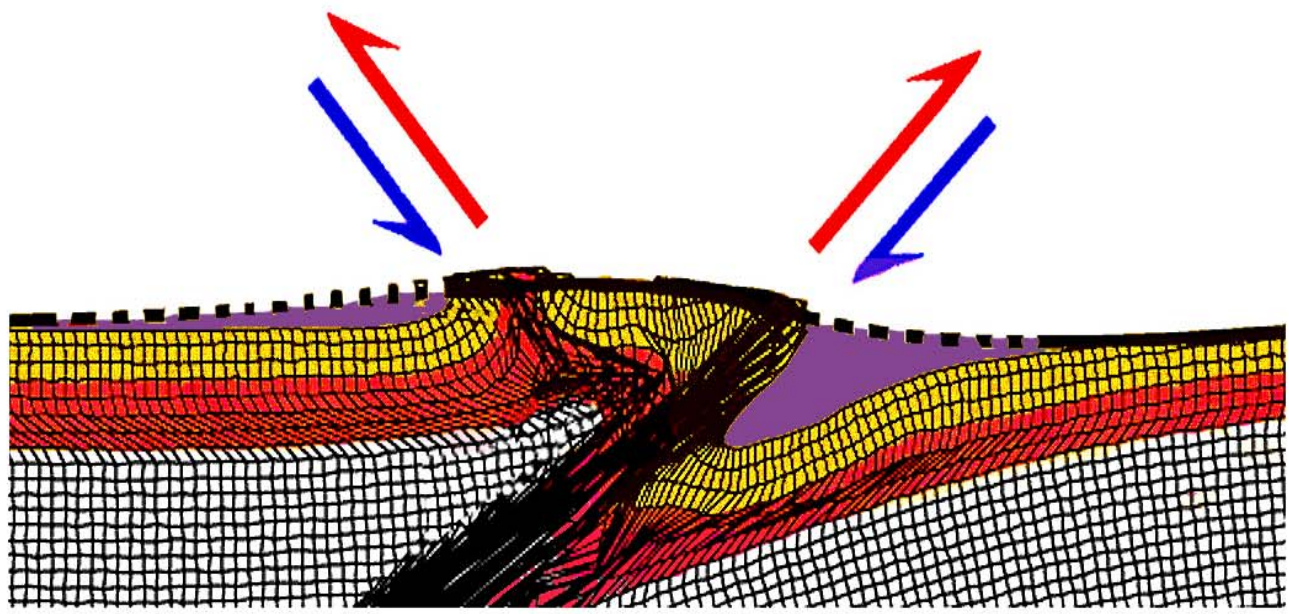
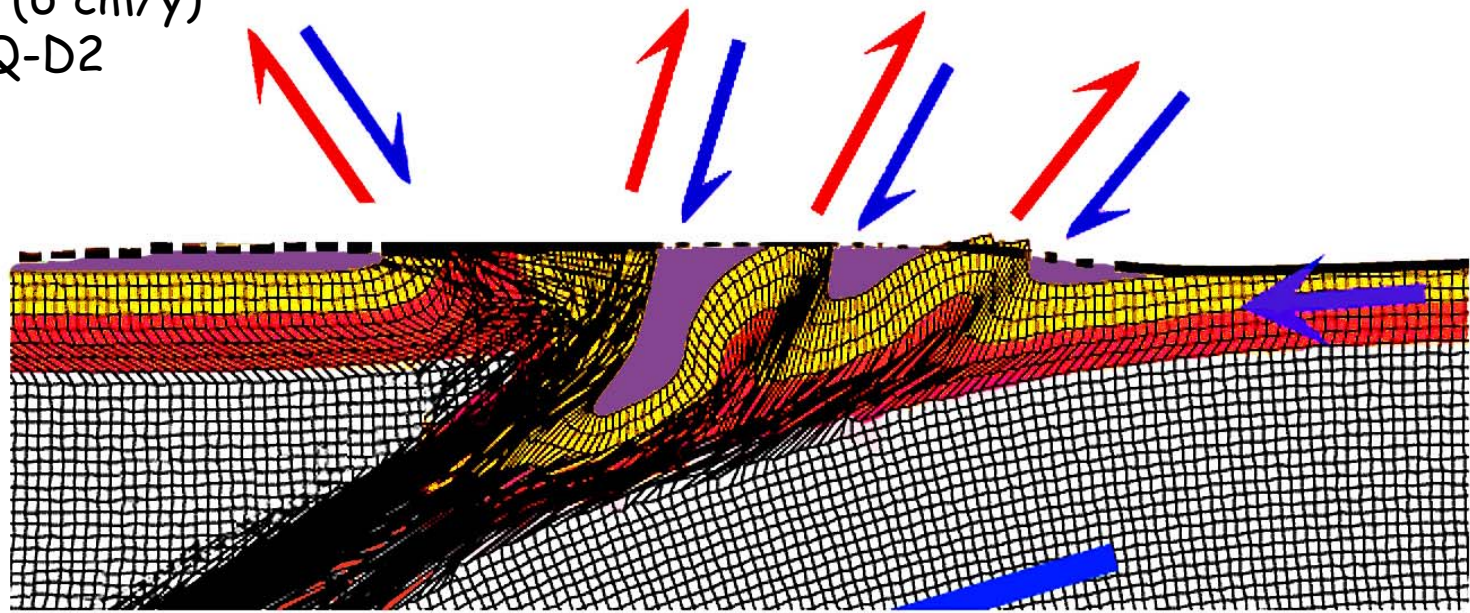
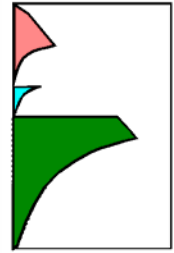


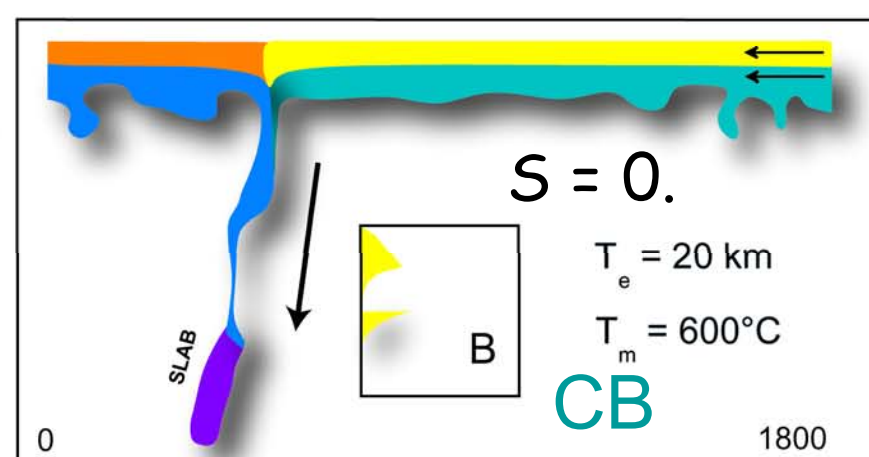
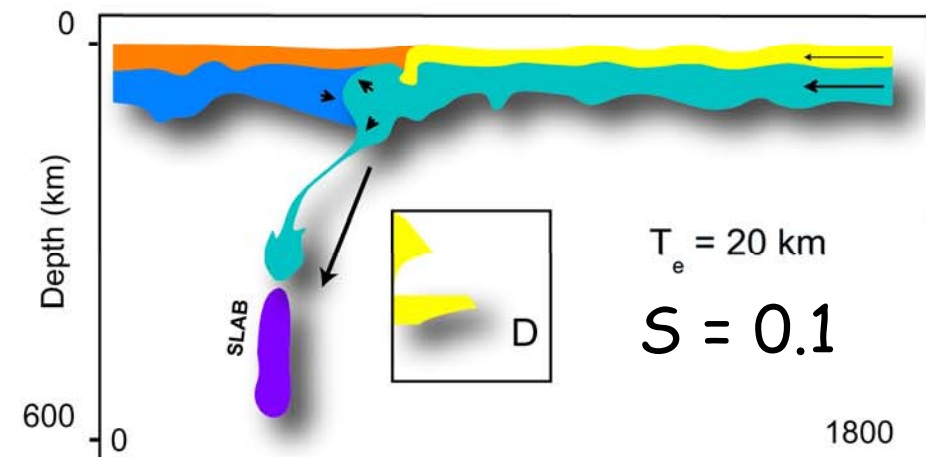
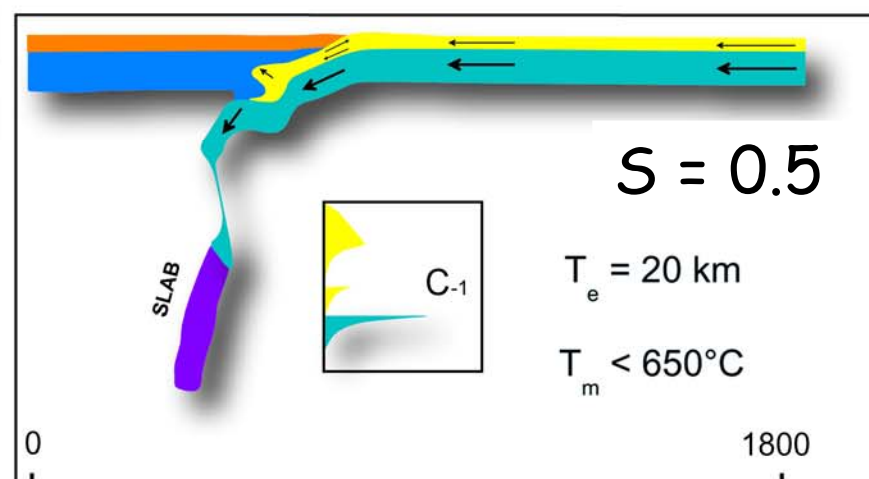
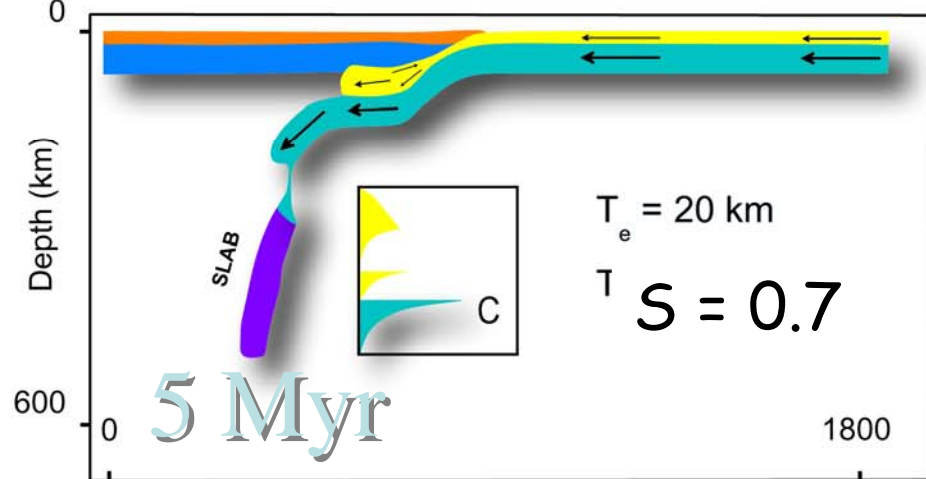
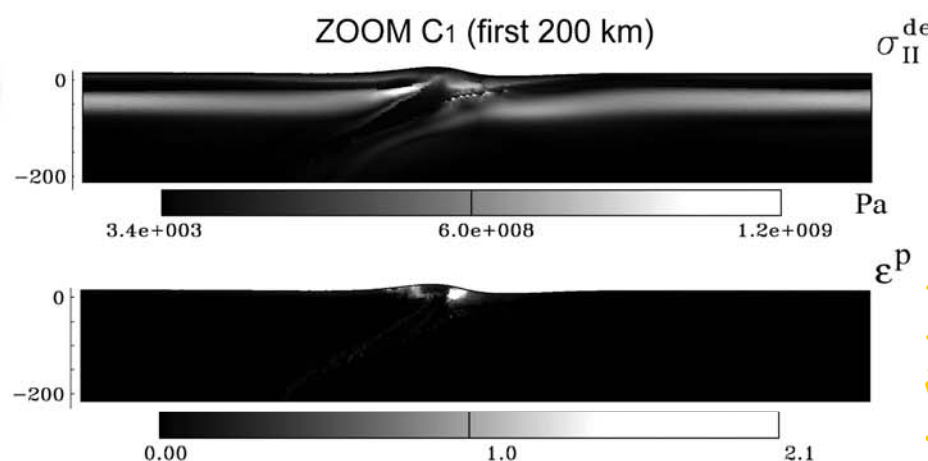
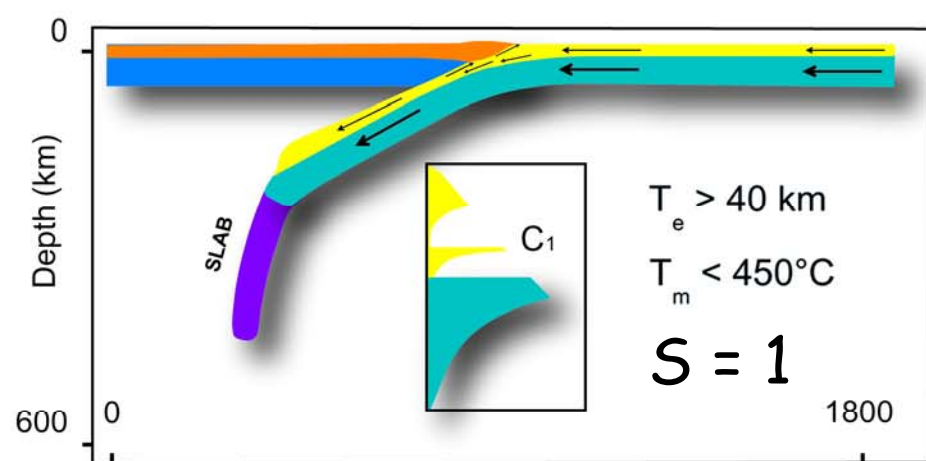
Time = 7.63 Myr



Time = 5.8 Myr

Fast (6 cm/y)
Q-D2

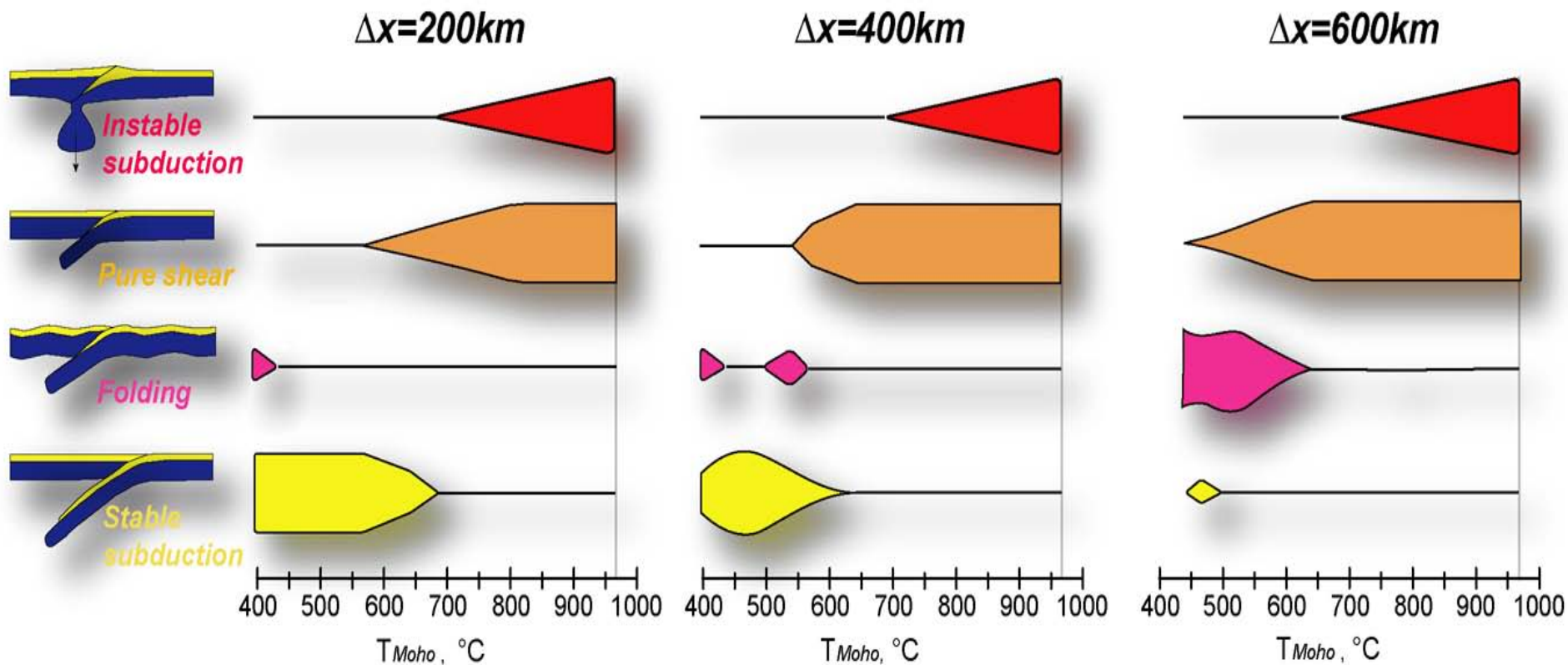




Dependence on rheology: summary

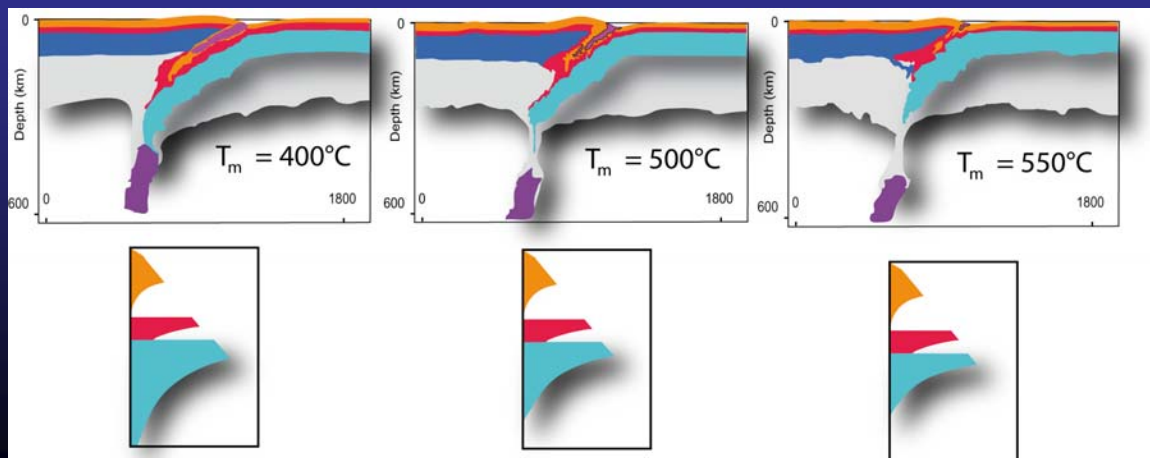
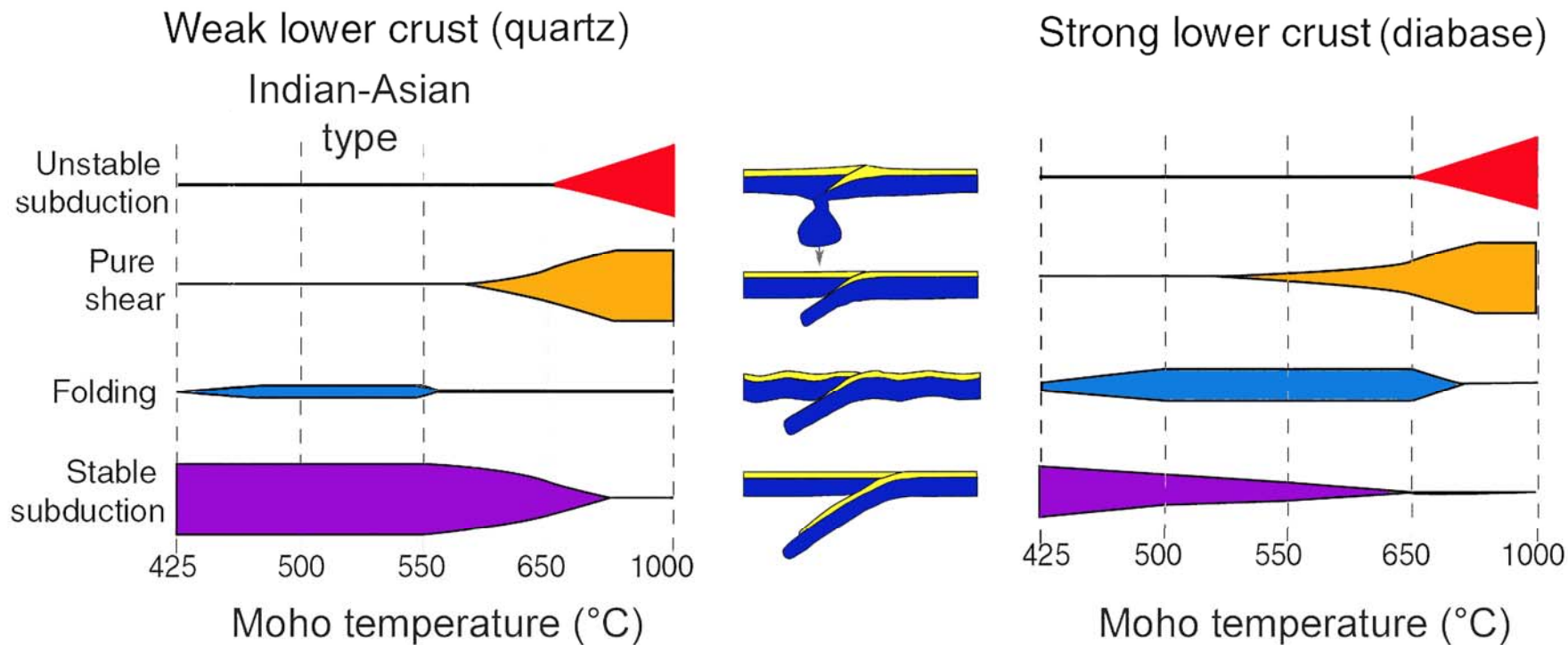
COTRIBUTION TO THE COLLISION STYLE FROM DIFFERENT DEFORMATION MODES

amount of shortening Δx



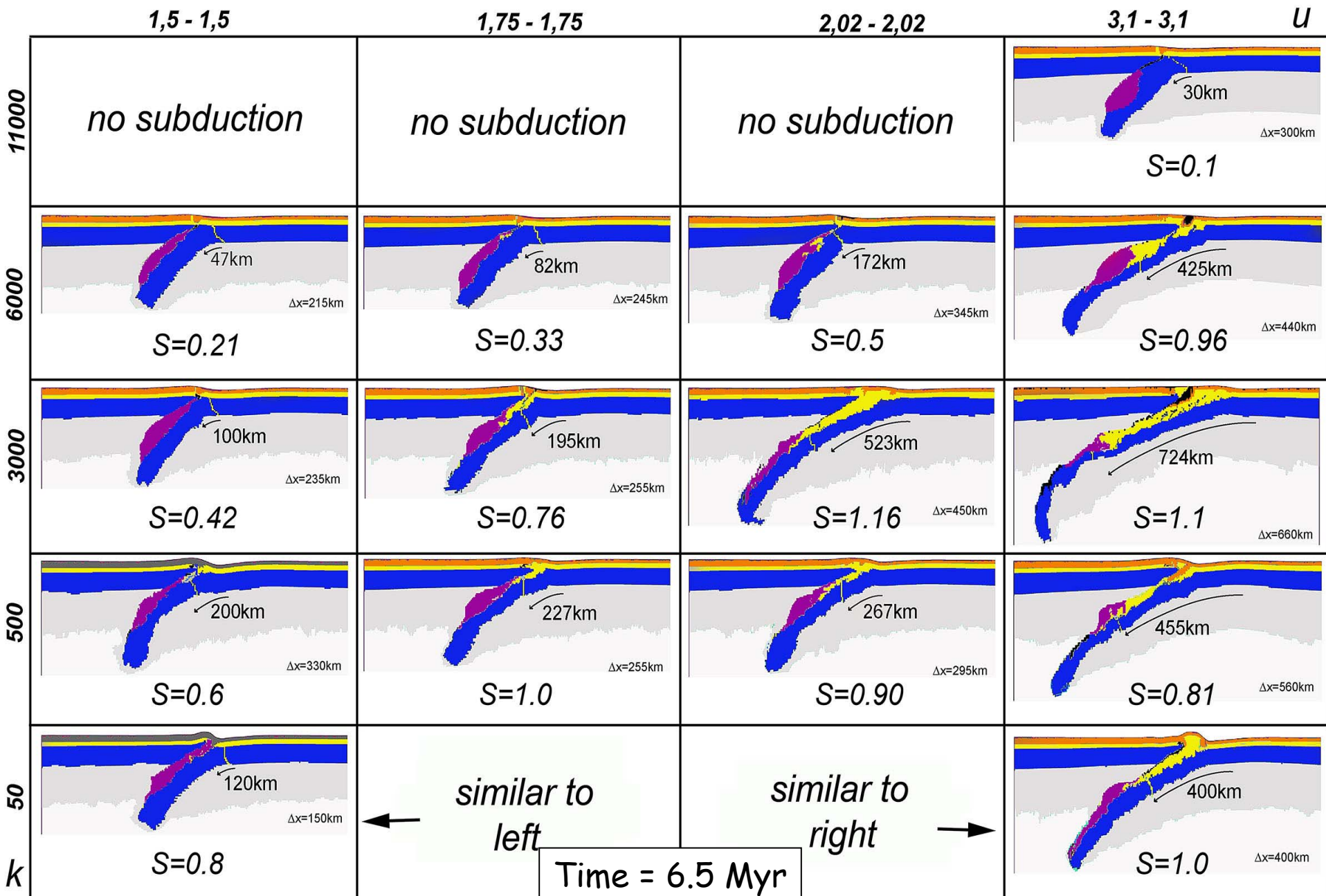
Moho temperature = Thermotectonic Age = thermo-rheological profile

Strong (diabase) lower crust promotes folding



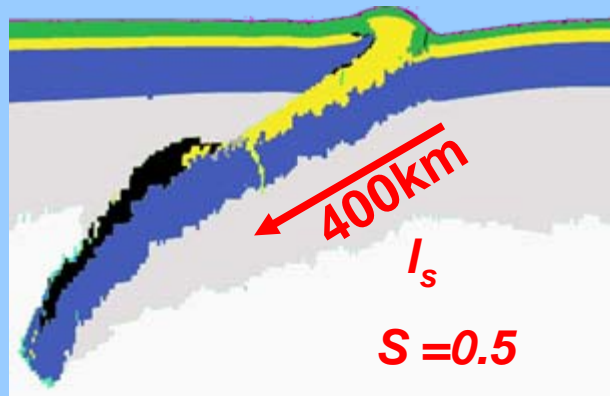
3. Influence of coupling with surface processes

Final stages of subduction-collision, as function of convergence and erosion rate

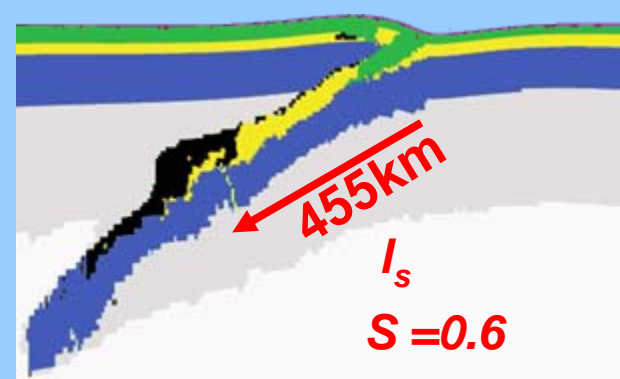


Dependence on efficiency of surface erosion rate (k)

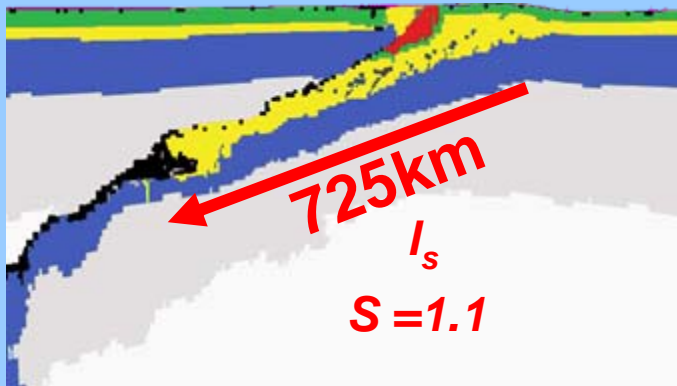
$dh/dt=0$ mm/yr ($k=0$)



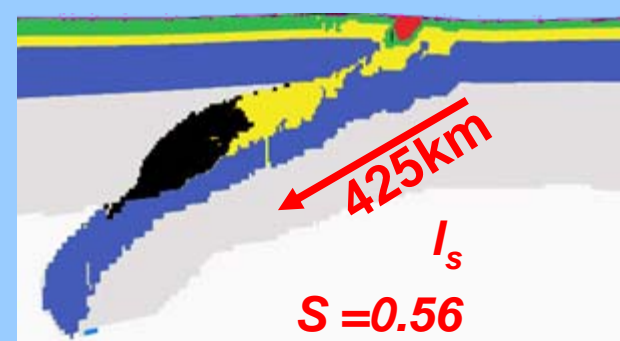
$dh/dt=6$ mm/yr ($k=500$)



$dh/dt=12\text{mm/yr}$ ($k=3000$)



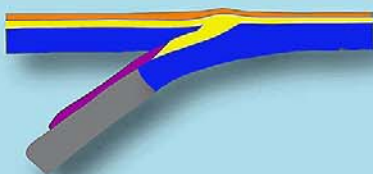
$dh/dt=20\text{mm/yr}$ ($k=6000$)



Maximal erosion rate and subduction length as function of k , convergence rate 60 mm/yr

**1. First 0 to 5 Myr:
similar initial development**

continental subduction and
formation a small accretion
prism mainly of lower crustal
material

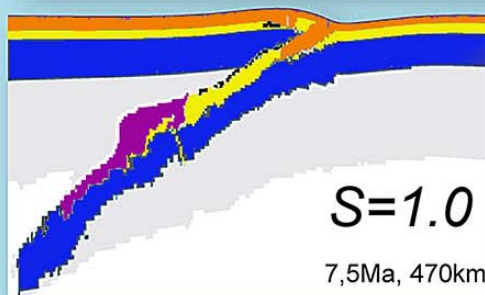
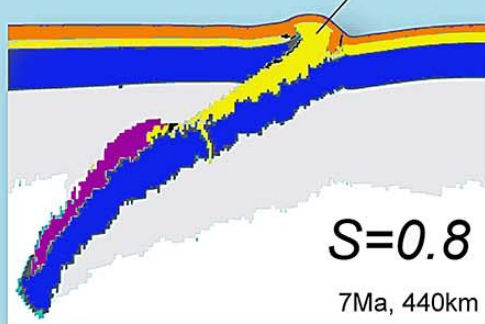


$k=50$

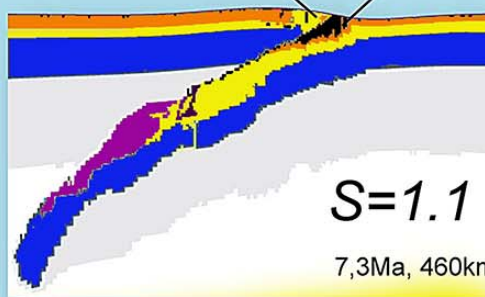
$k=500$

$k=3000$

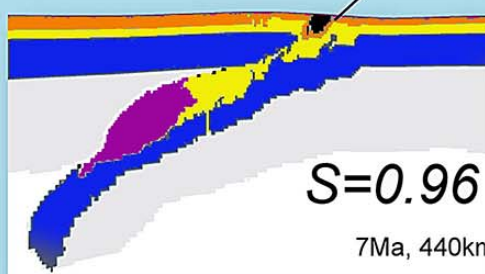
$k=6000$



exhumation l. crust sediments



sediments

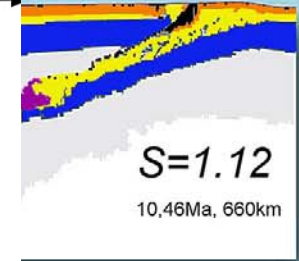


**3. After 8 Myr,
evolution scenarios
come different**

evolution ends up before
; as whole-scale
evolution with excessively
unrealistic topography
develops

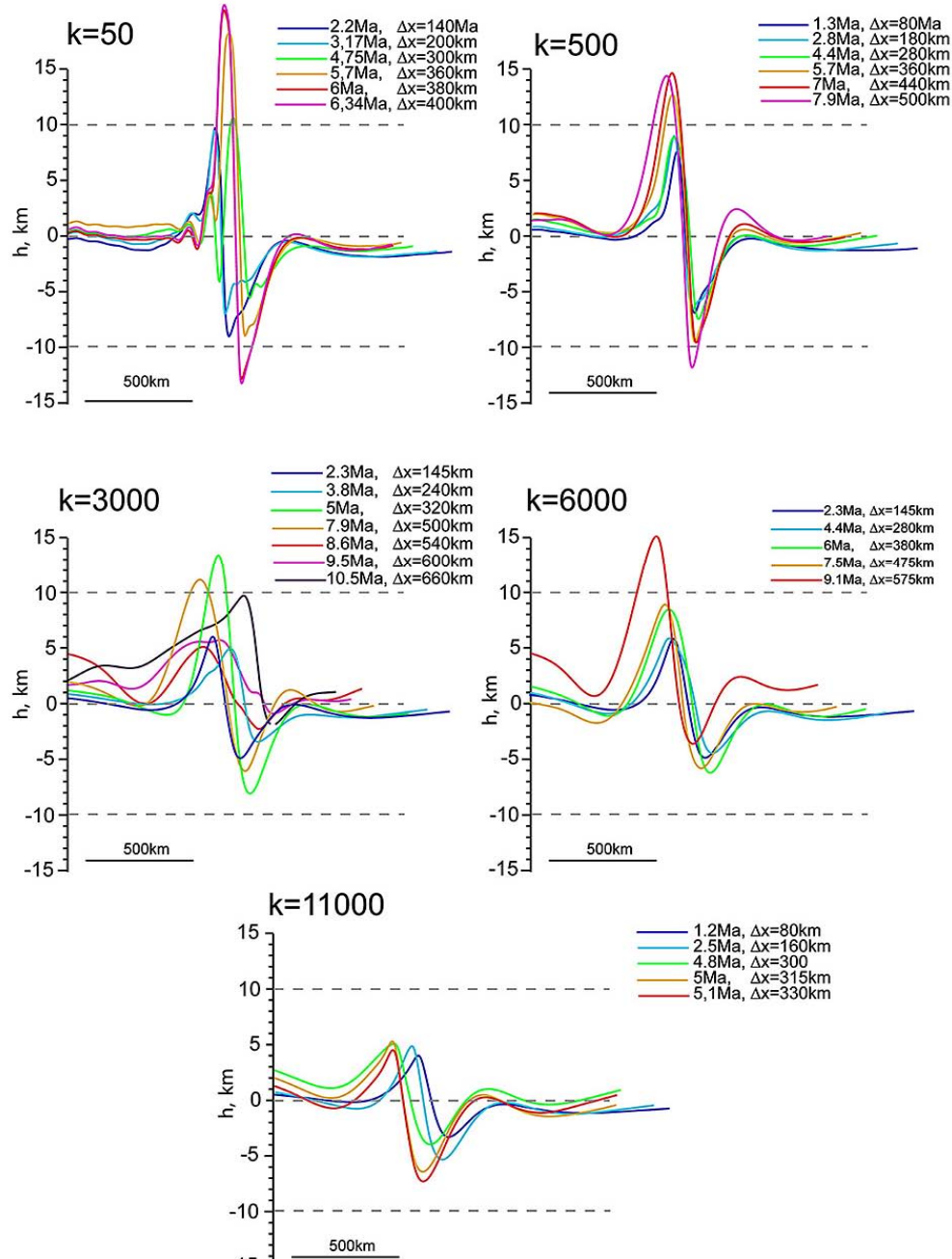
topography becomes
high due to buckling and
it must be compensated by
erosion

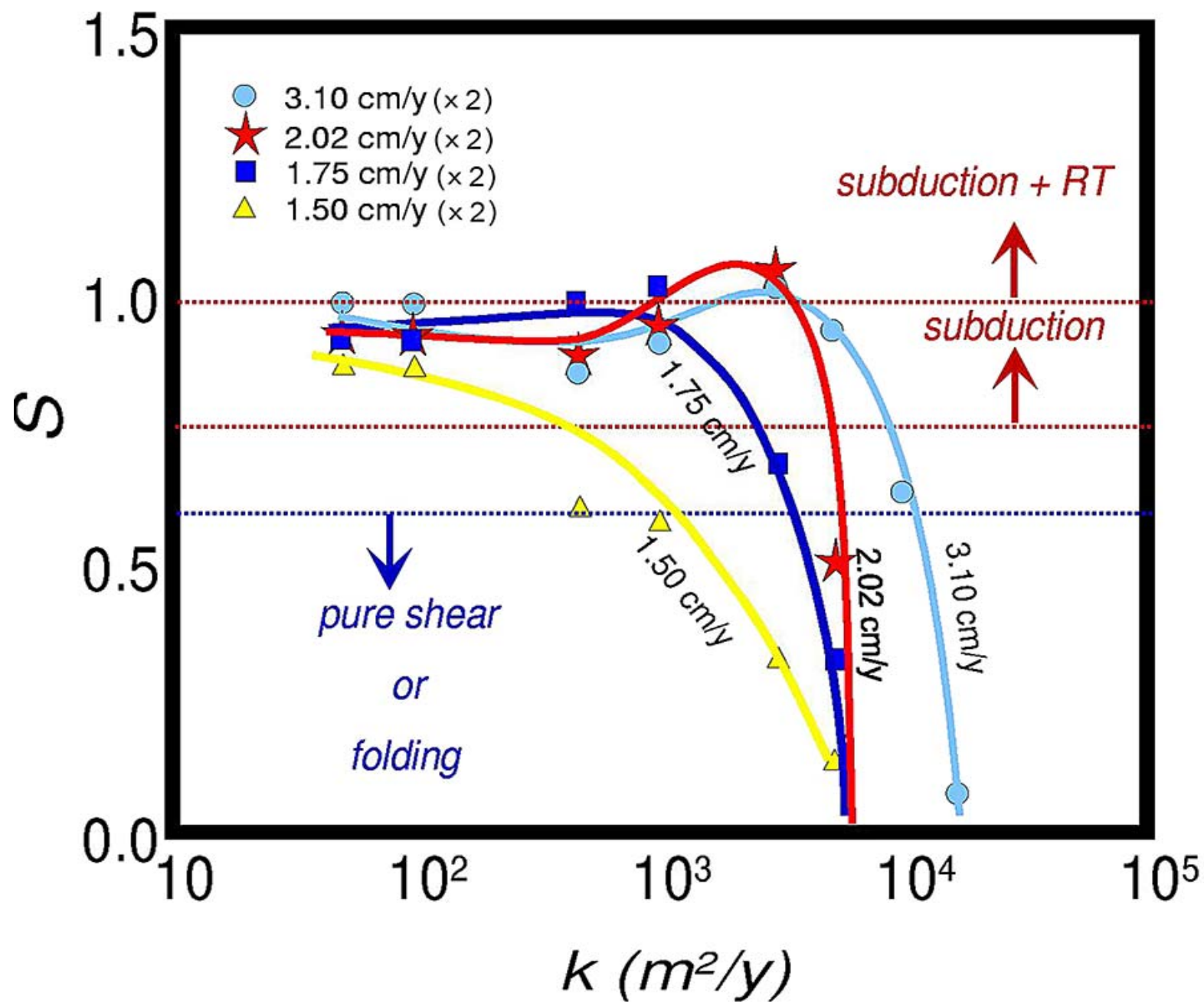
Evolution still goes on



100 km of subduction,
coupling occurs and
system enters into pure
collision mode with
topography

Topography evolution



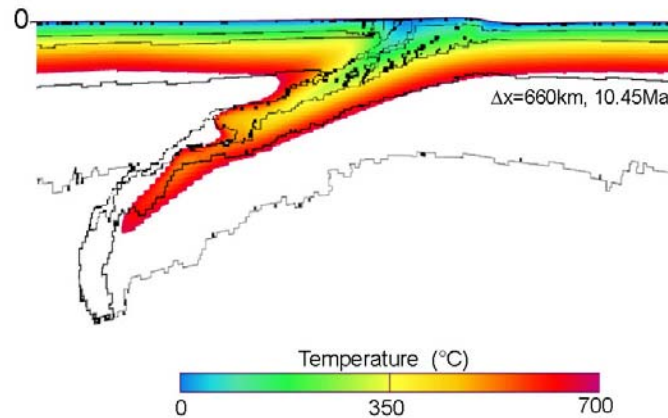
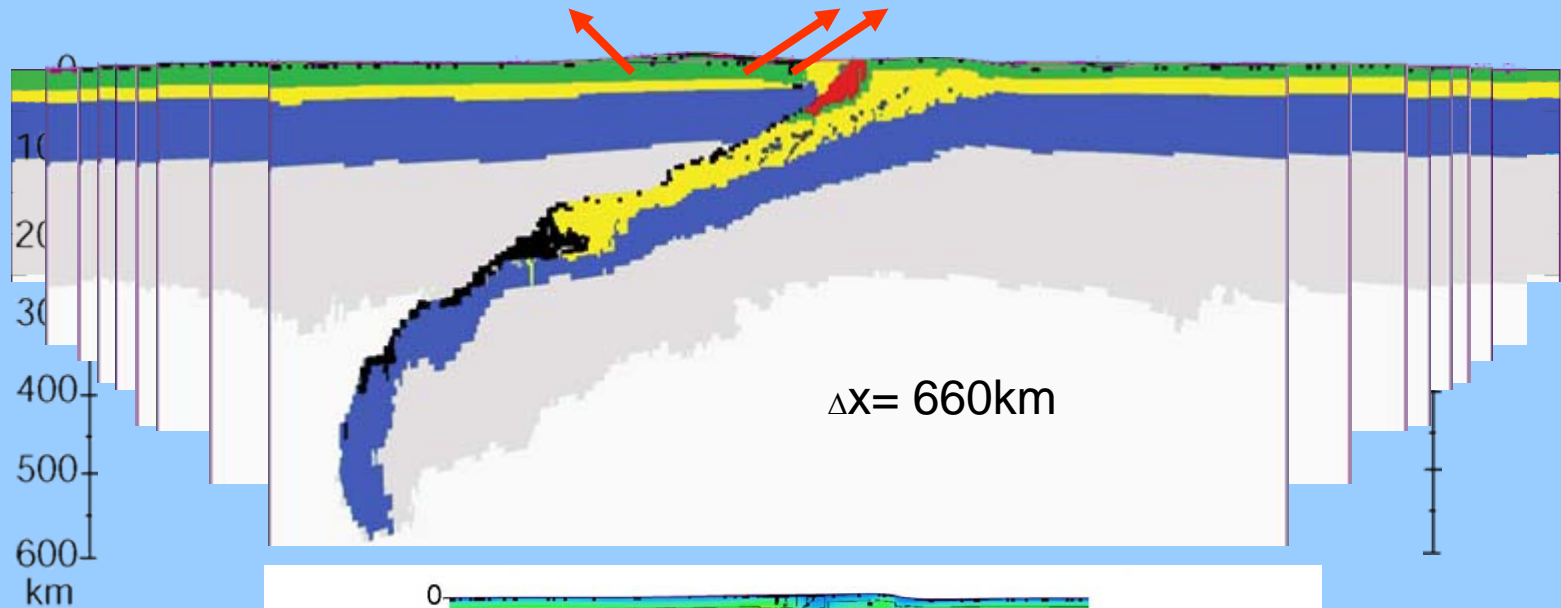


A simulation compatible with Indian -Asian collision

Geotherm 450 Ma
($T_{\text{Moho}} = 400^{\circ}\text{C}$)

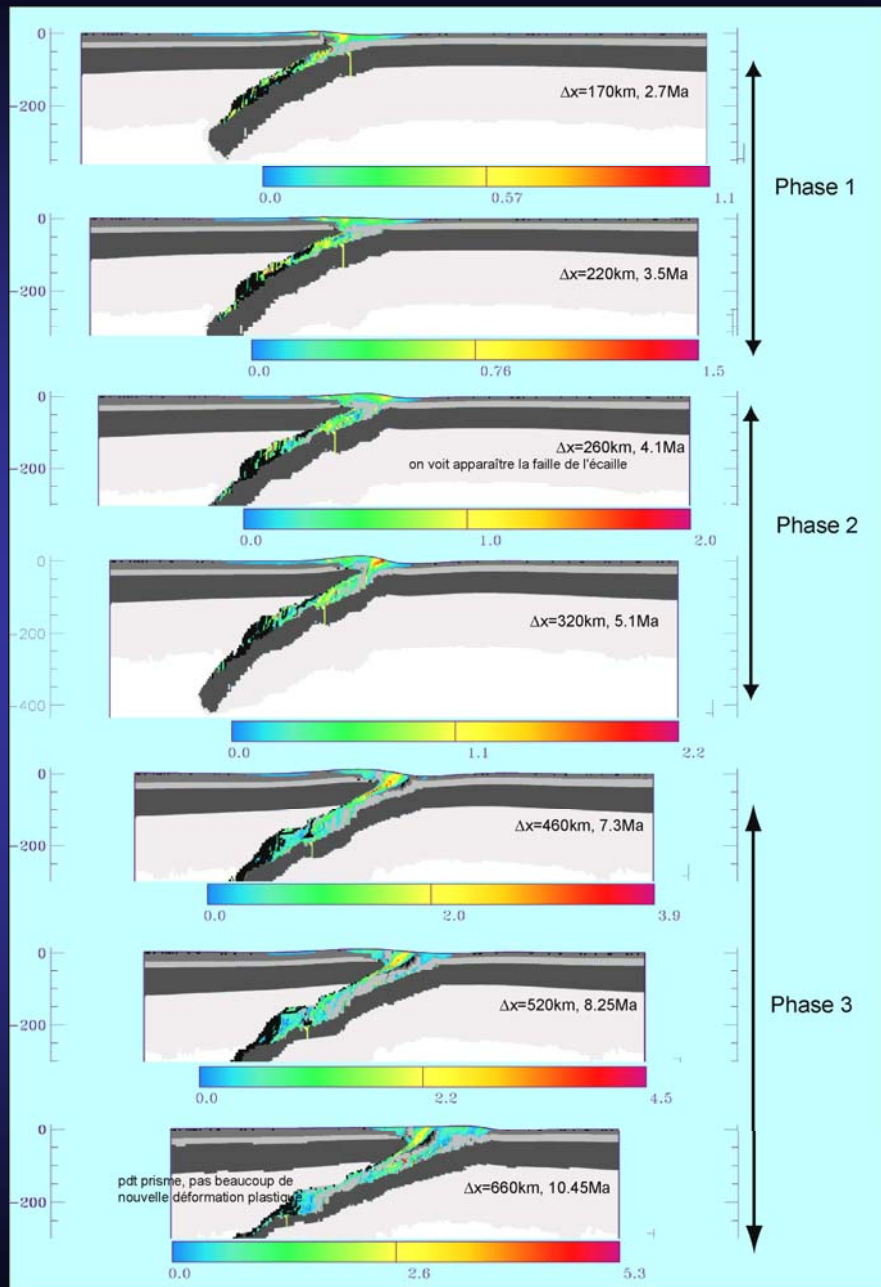
High initial
convergence rate
(6cm/y)

About 700km of
subduction

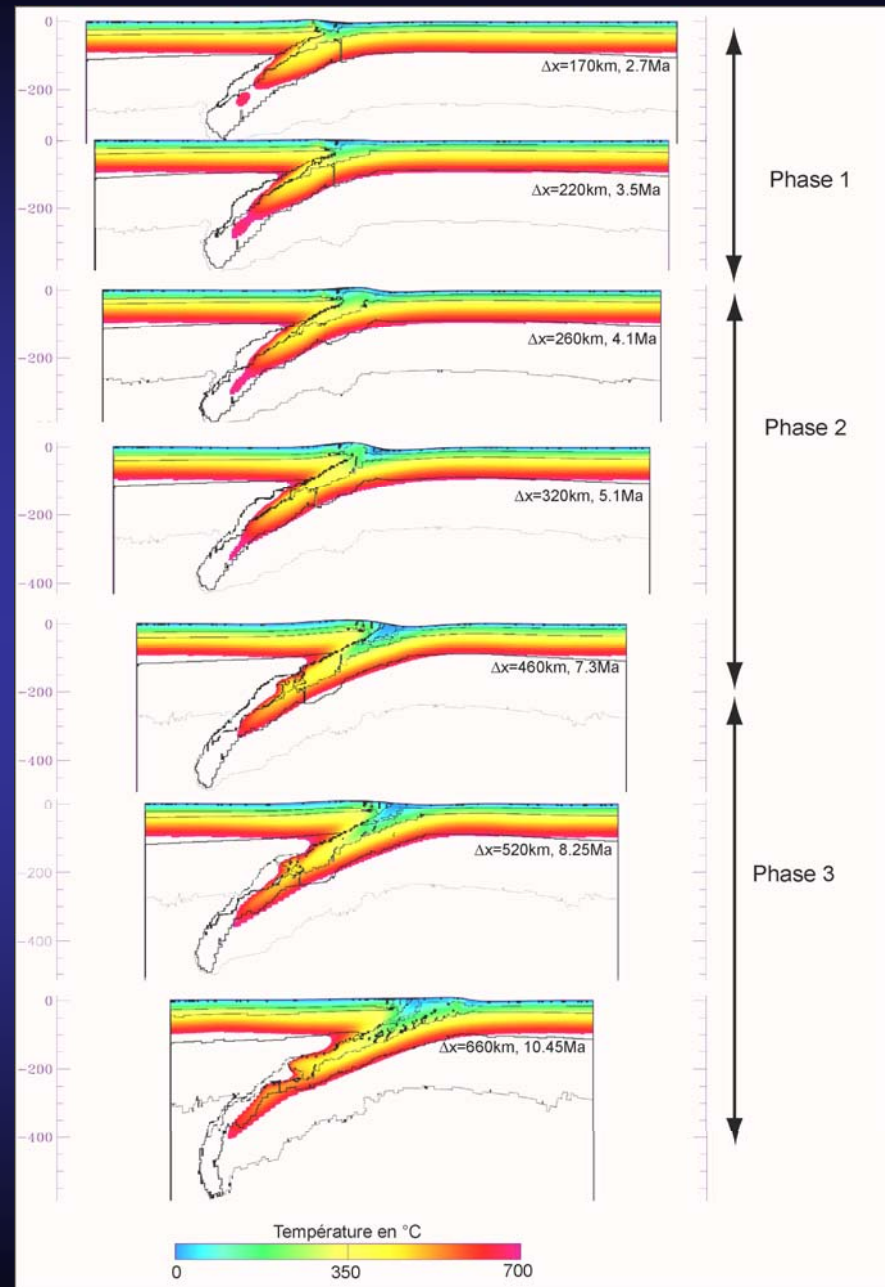


wait ...

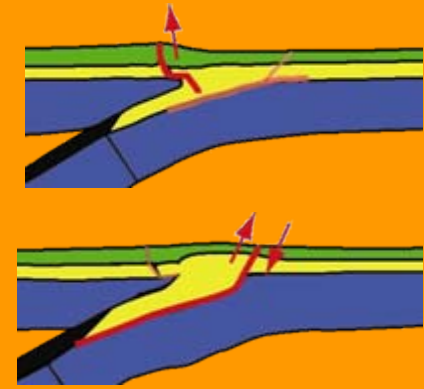
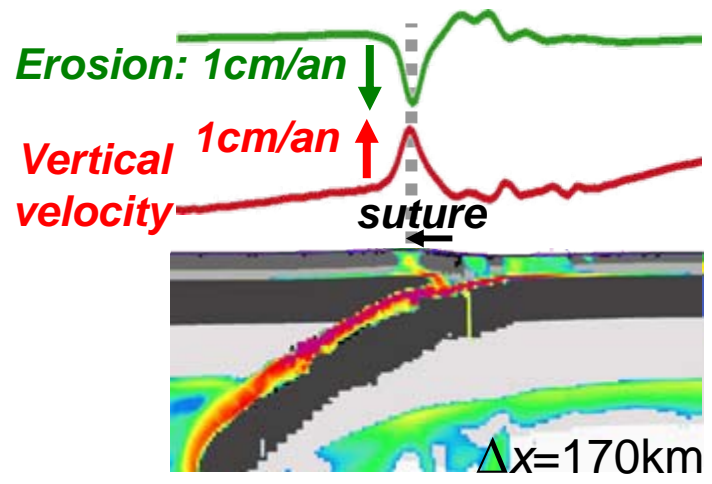
Plastic strain



Temperature

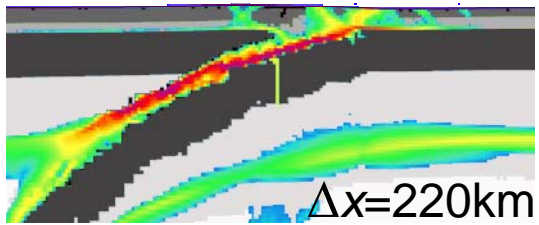
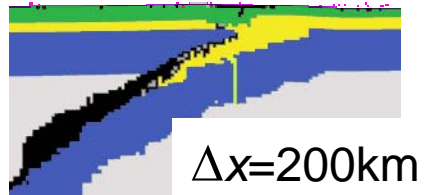


Phase 1 (dx= 0-220km): deformation at suture

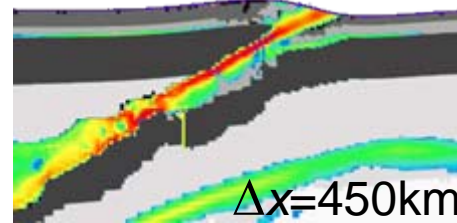
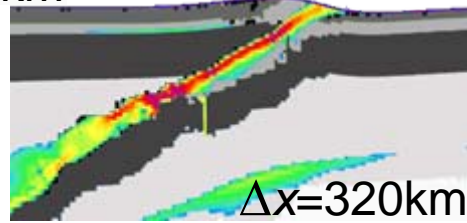
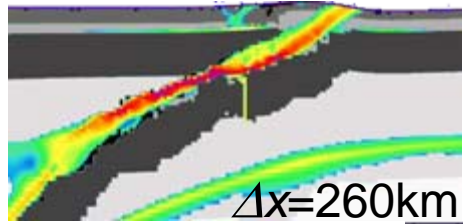


Lower crustal prism

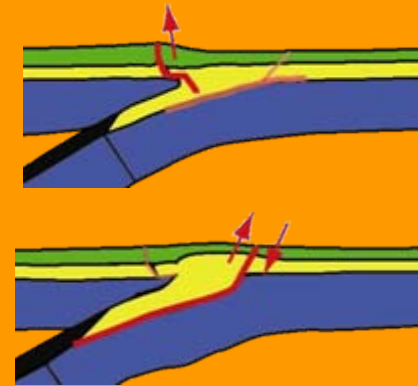
Transitory regime...



Phase 2: Majour thrust fault activity



All deformation is concentrated on a single thrust during 250km of shortening



erosion



vertical vel.



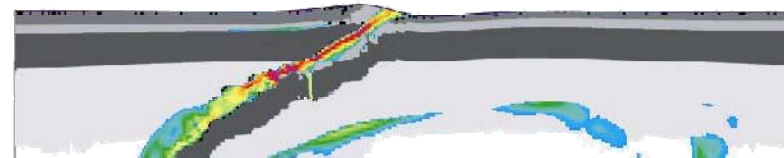
horizontal vel.



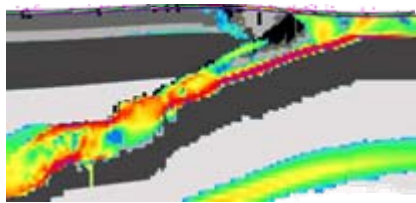
topography



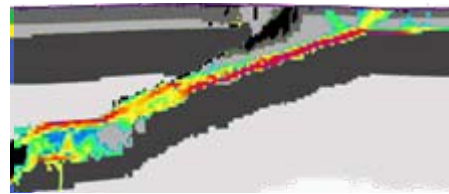
It controls all surface deformation



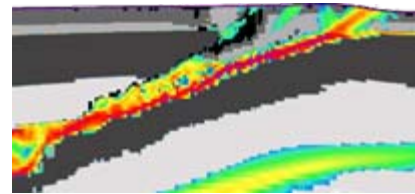
Phase 3: accretion of a large crustal prism



$\Delta x = 520 \text{ km}$



$\Delta x = 600 \text{ km}$



$\Delta x = 660 \text{ km}$

Successions of frontal thrusts towards South

→ **Formation of an asymmetric chain above the prism**

erosion

vertical vel.

horizontal velocity
+3cm/y

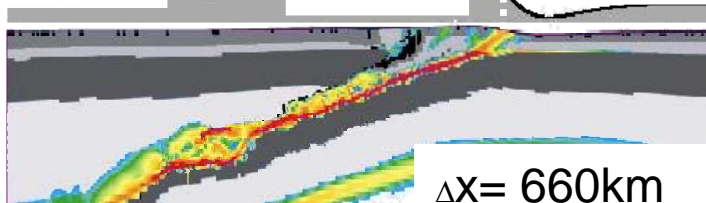
topography

1cm/an

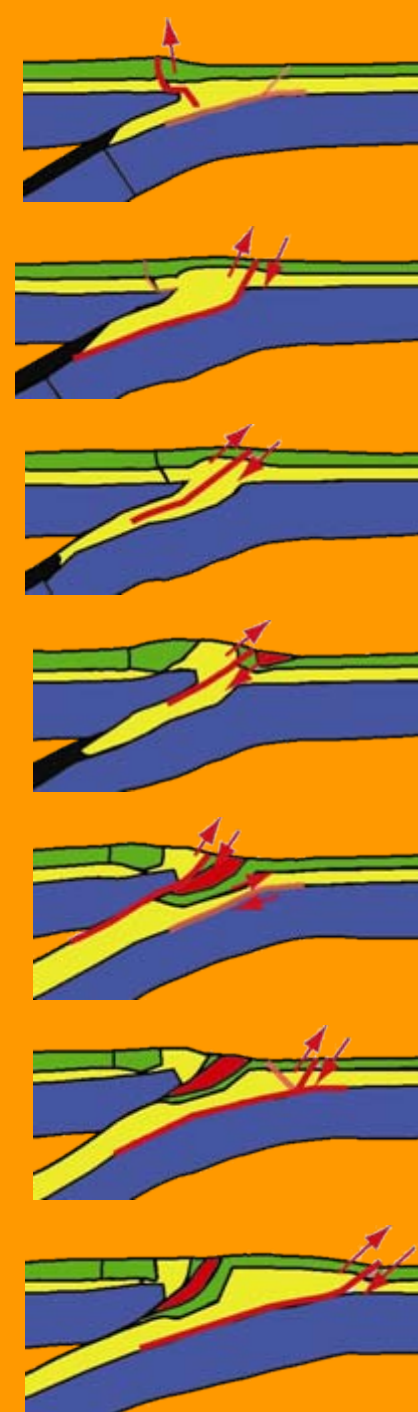
1 cm/an

8 km

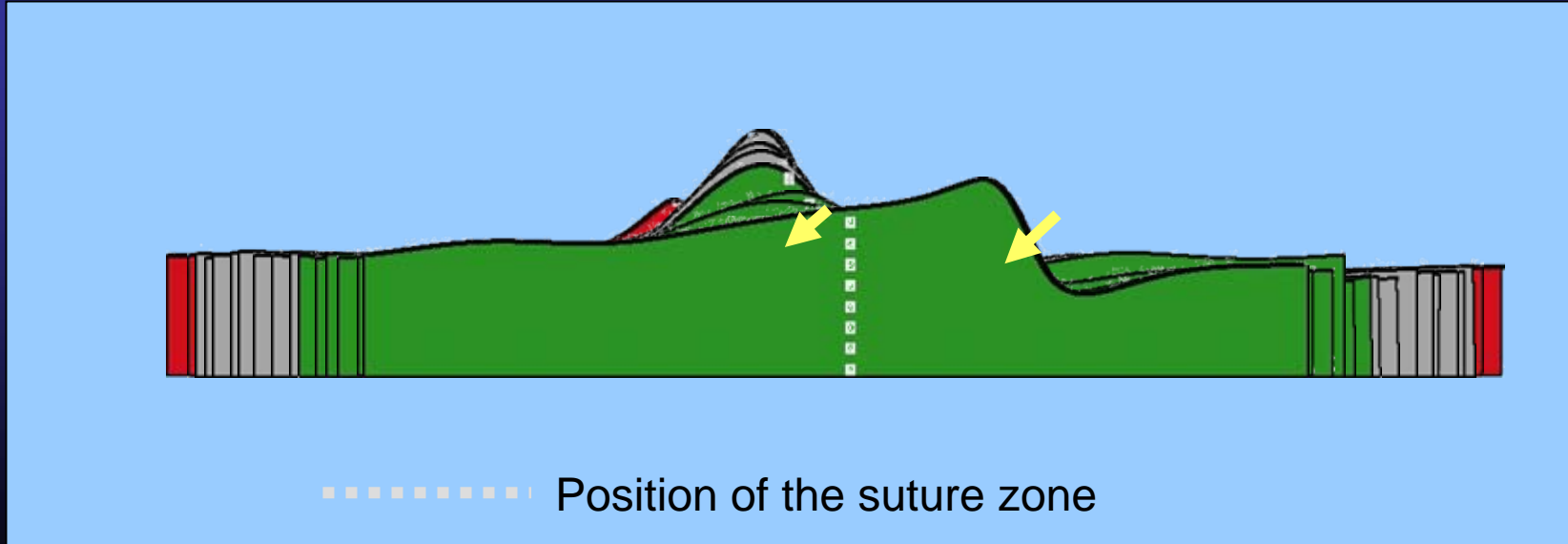
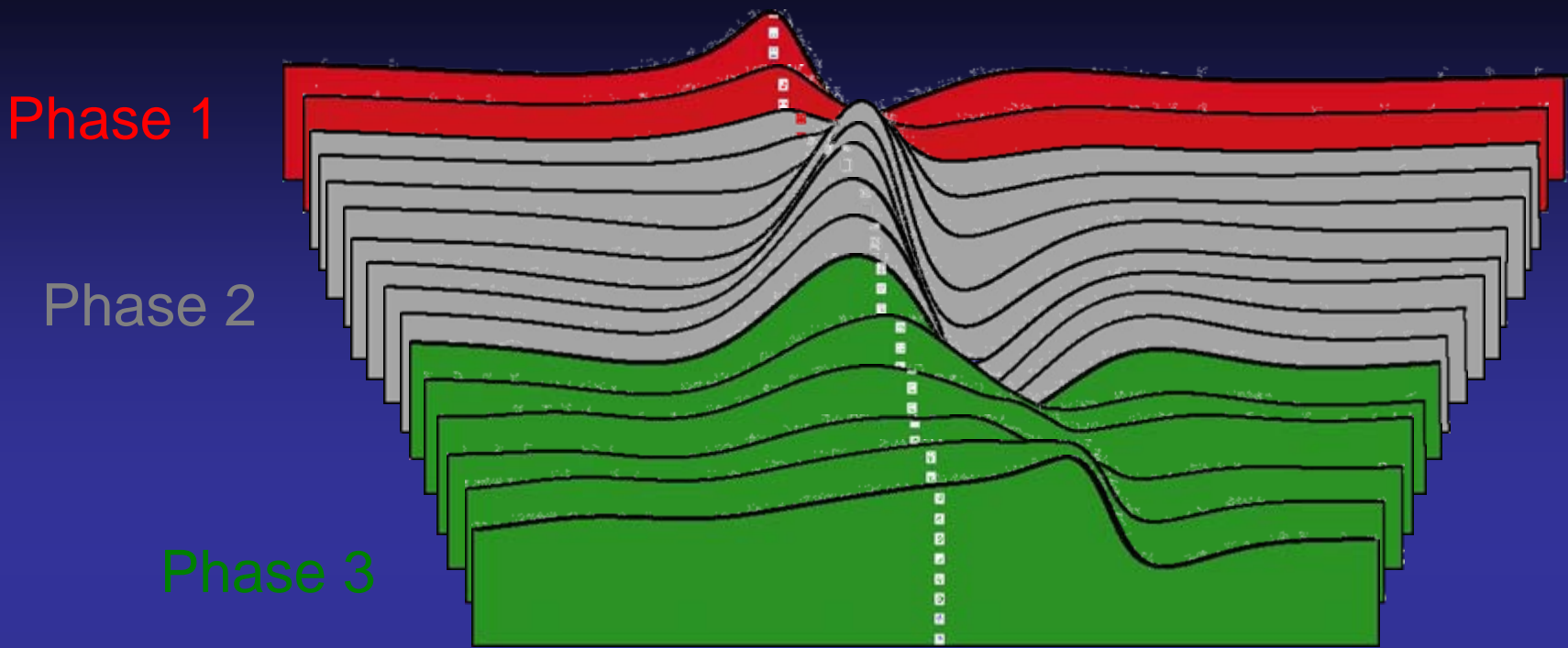
-3cm/y



$\Delta x = 660 \text{ km}$



Topography evolution



Δx from 220 to

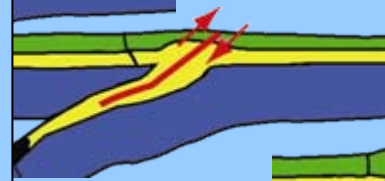
from $\Delta x = 0$ to 220km =
Himalaya between 50 and
30Ma?



- Deformation (backthrusting at suture)

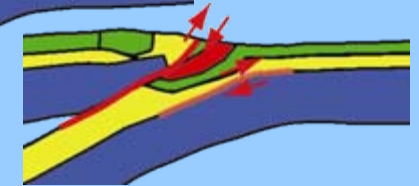


North of
the Southern
Frontal Thrust (STD)?

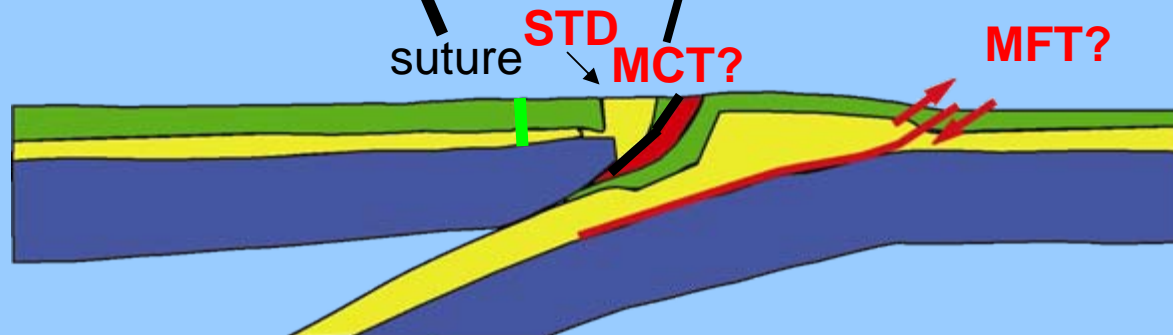


Major Thrust =
MCT?

lower crustal
exhumation



$\Delta x = 660\text{km}$ = Actual
Himalaya ?



- large prism developed at South of suture
- comparable size of the crustal prism
- deformation localized along the Frontal Thrust

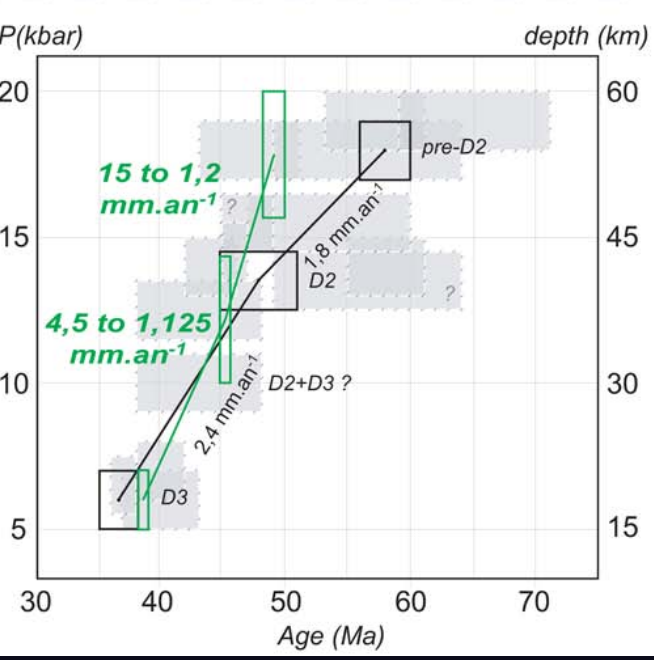
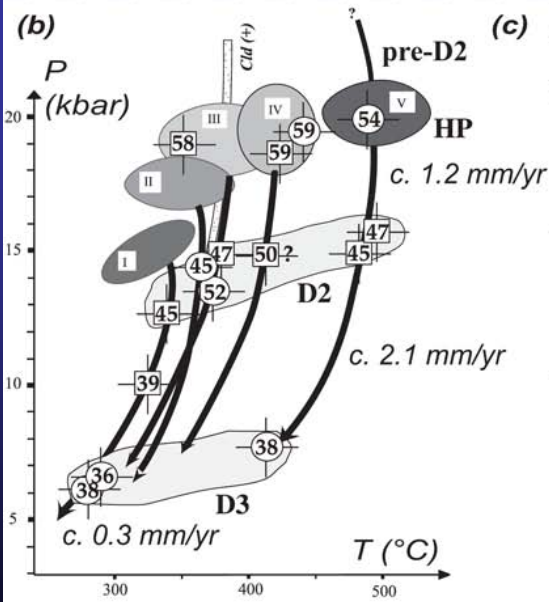
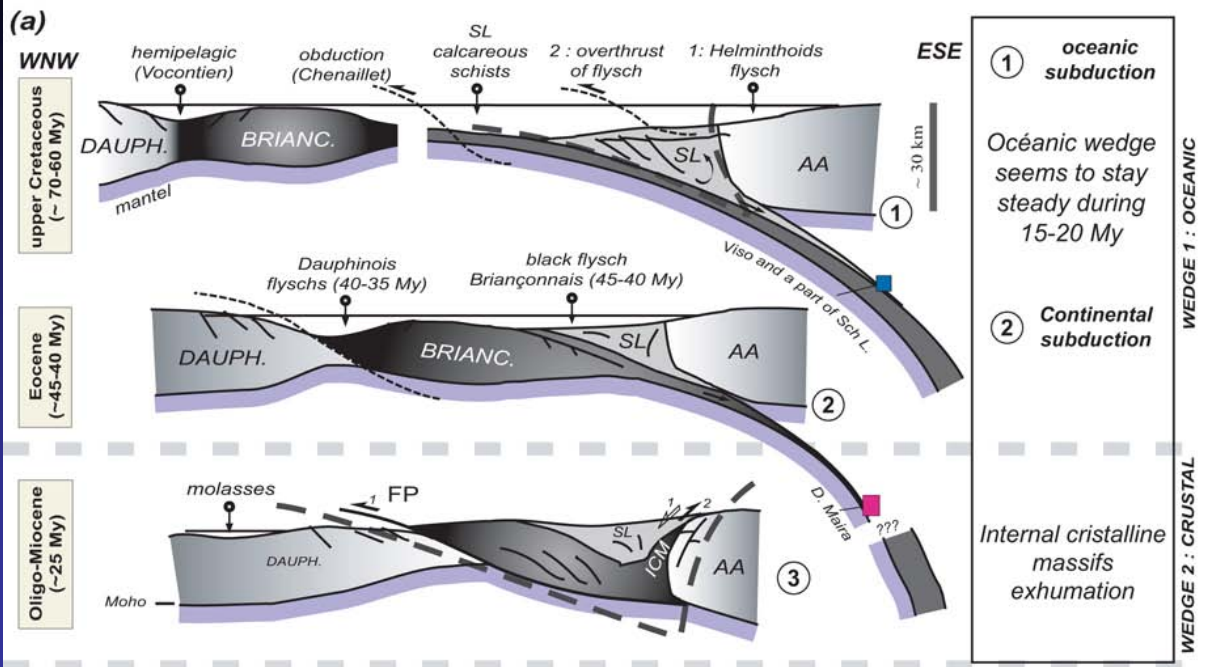
End-member case:

Low Peclet number (i.e. slow)

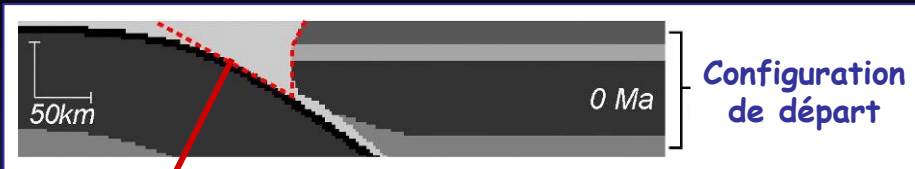
Convergence

Slow Alpine Collision I: Oceanic phase

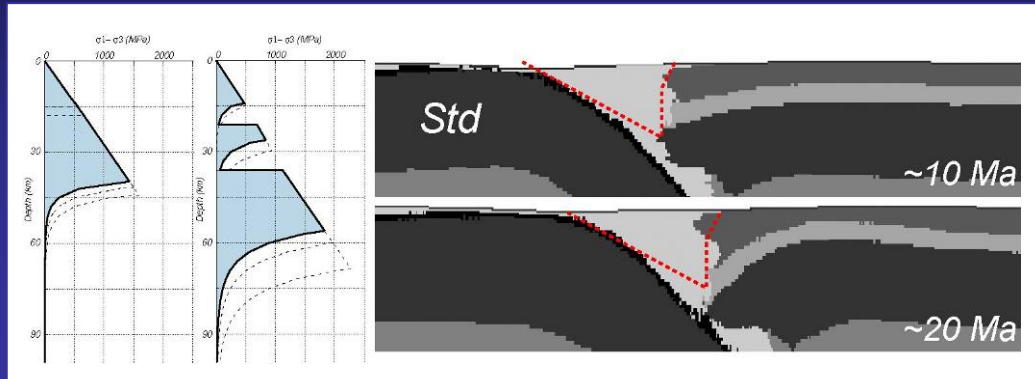
*PhD thesis of Ph. Yamato;
Yamato et al., 2007*



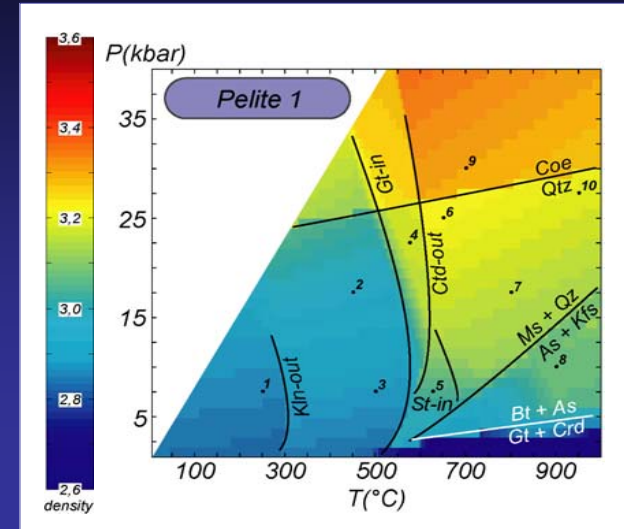
Accretion prism stability



Initial geometry

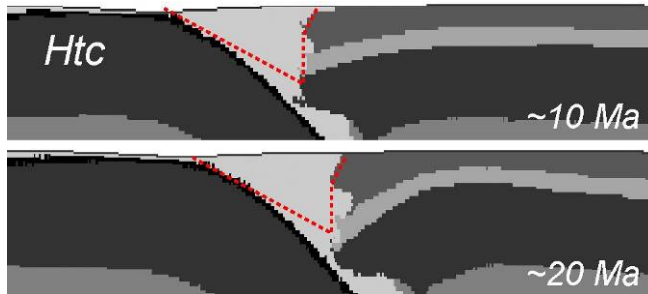


Stable case



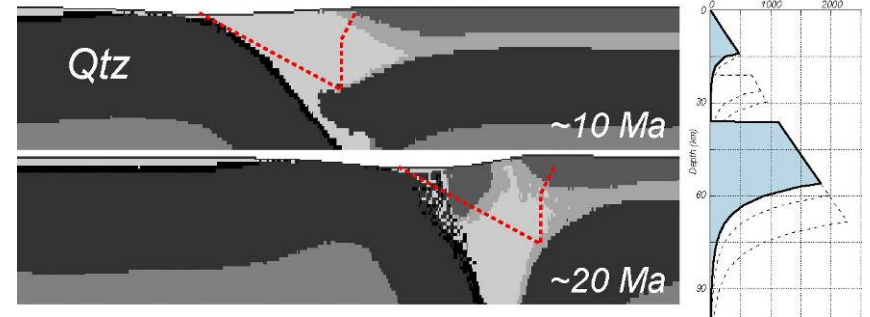
Instable case

strong continental crust

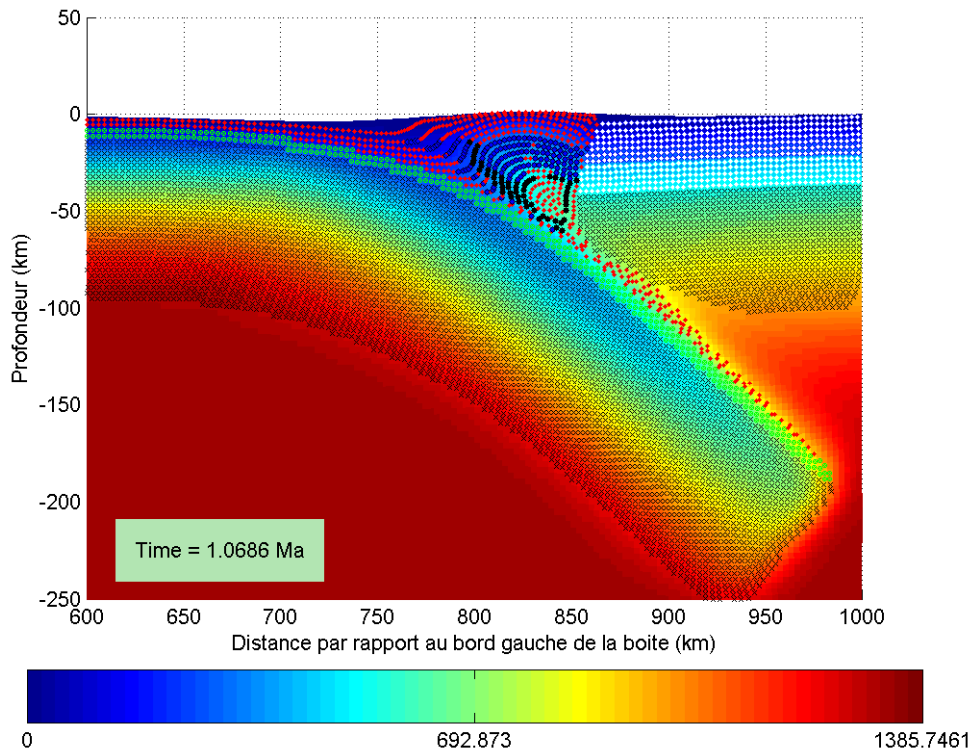
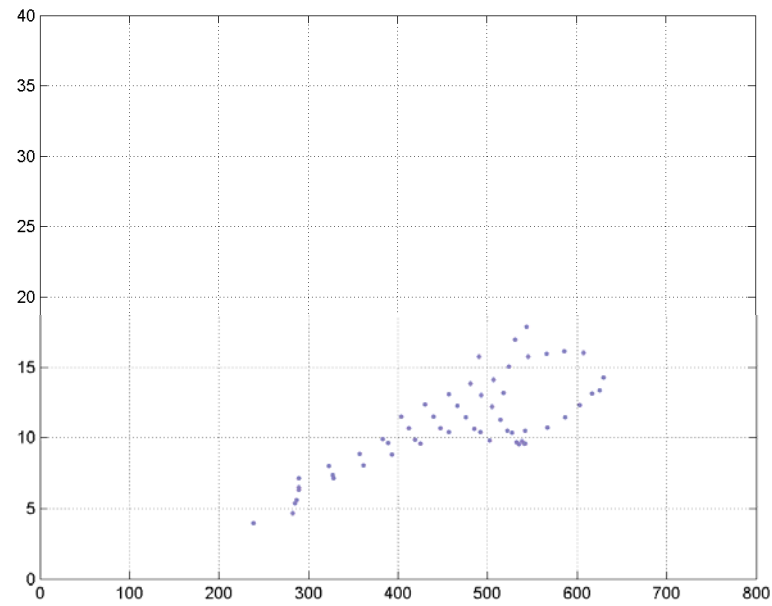
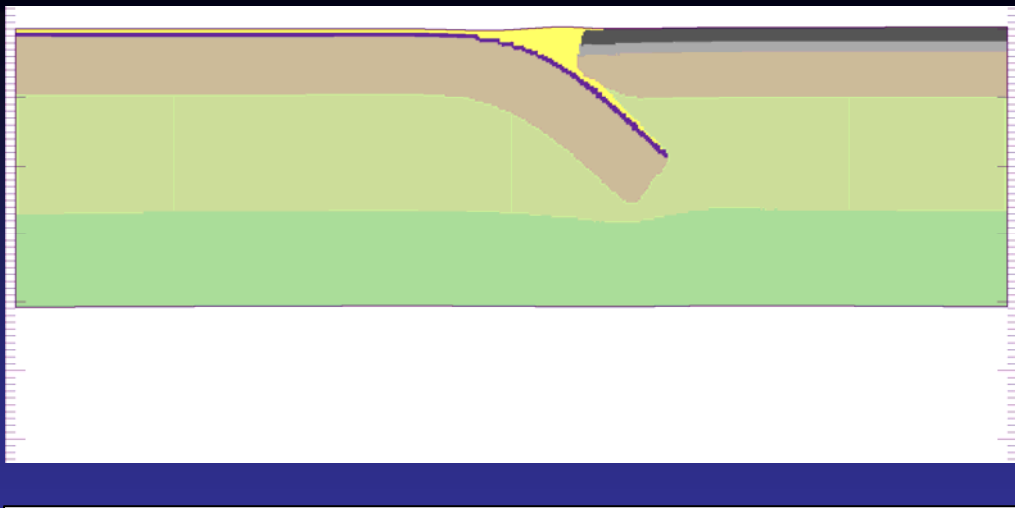


Old upper plate

weak continental crust

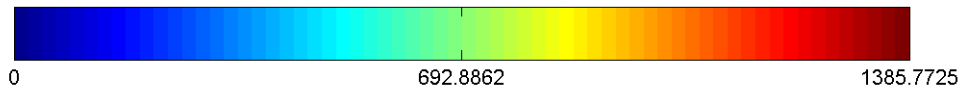
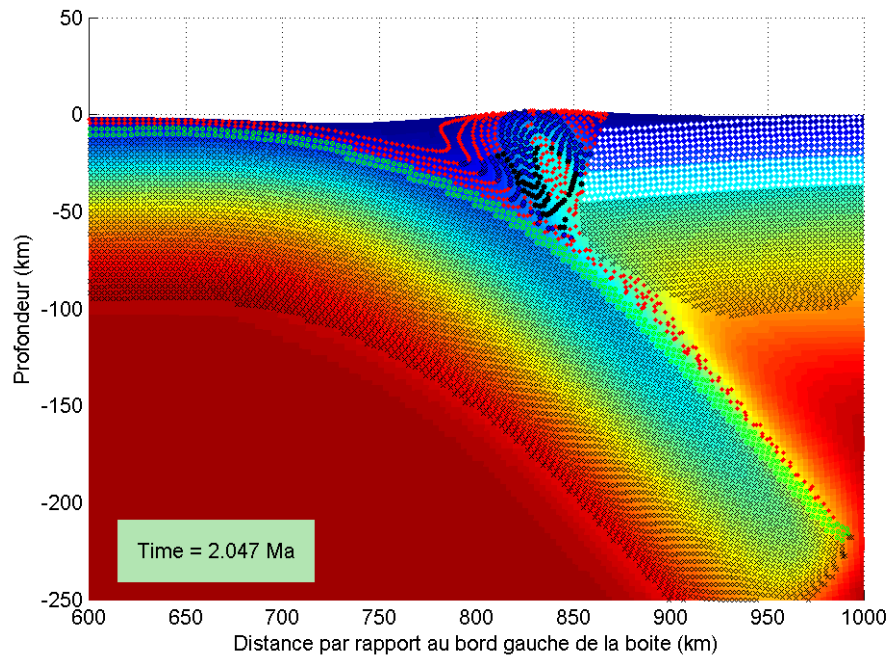
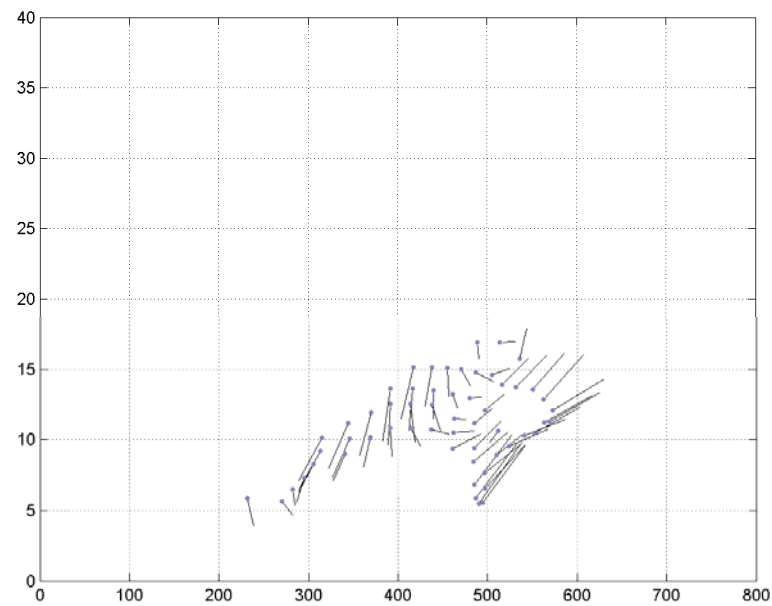
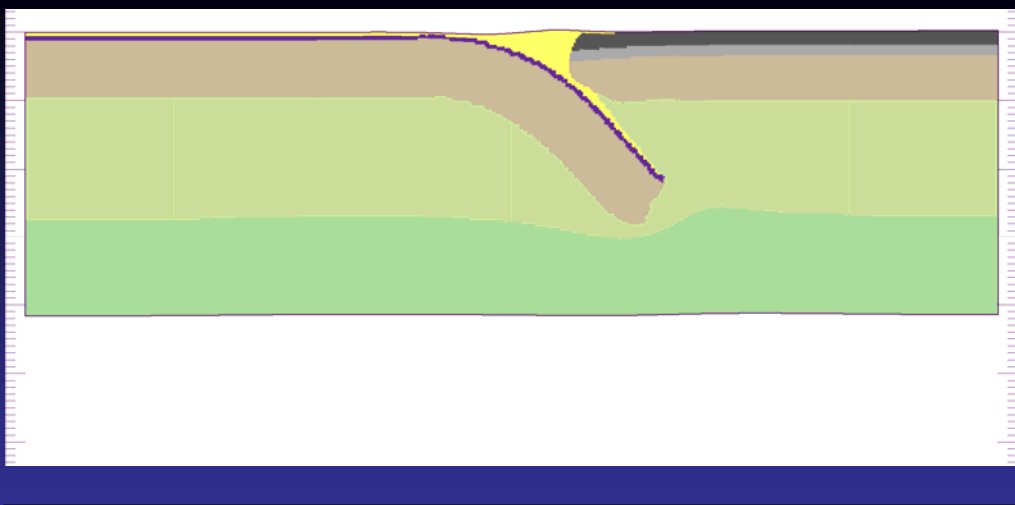


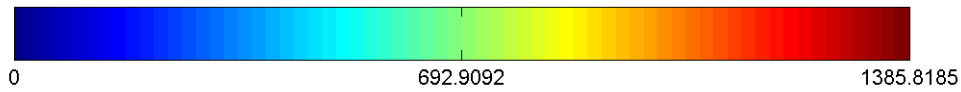
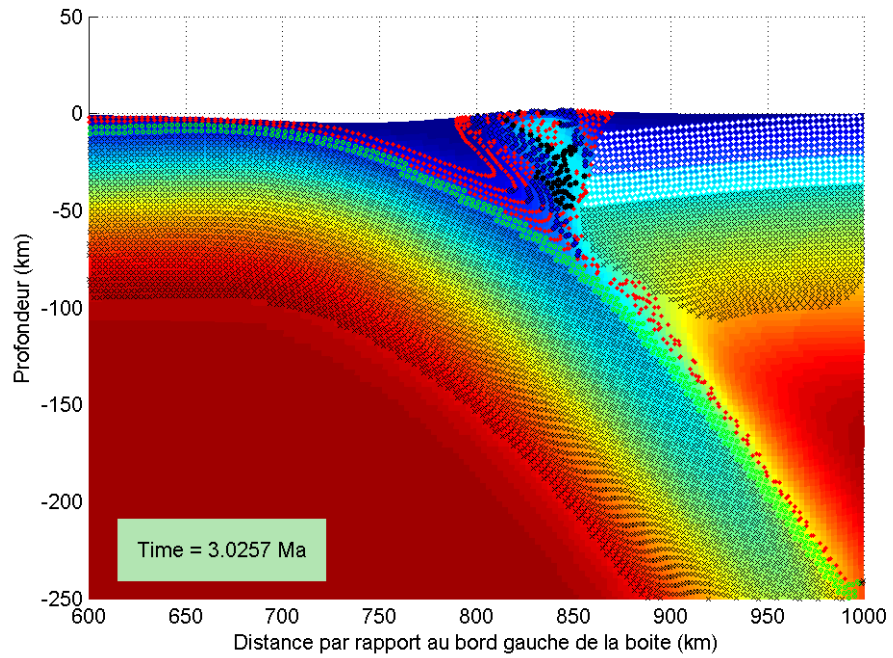
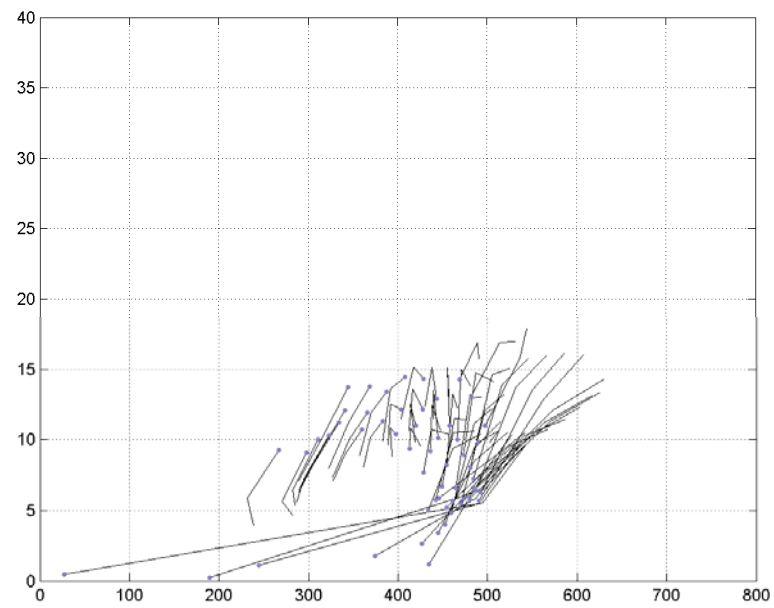
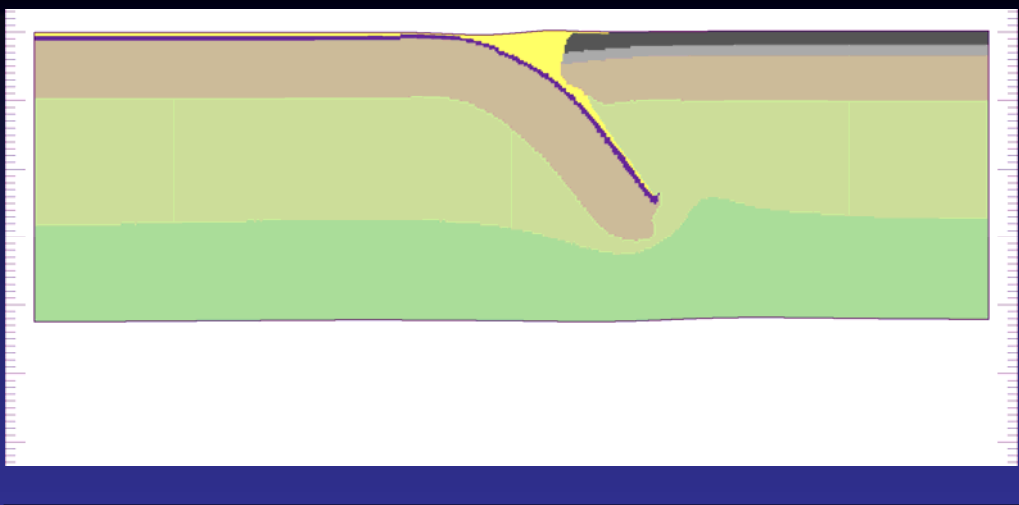
$V = 1,5 \text{ cm.an}^{-1}; V = 6 \text{ cm.an}^{-1}$
 Low sediment viscosity
 Schistes go down
 Pelite less rich in Al

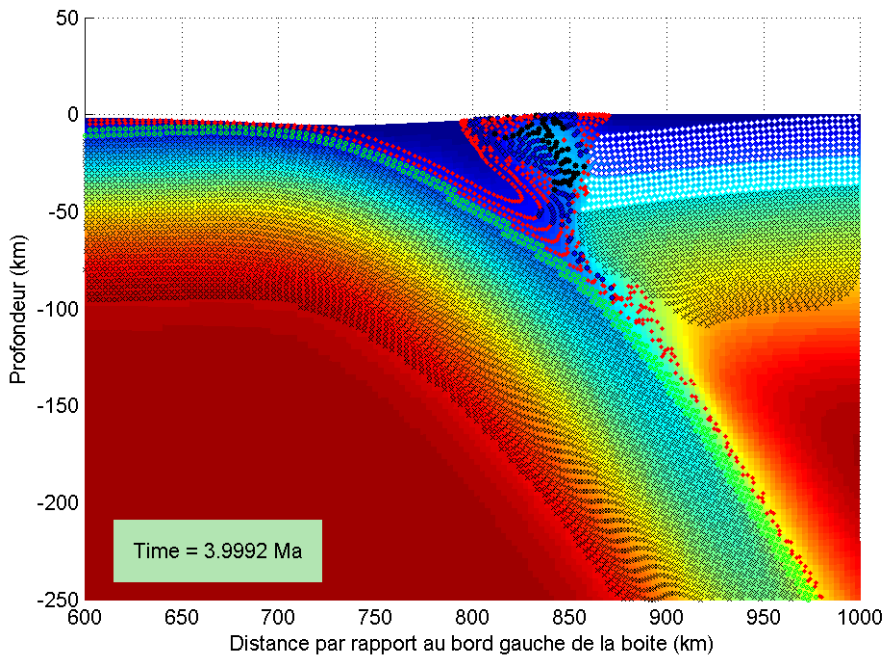
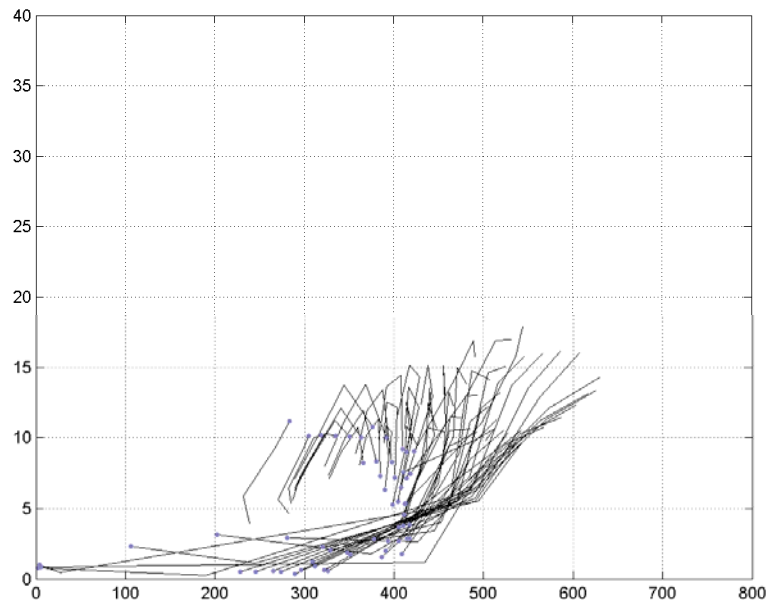
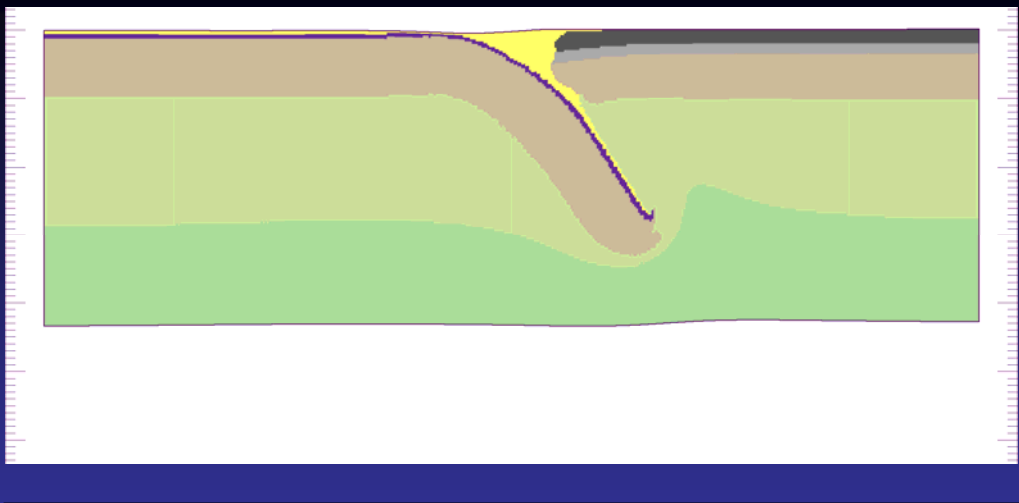


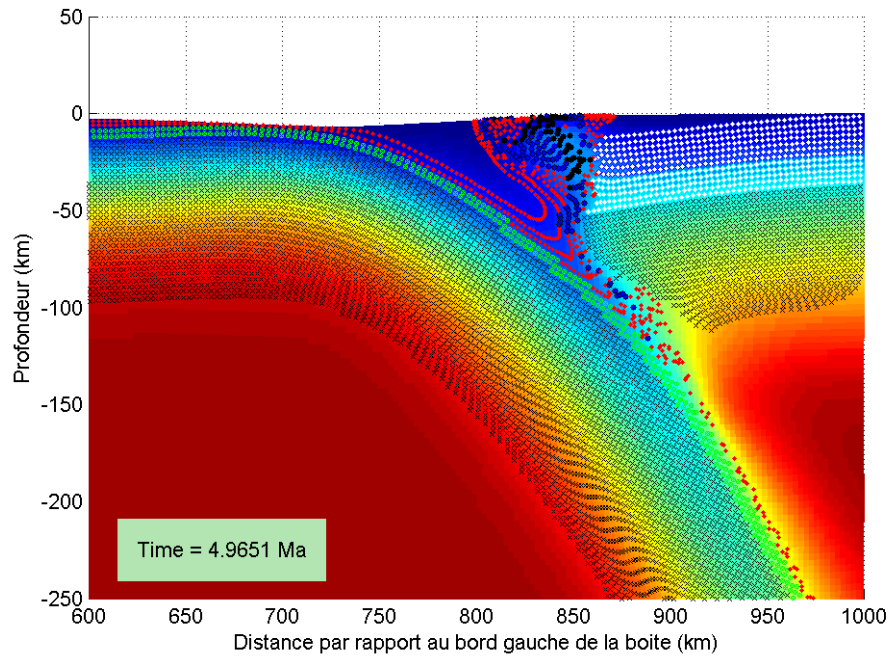
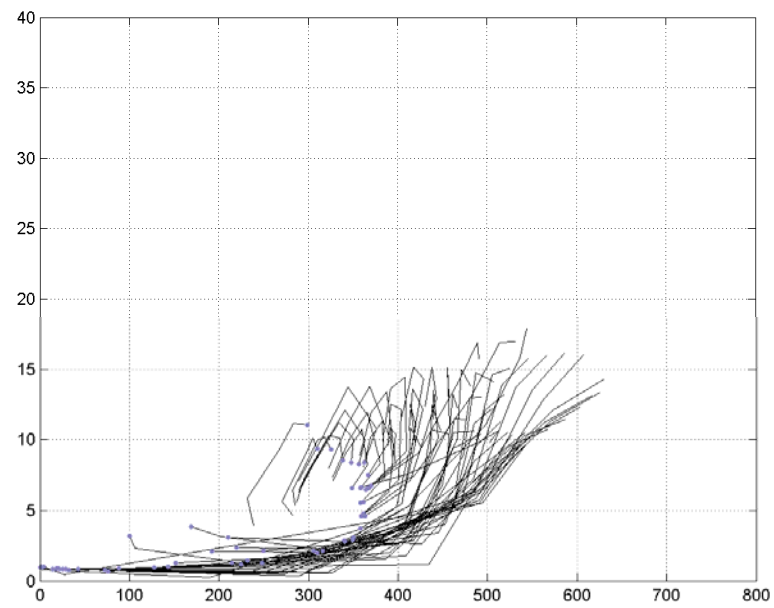
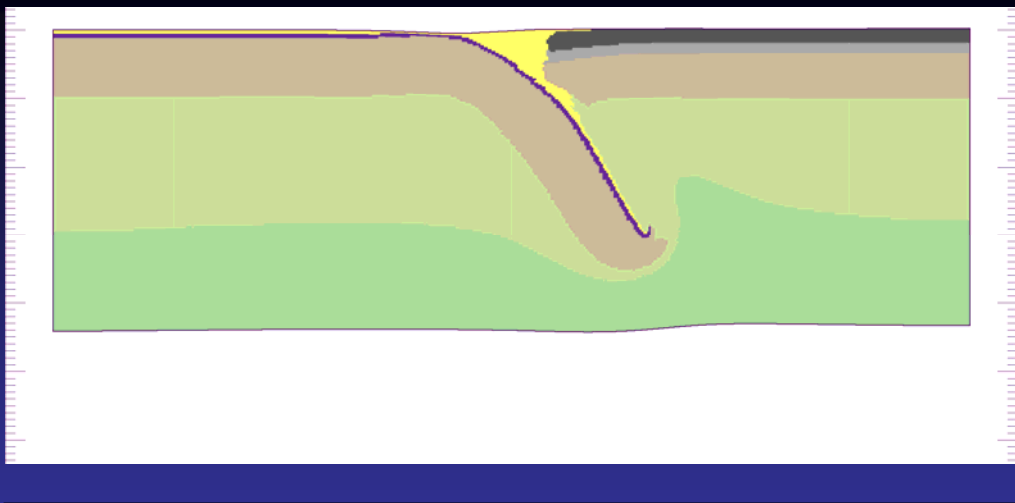
wait ...

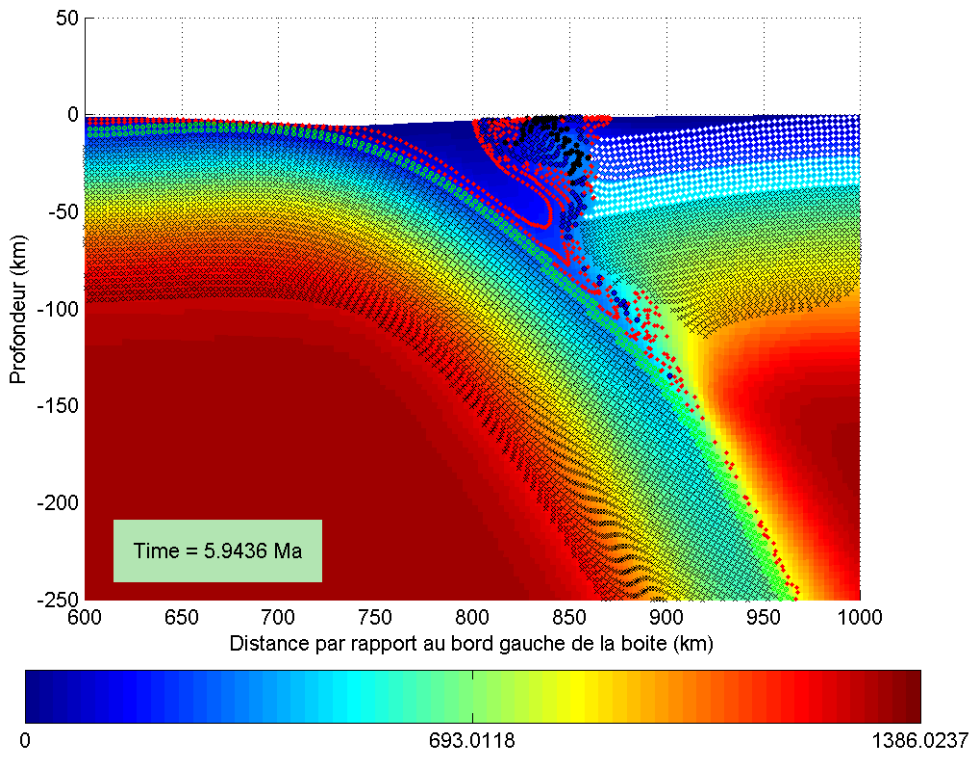
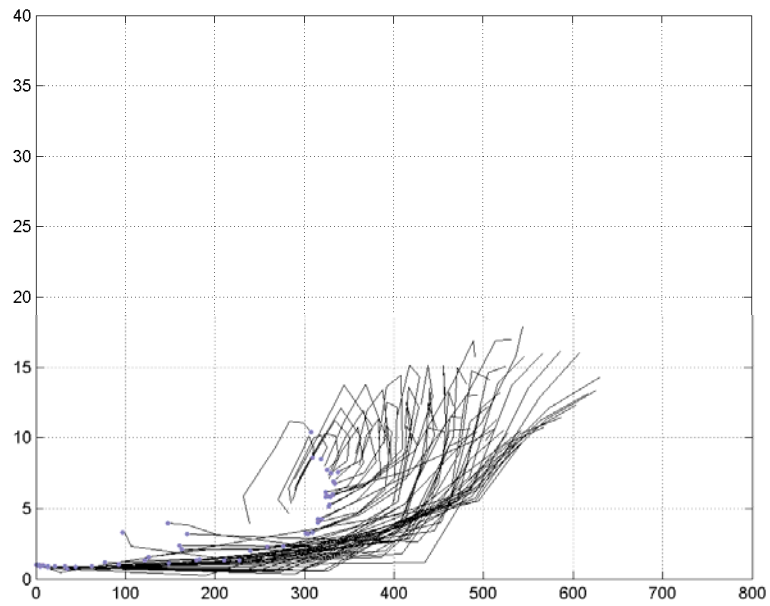
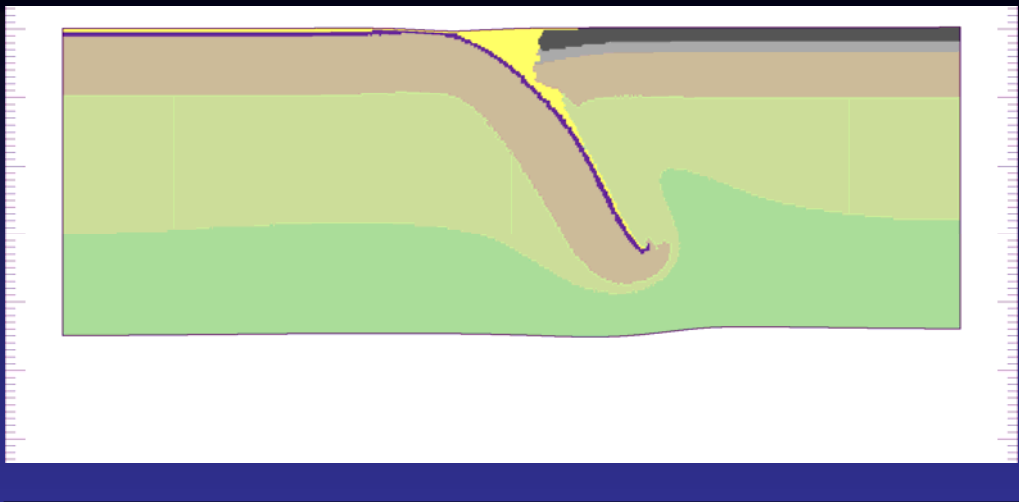
*PhD thesis of Ph. Yamato;
Yamato et al., 2007
Burov and Yamato, 2007*

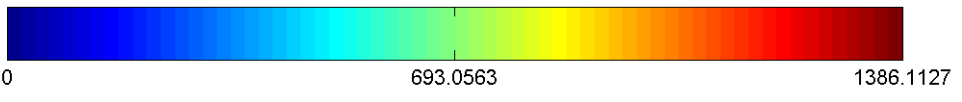
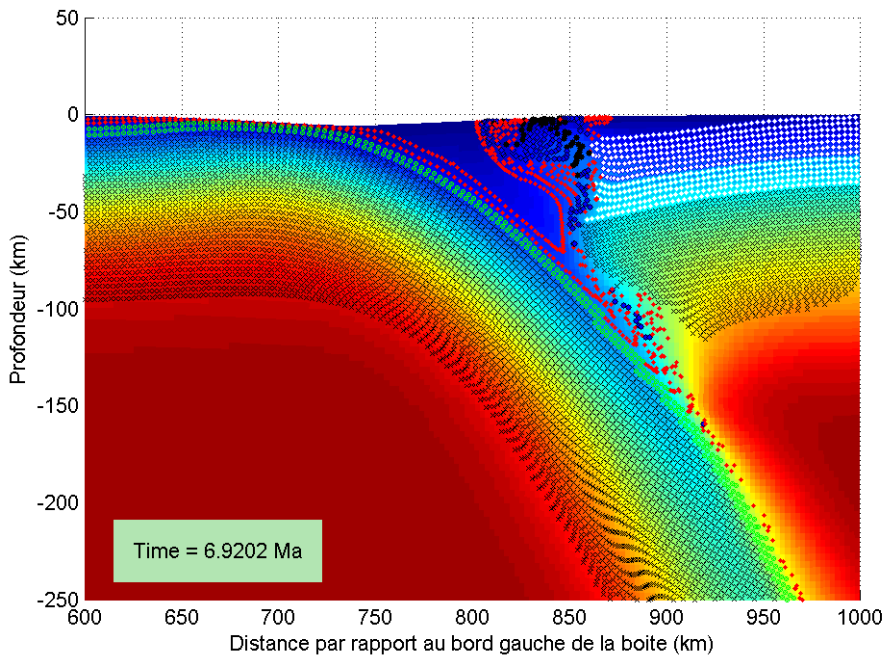
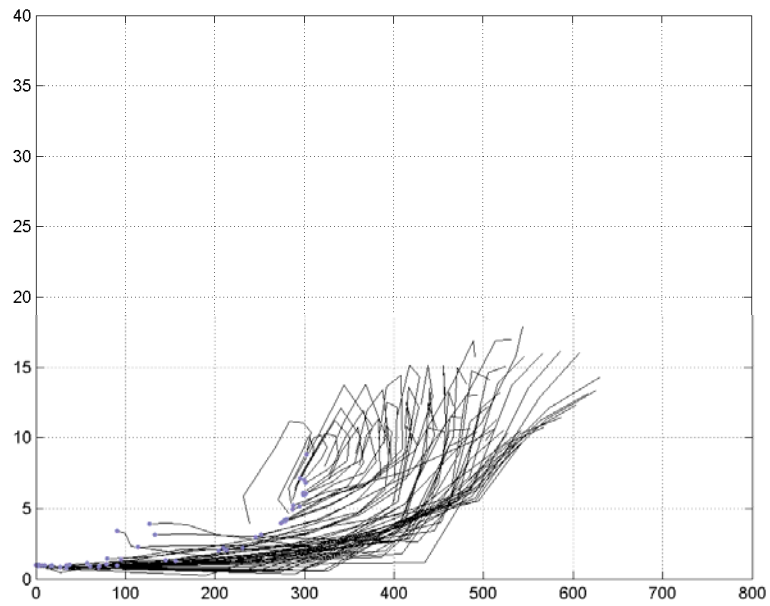
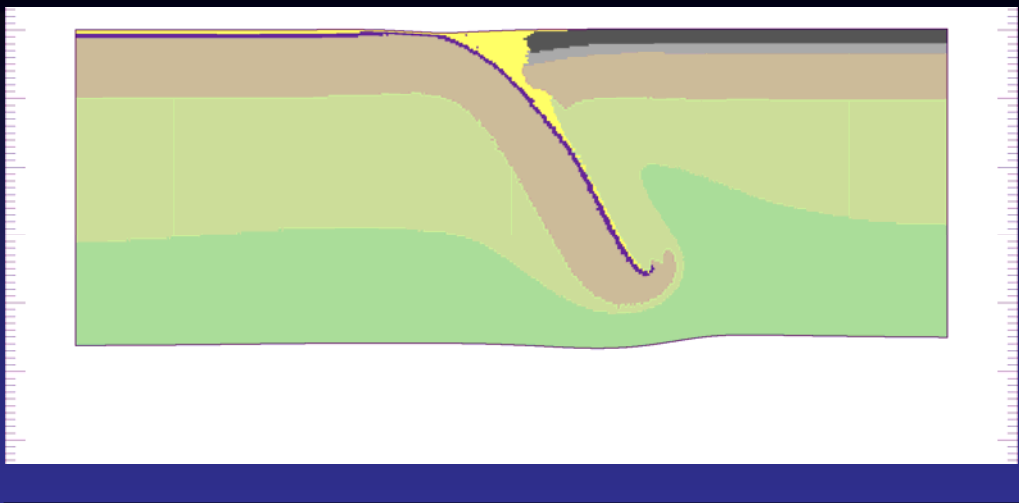


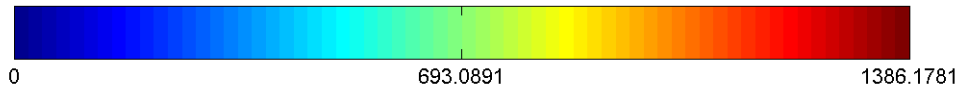
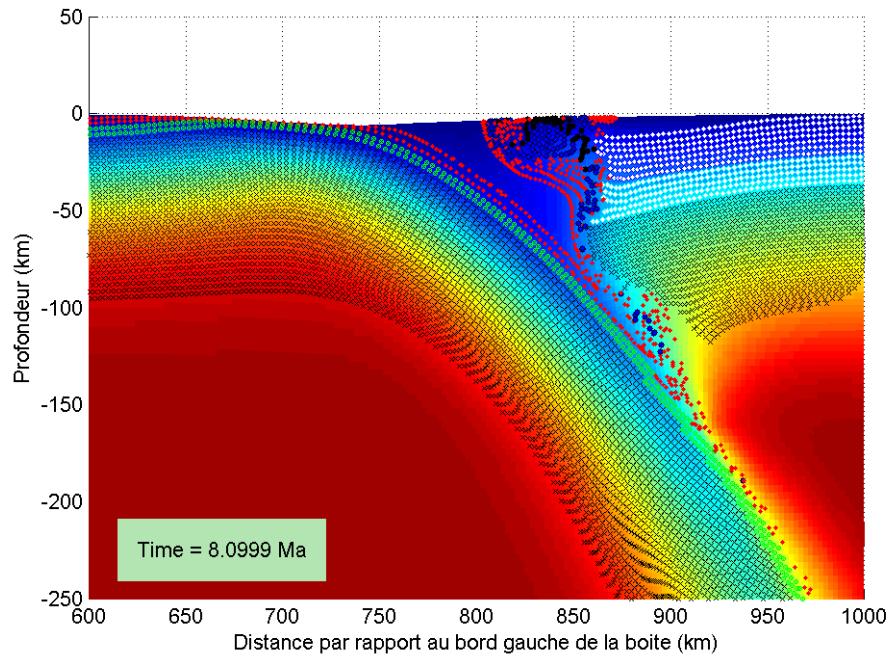
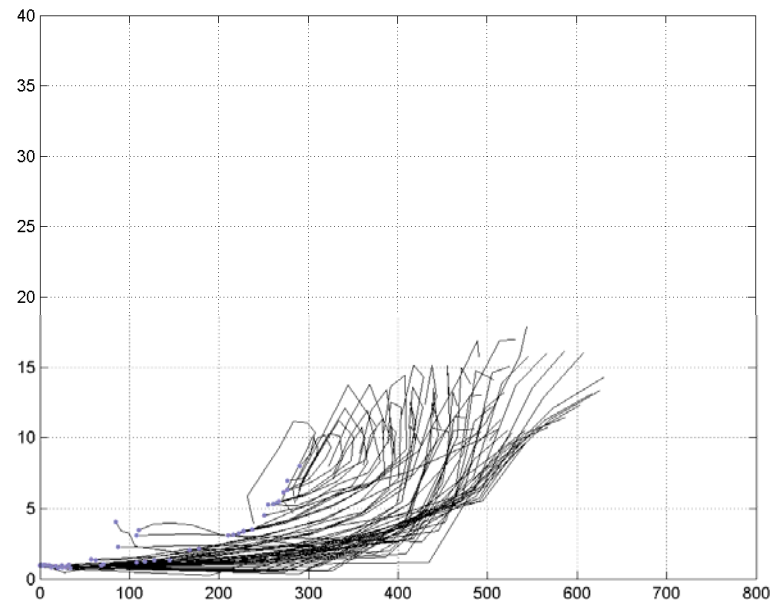
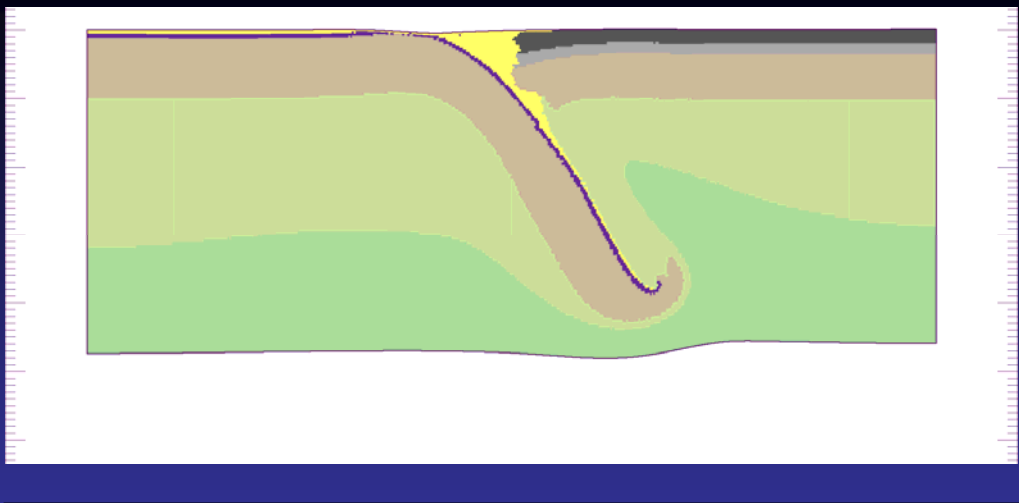


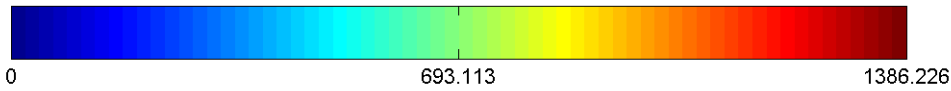
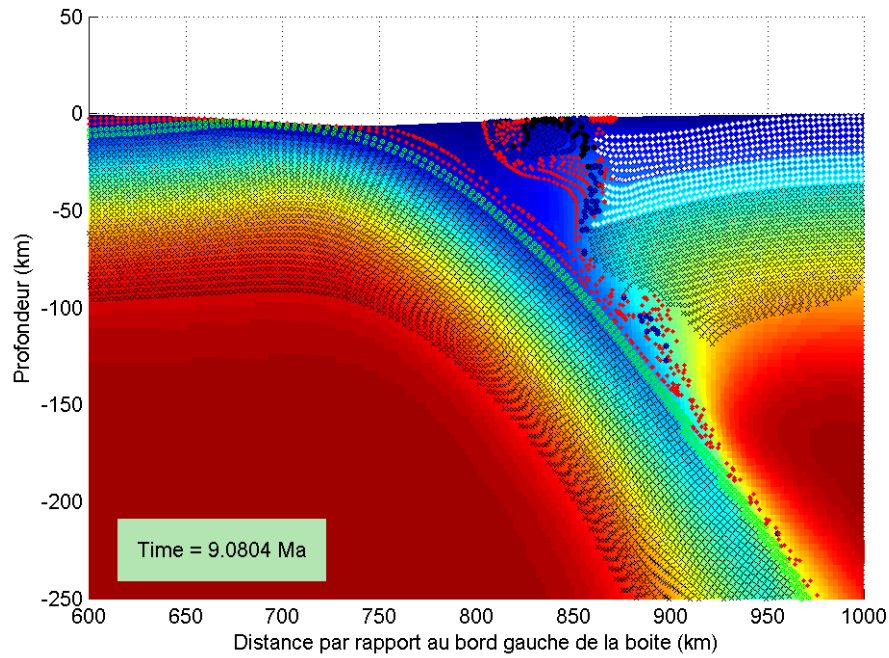
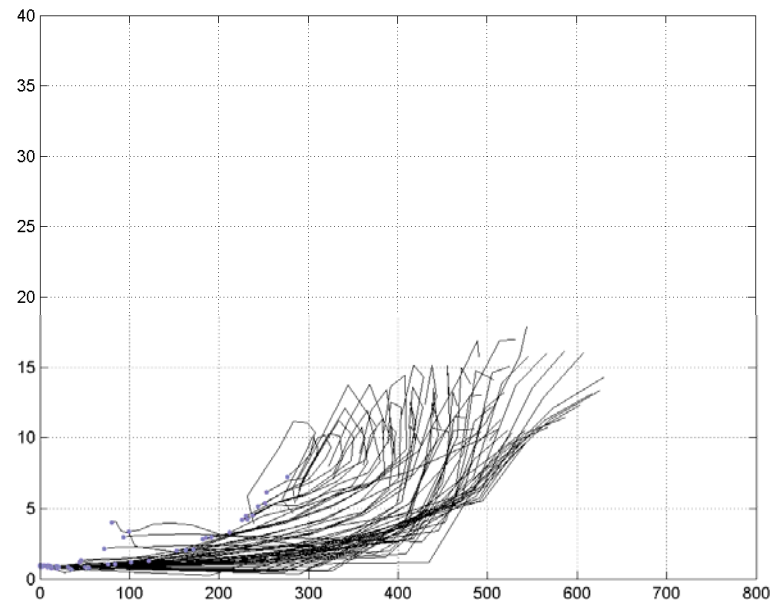
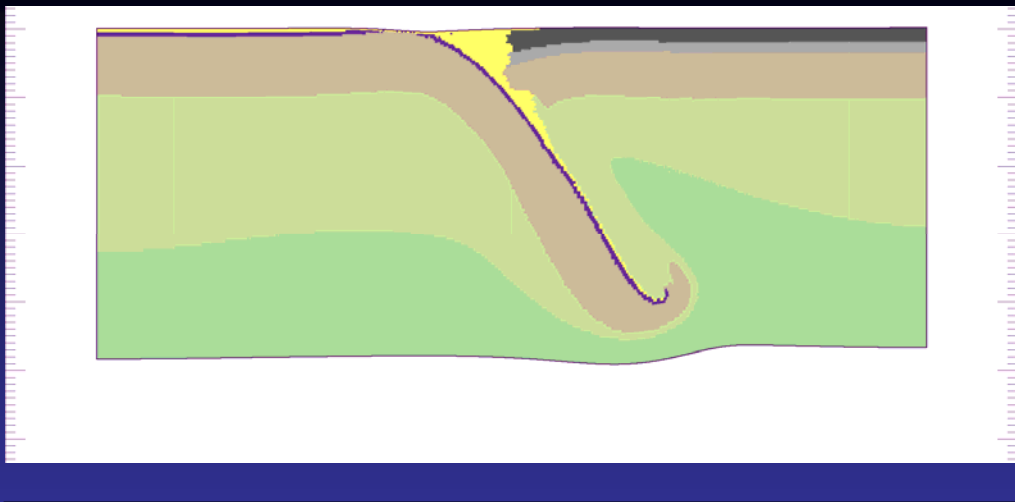


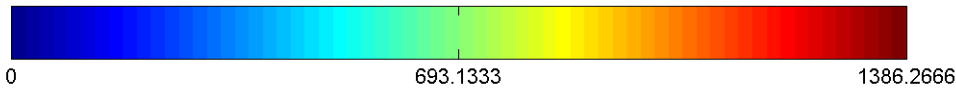
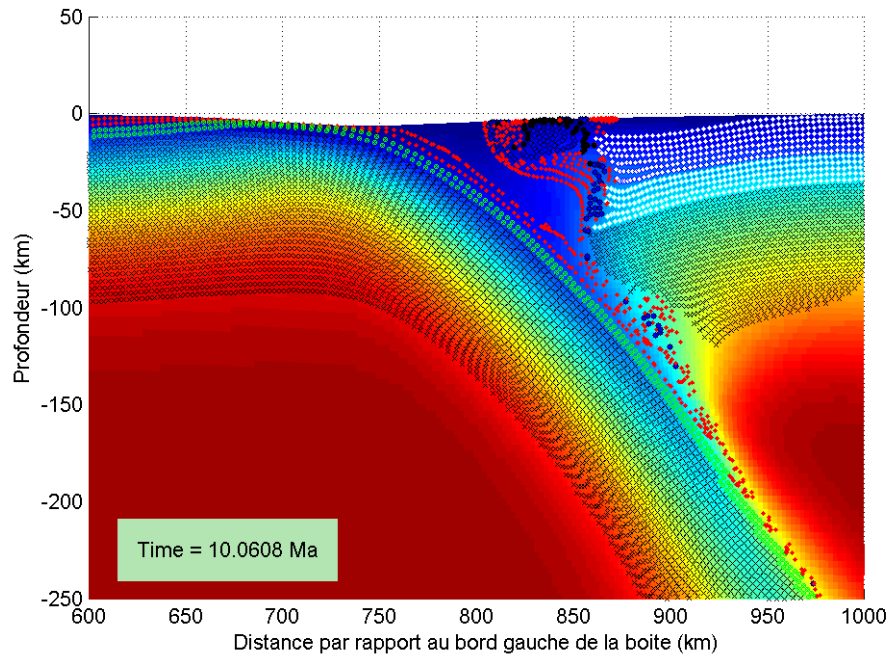
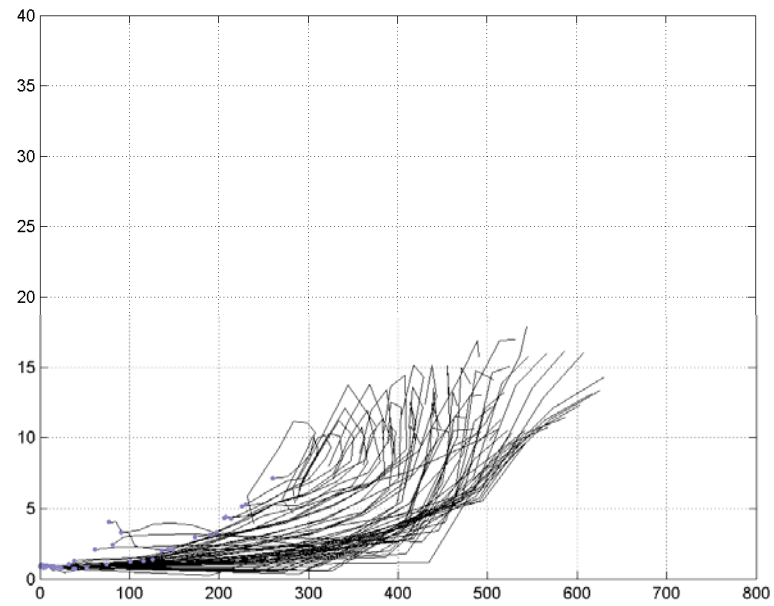
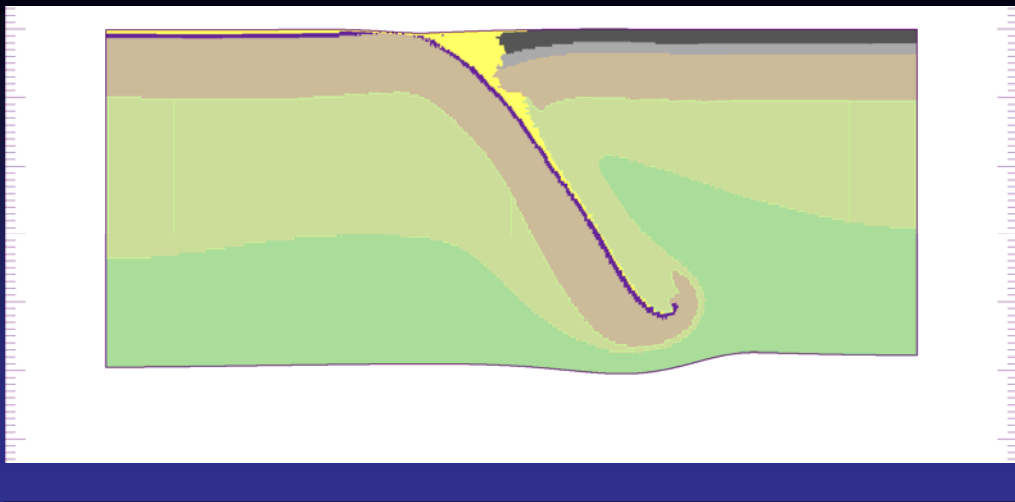


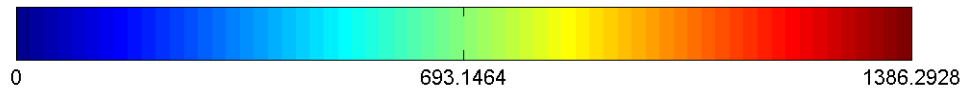
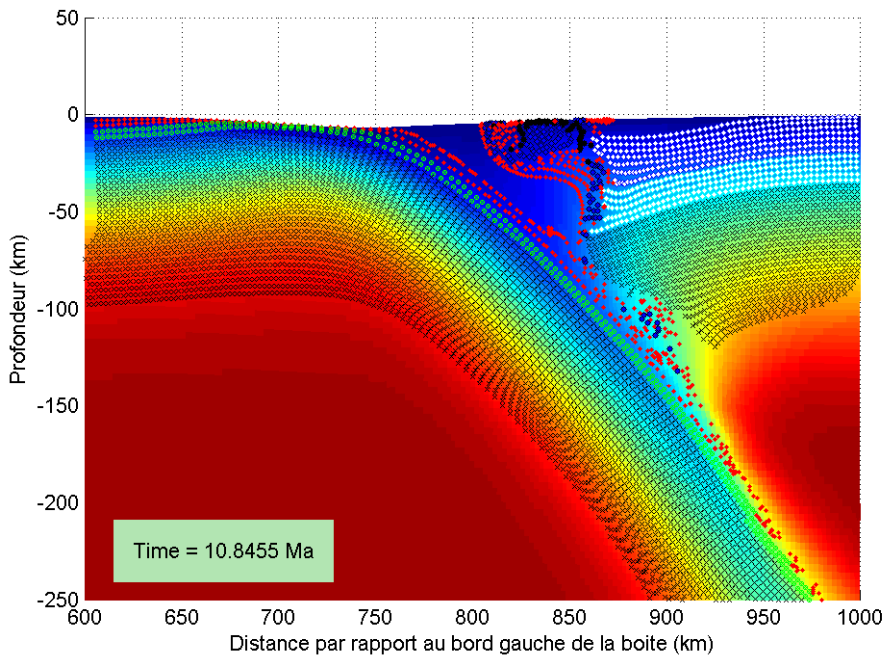
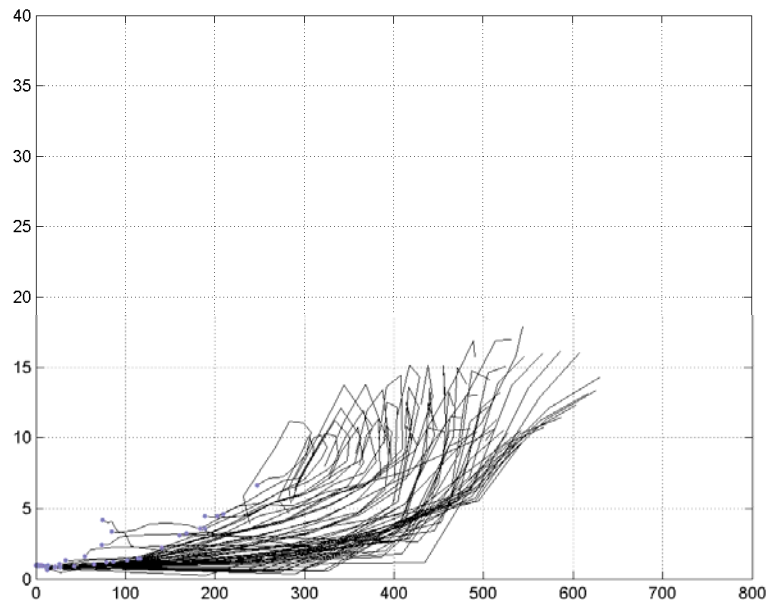


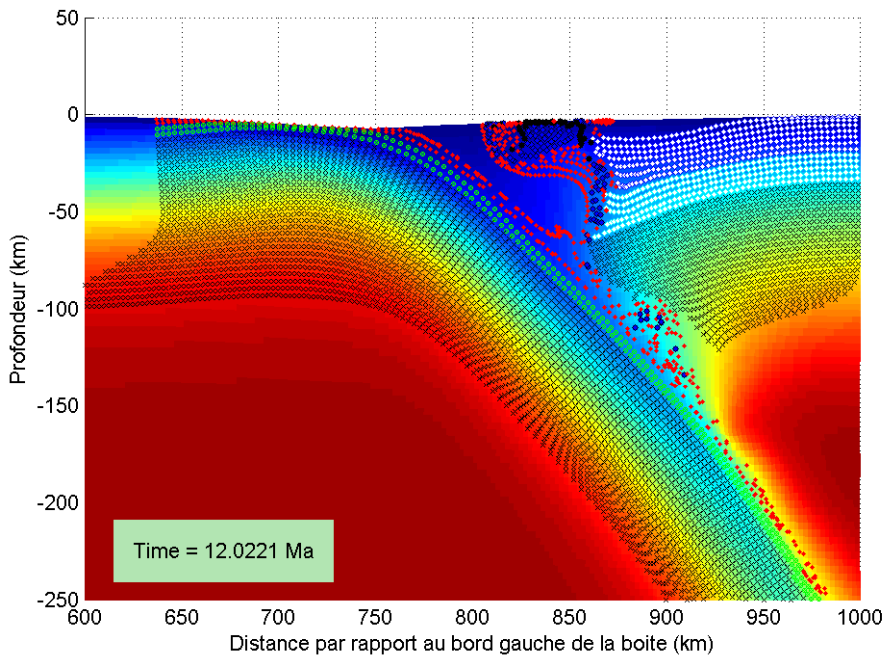
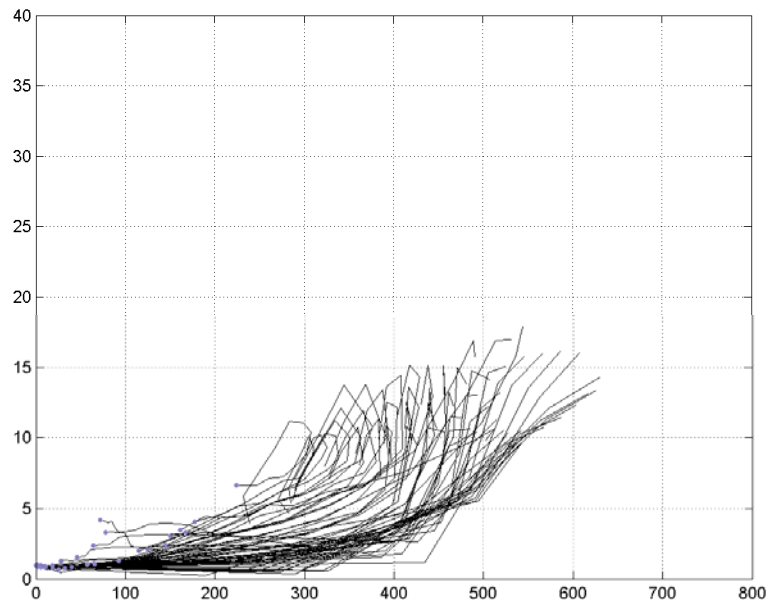


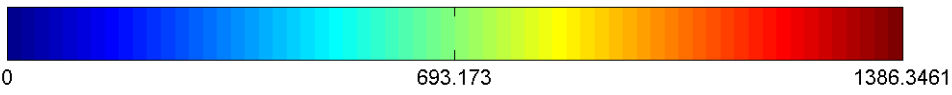
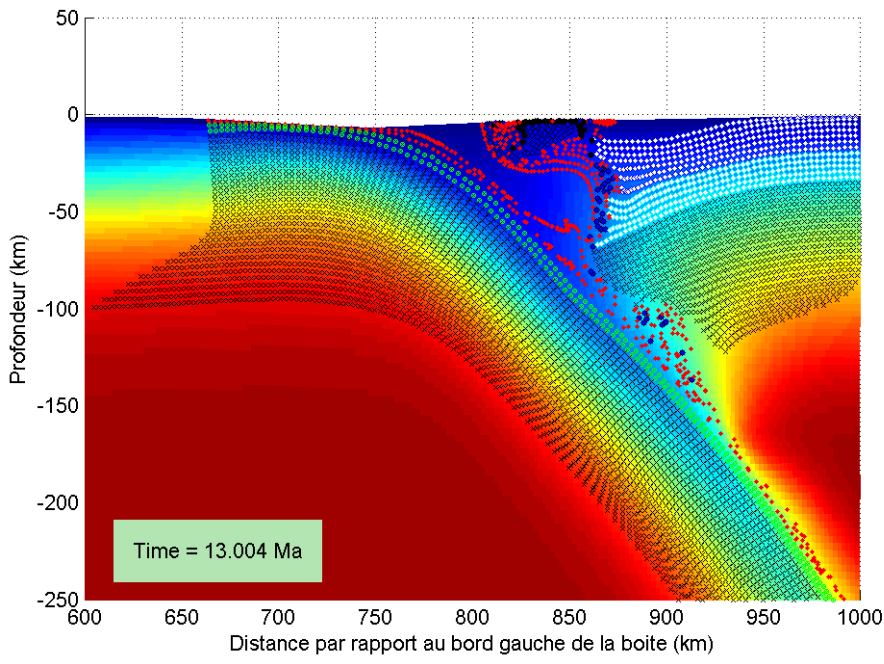
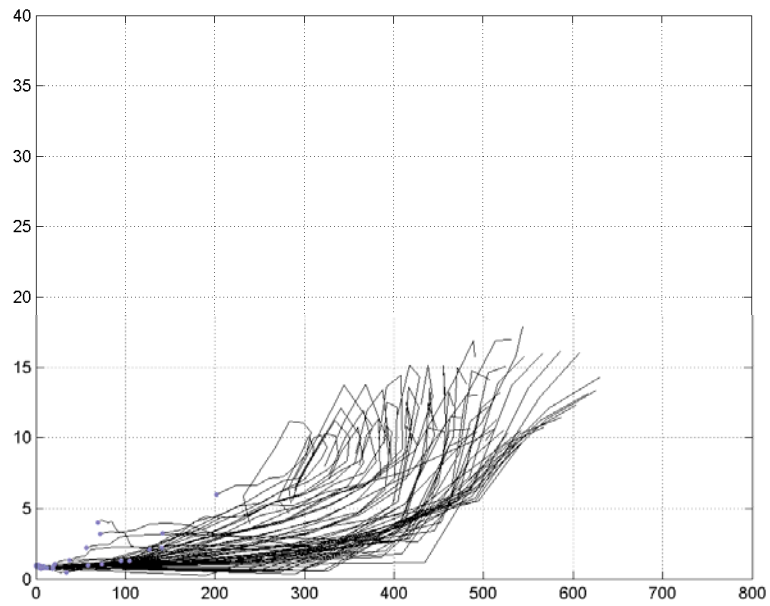
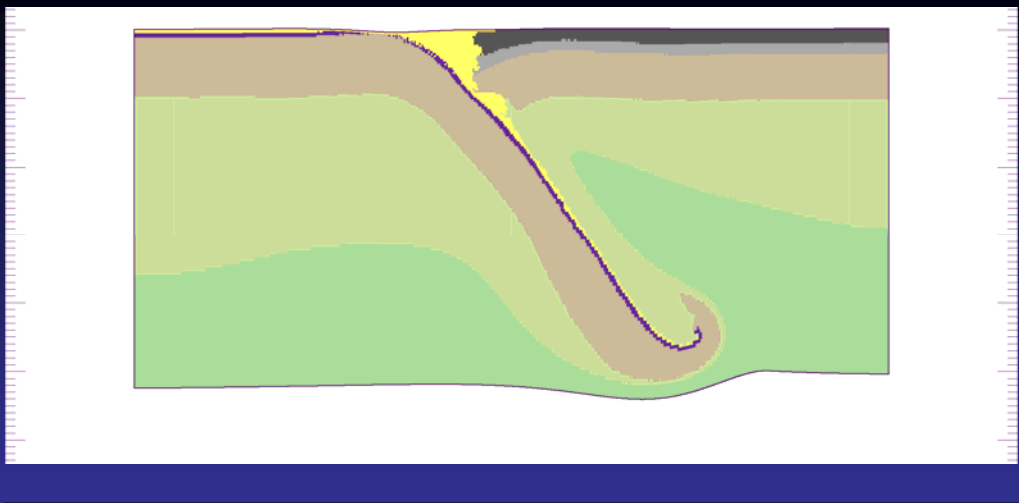


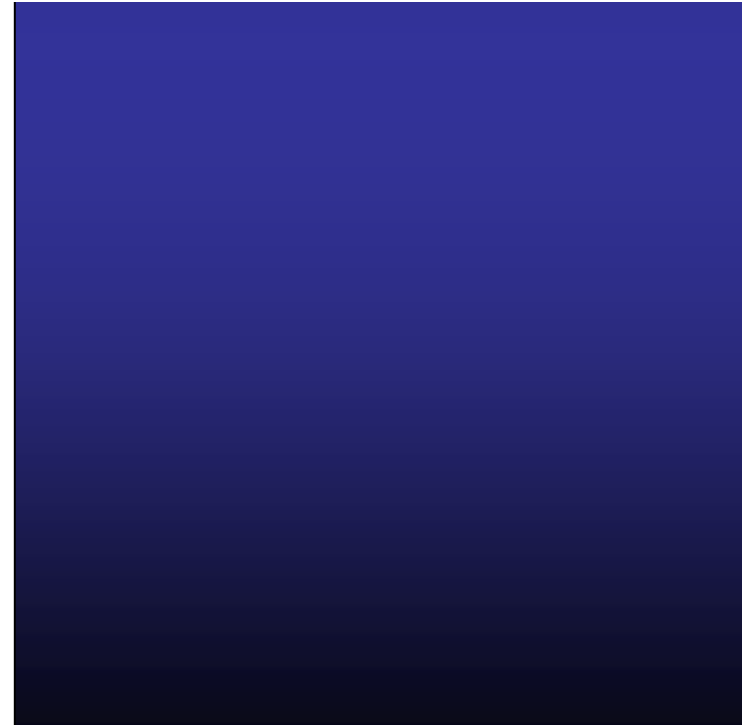
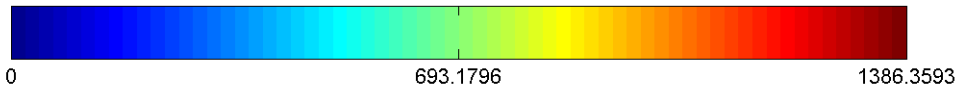
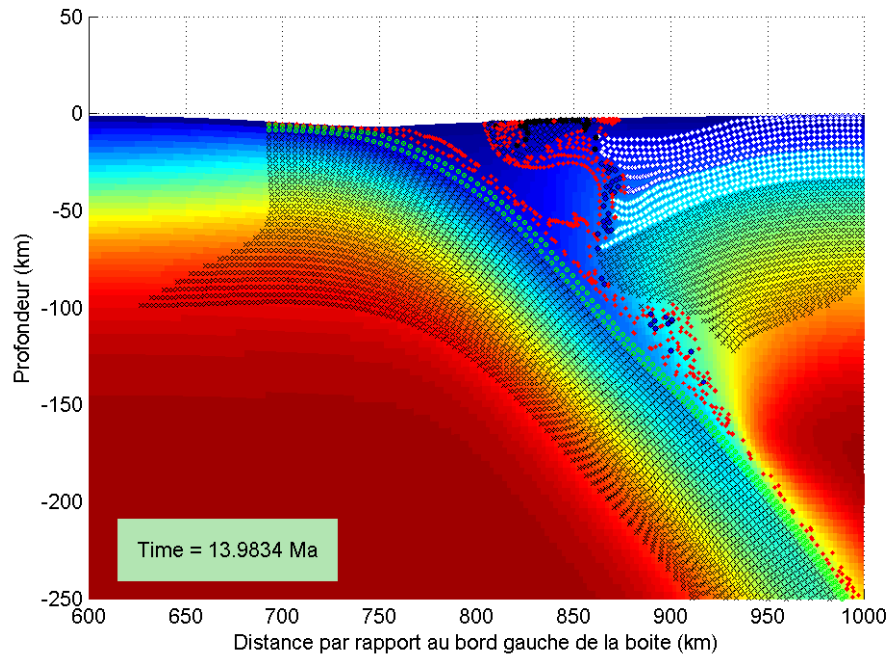
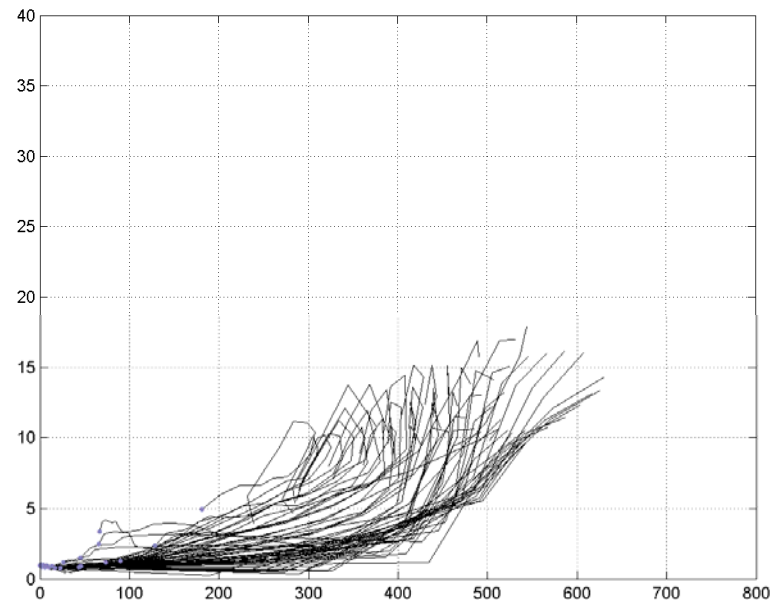


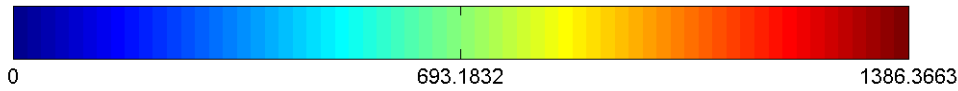
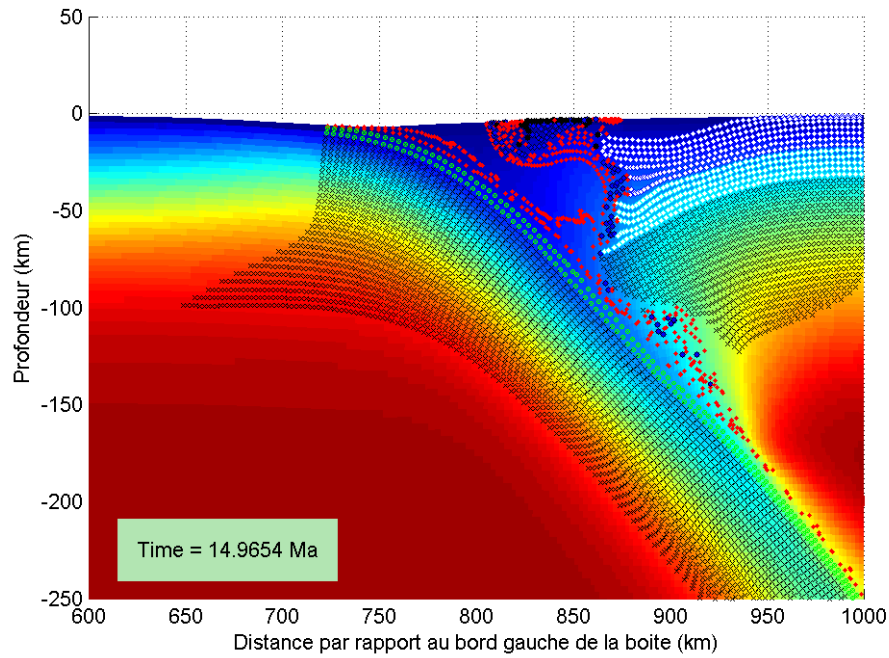
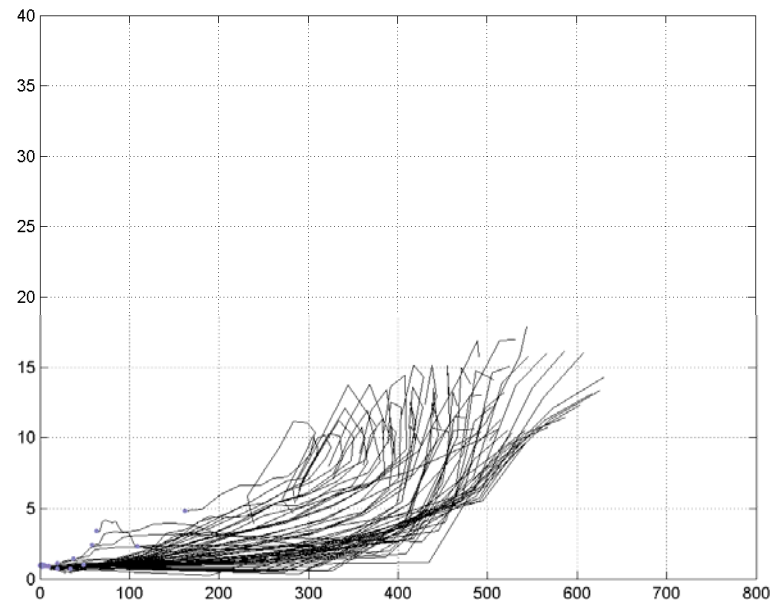
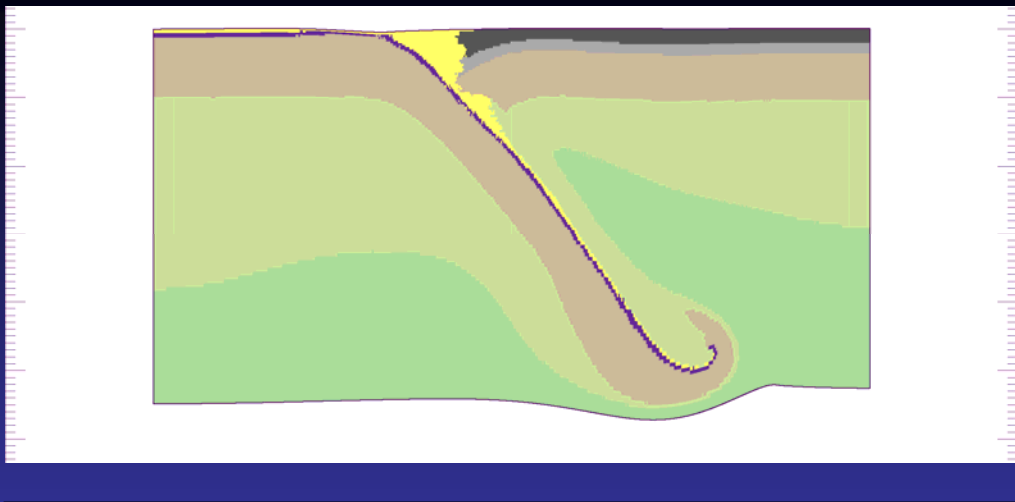


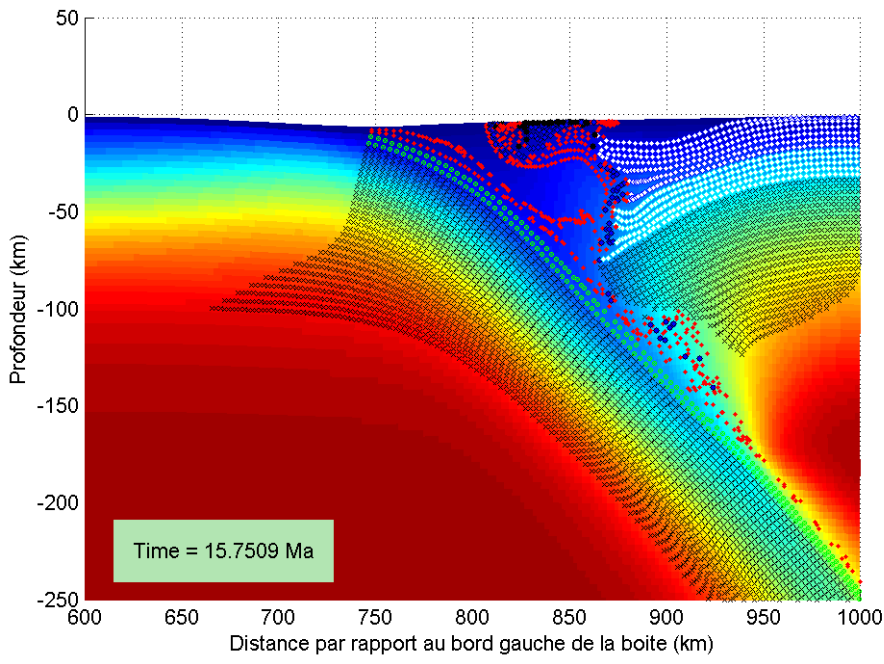
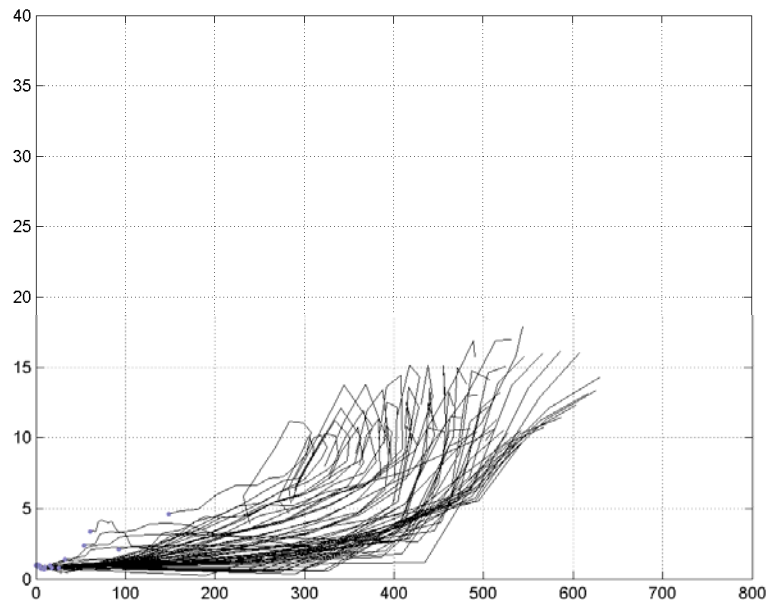
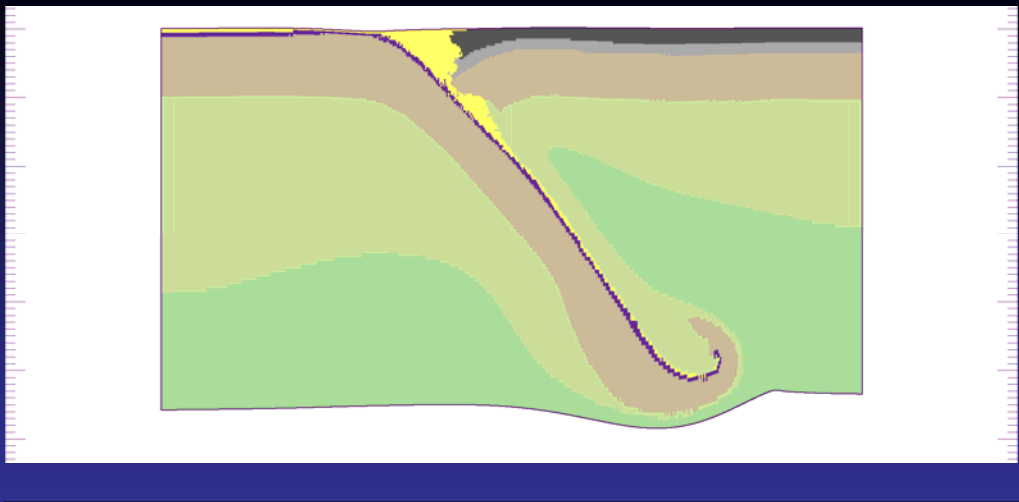


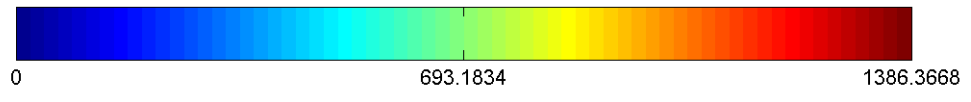
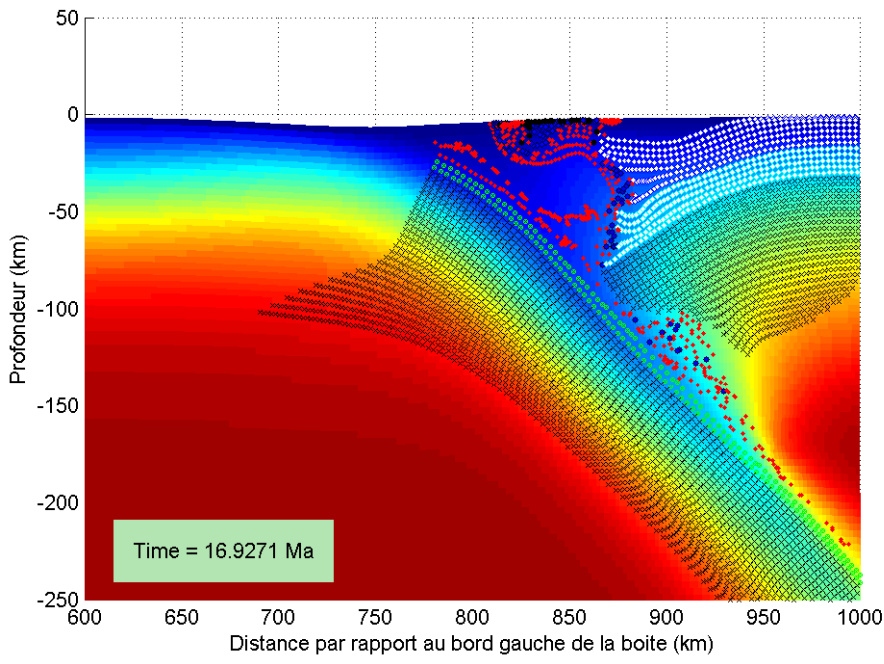
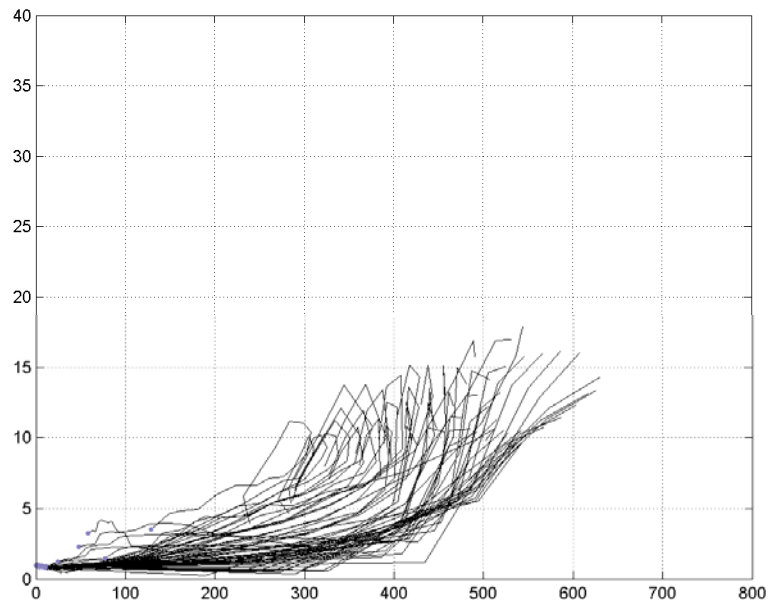
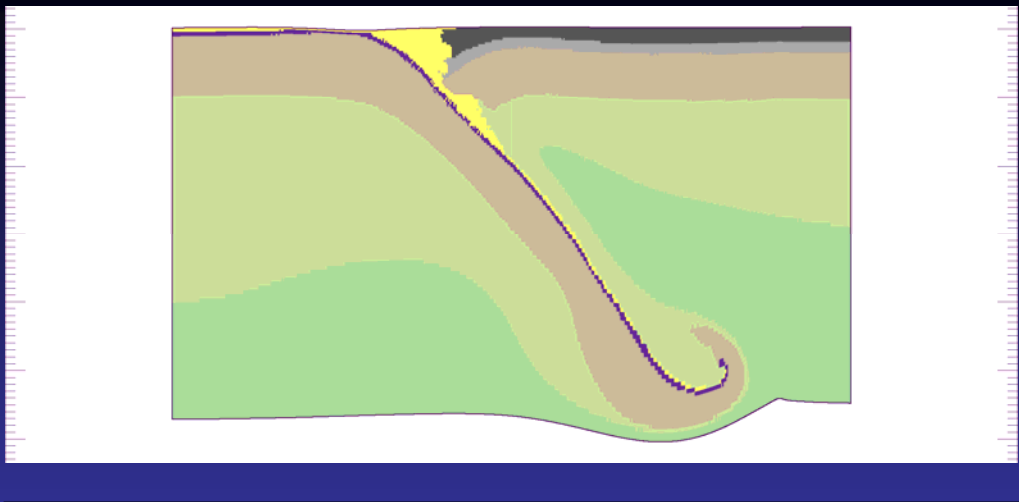


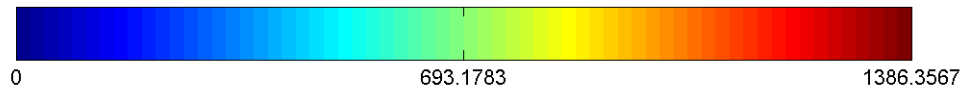
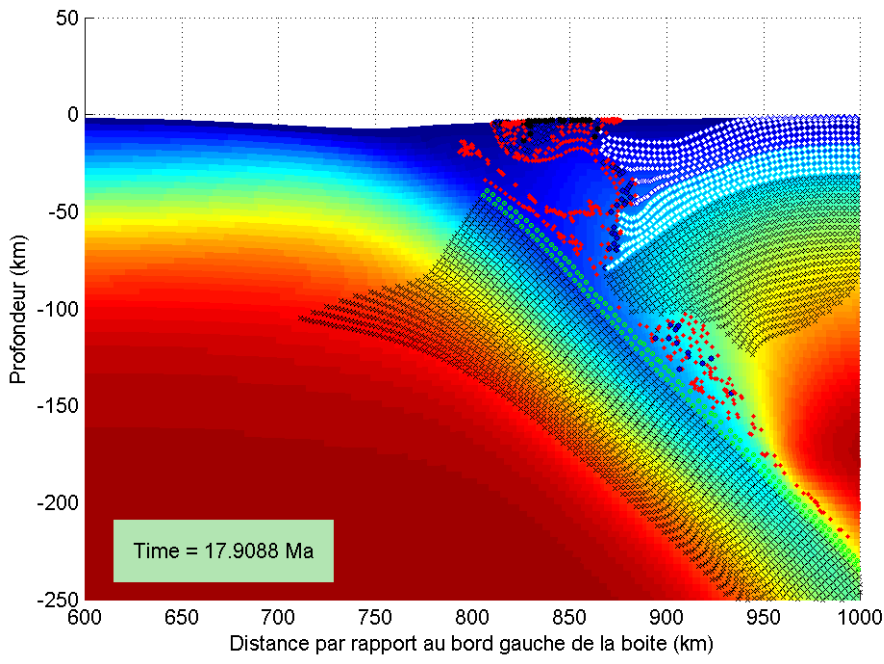
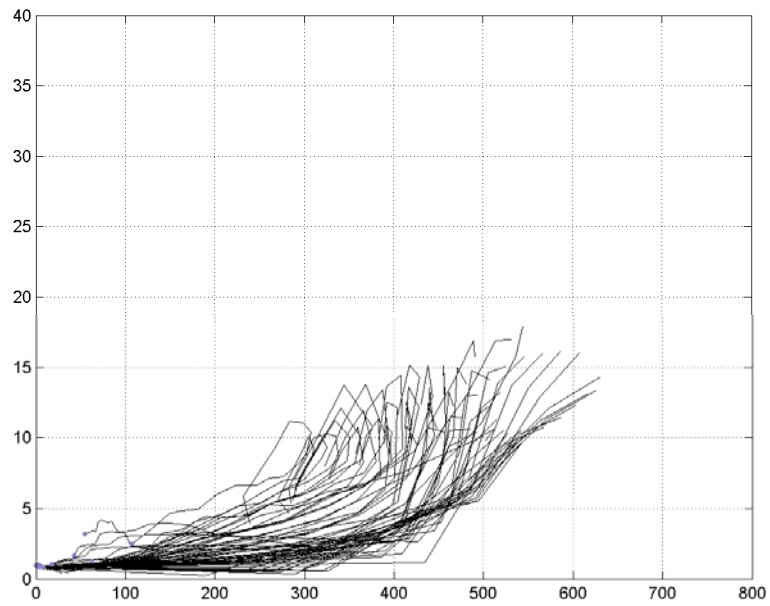


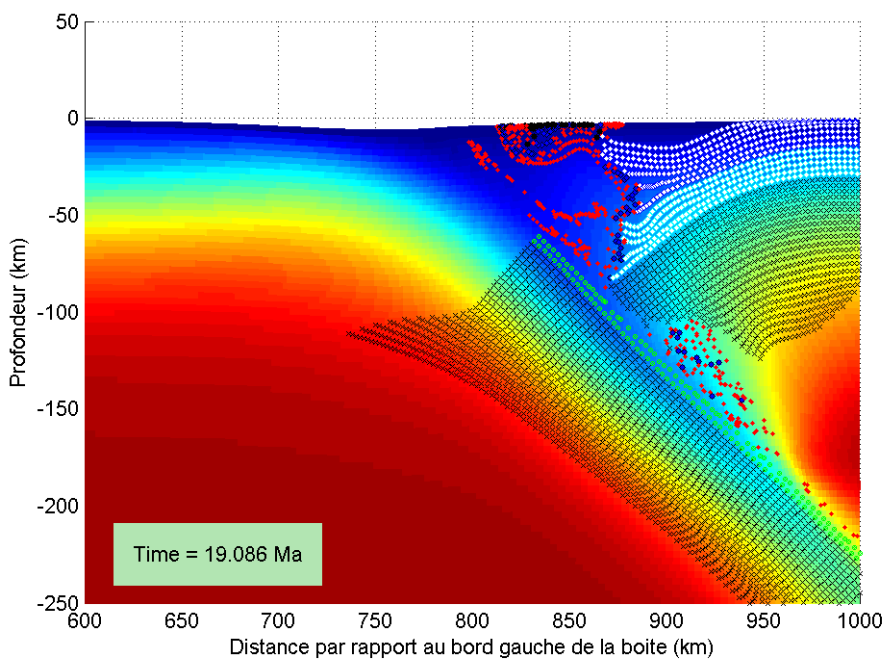
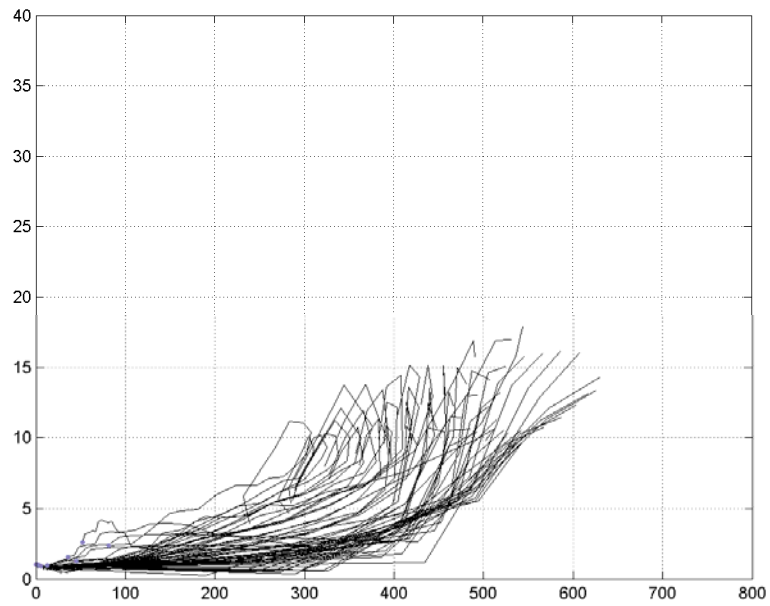
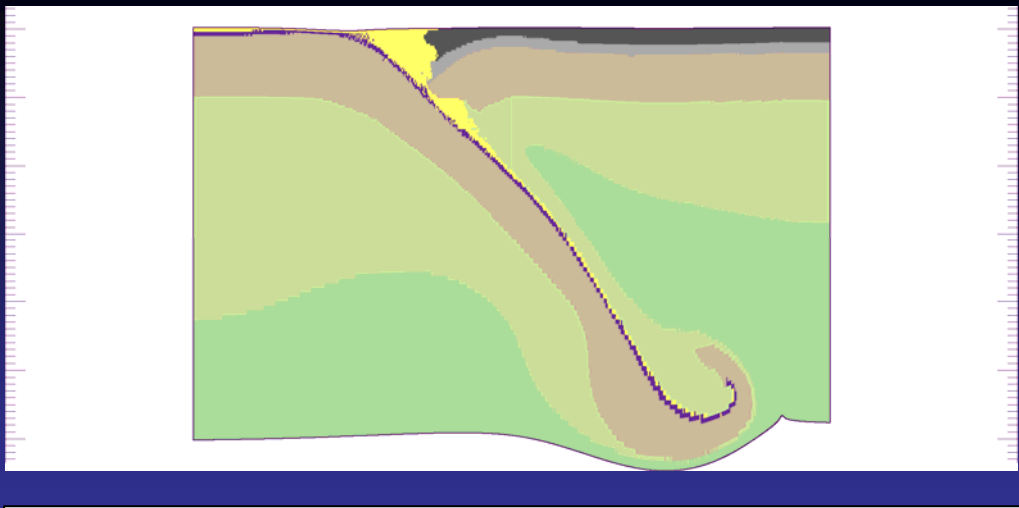


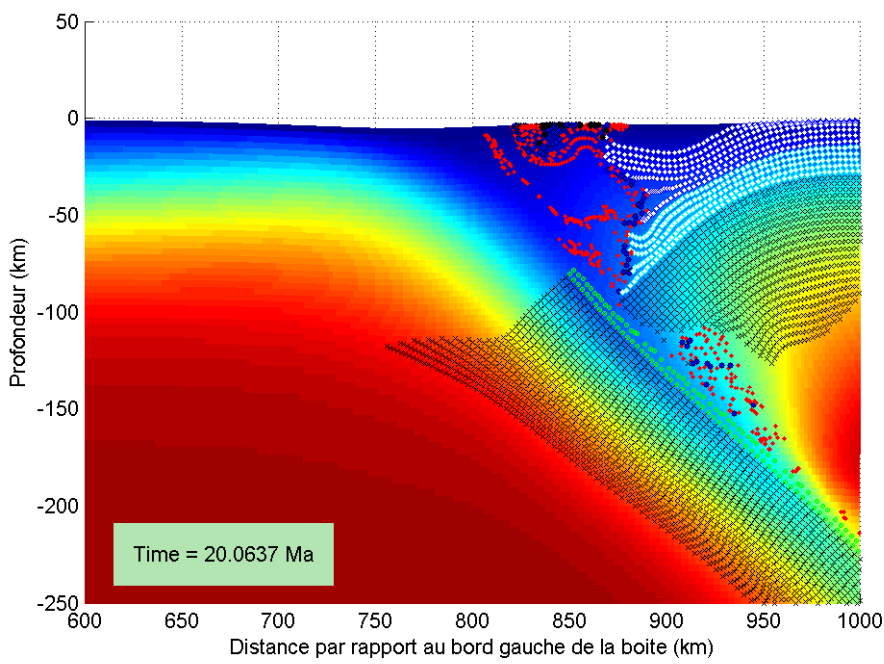
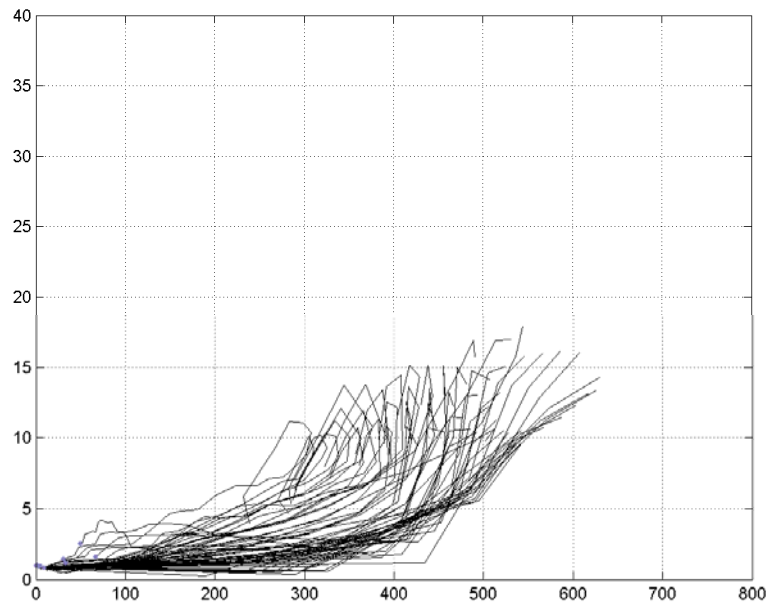
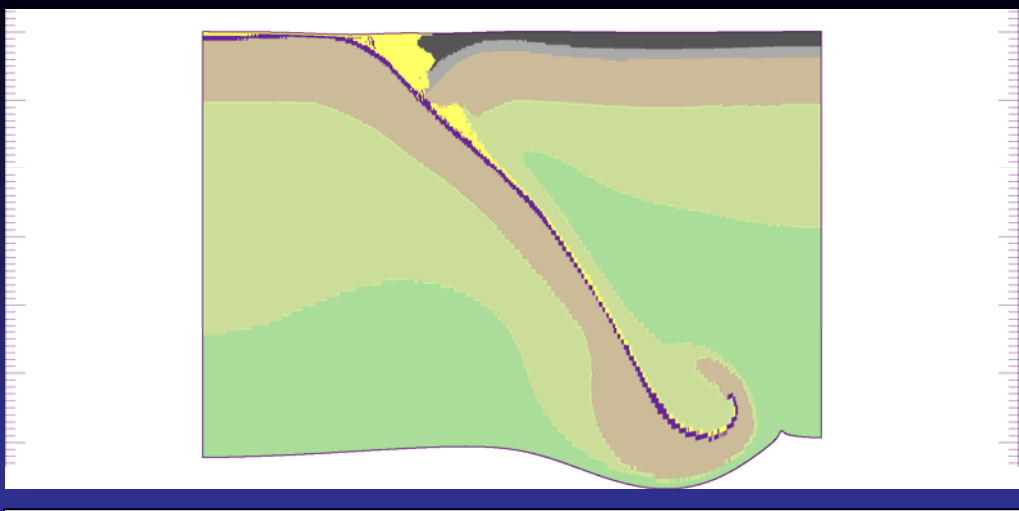






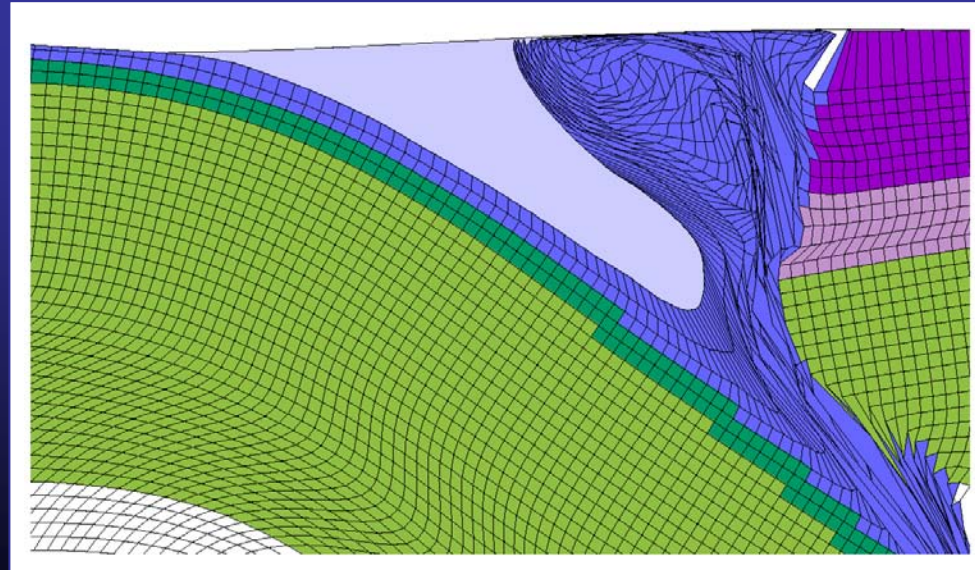
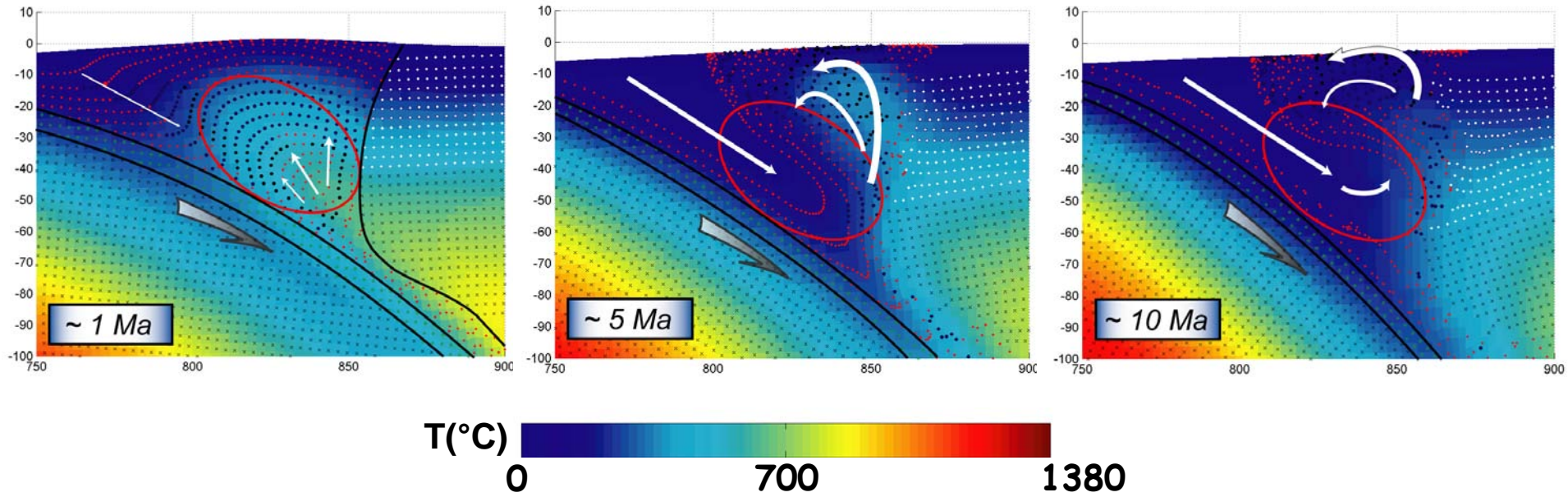






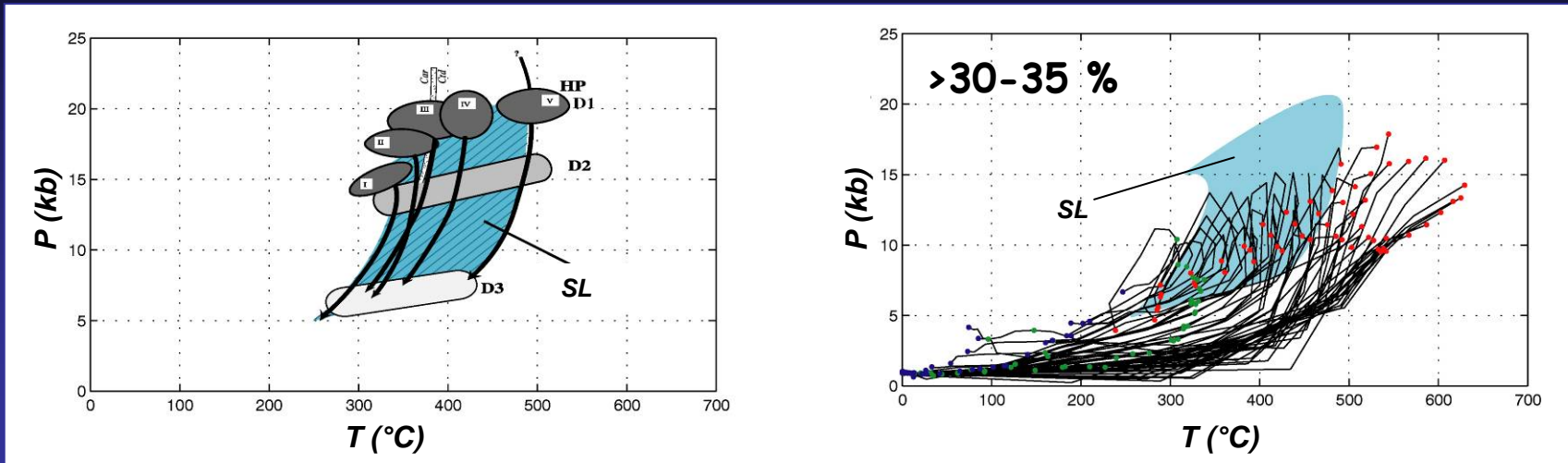
The Results:

Evolution of an accretion prism

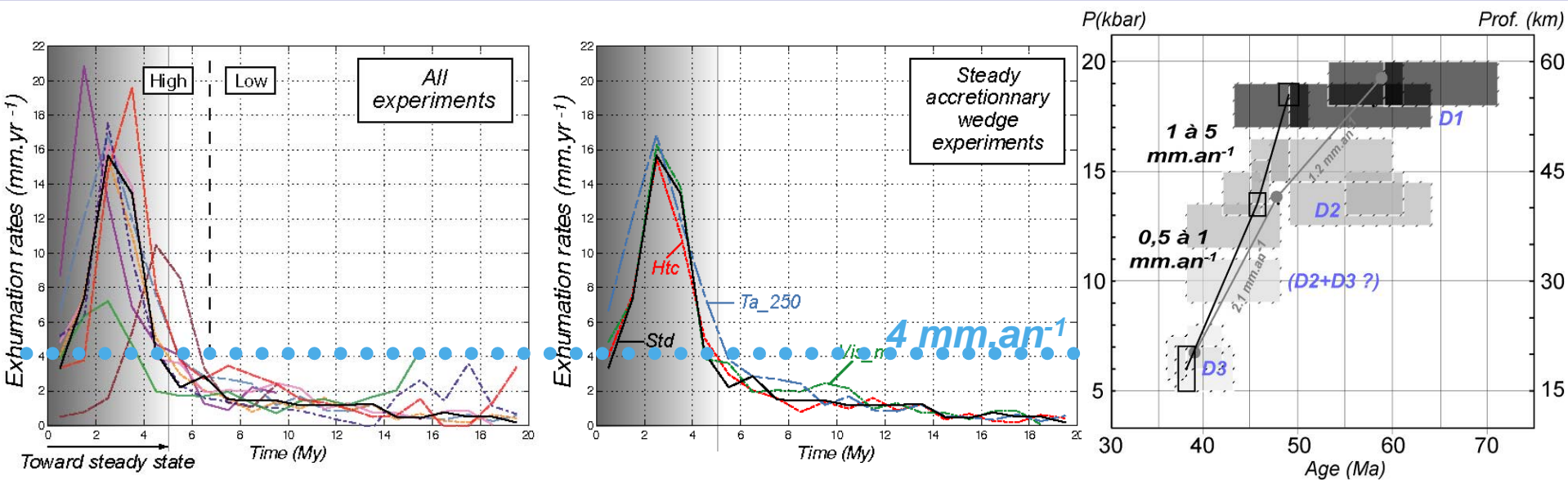


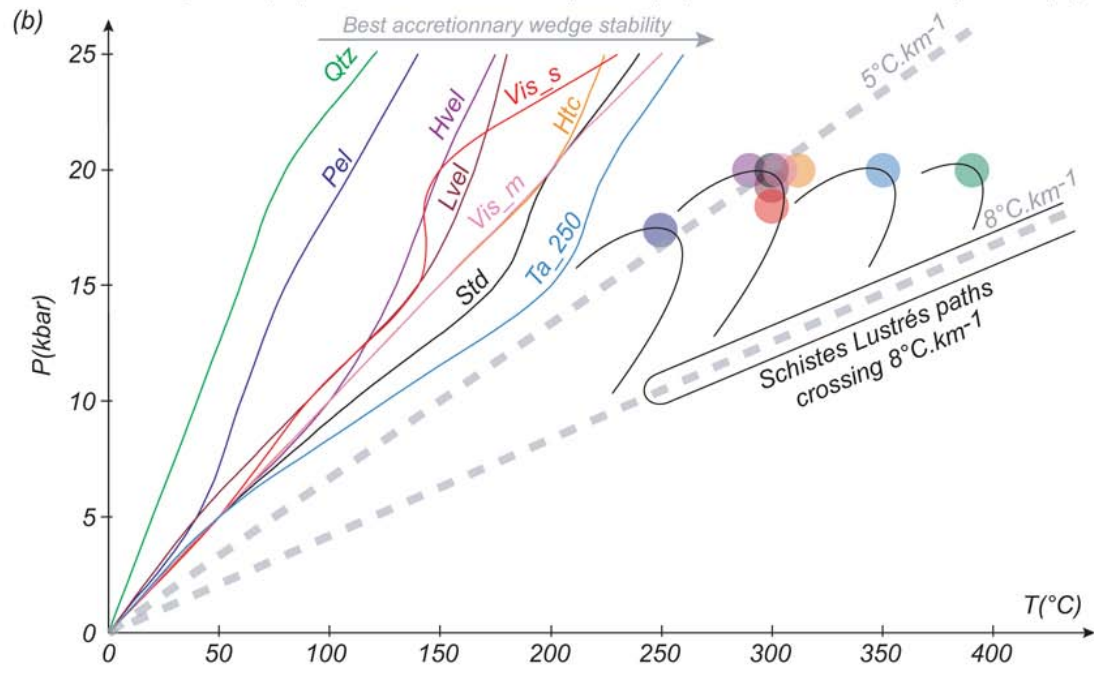
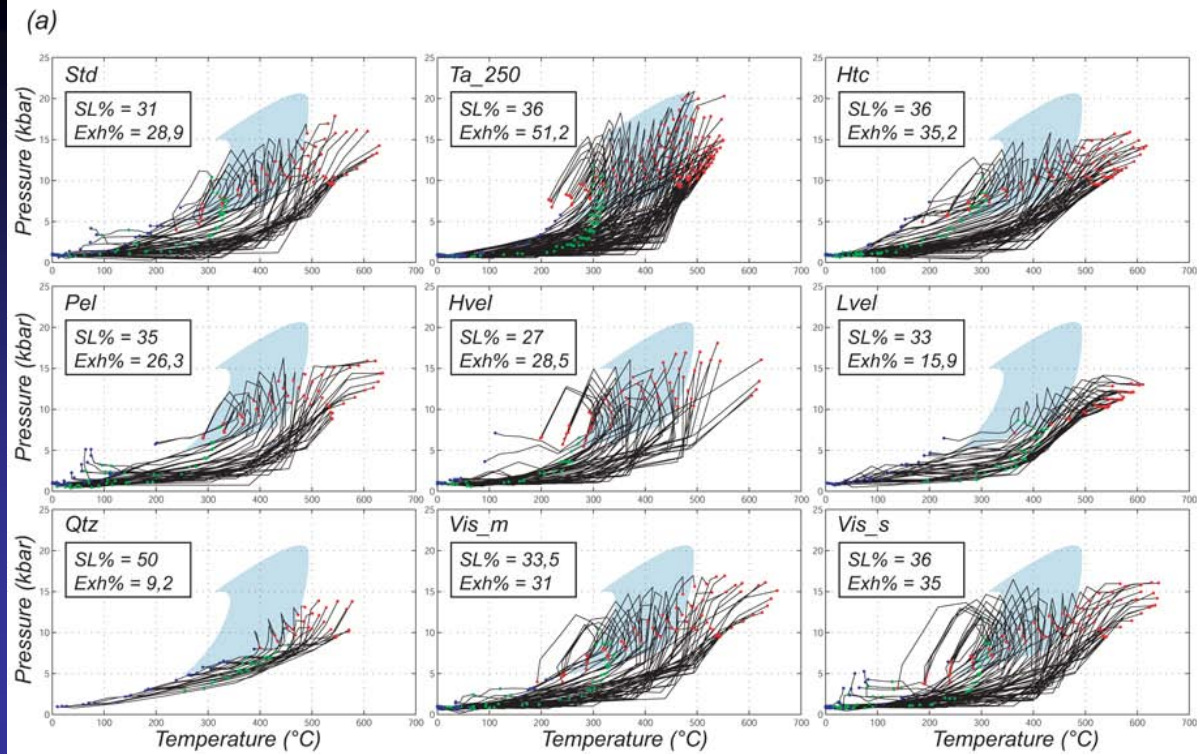
The Results

Observed versus predicted P-T-t paths

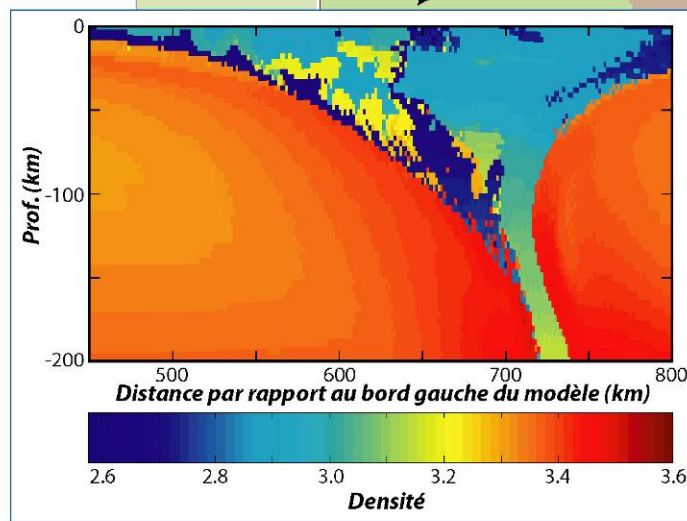
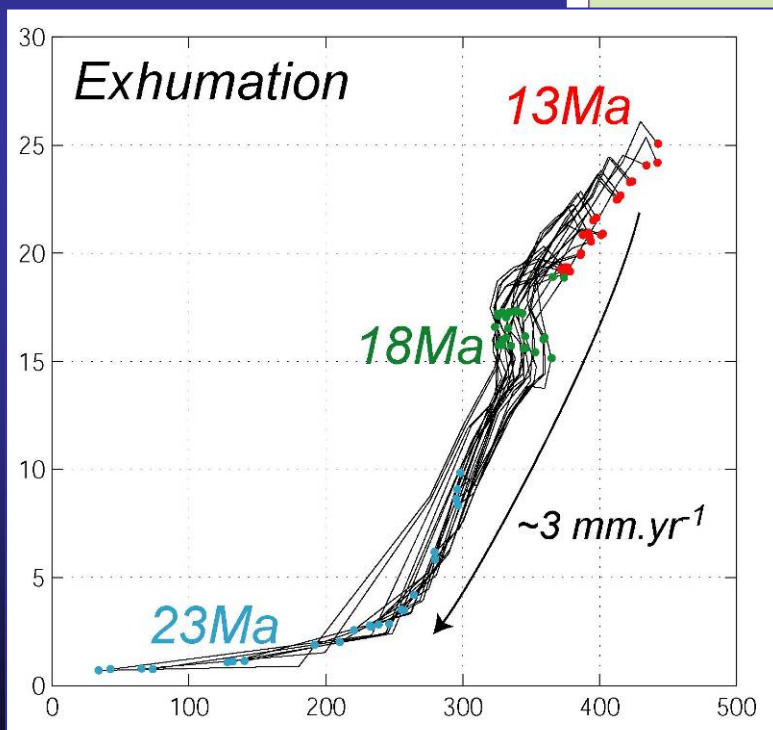
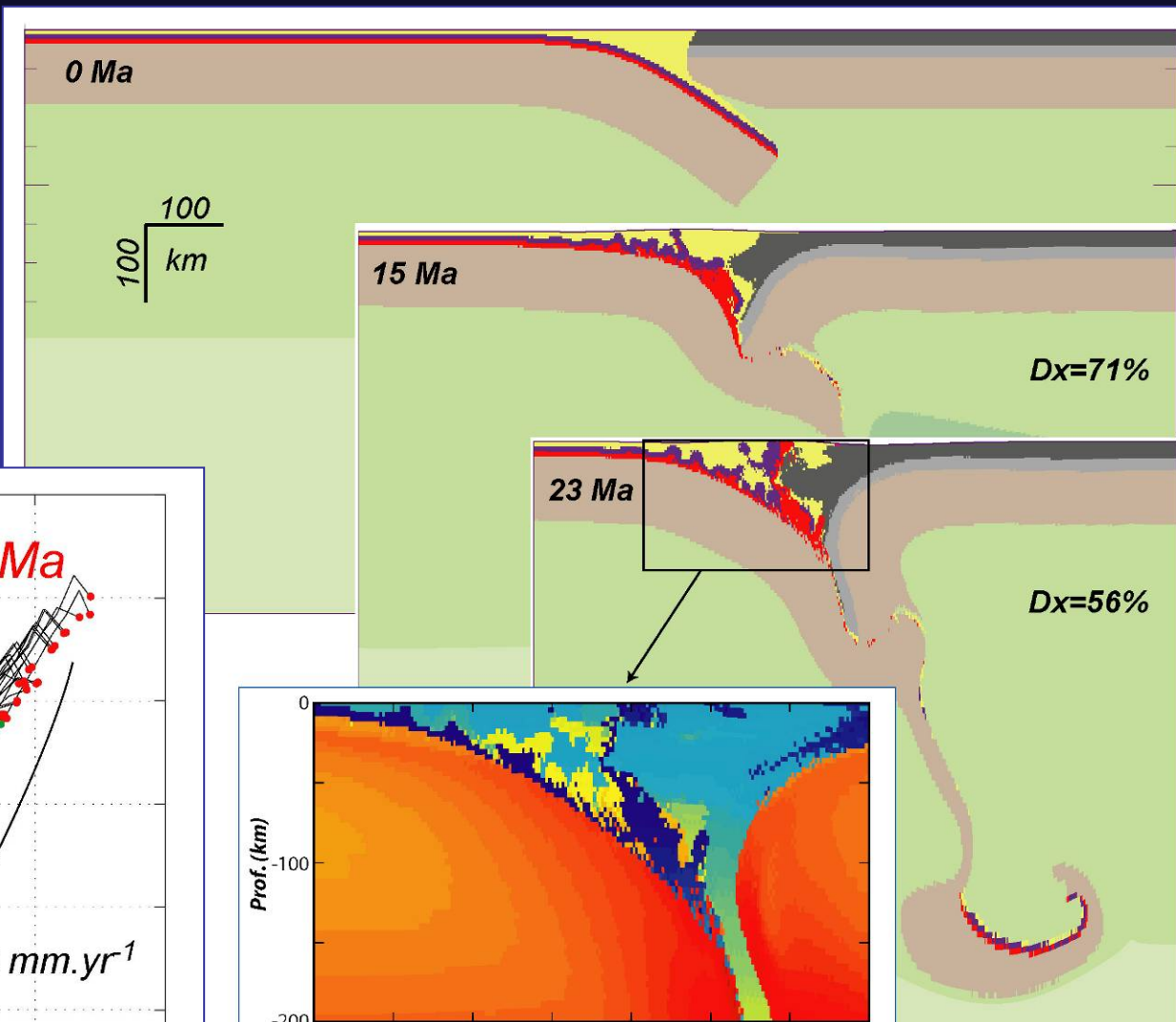
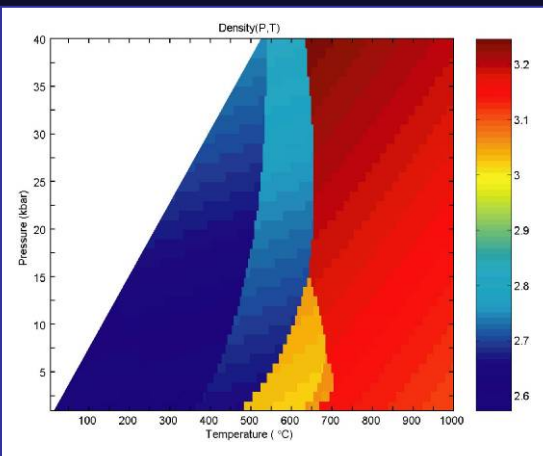


Exhumation rates of sediments in the accretion prism





Serpentinite layer (light, weak) below the oceanic crust: important condition for oceanic subduction

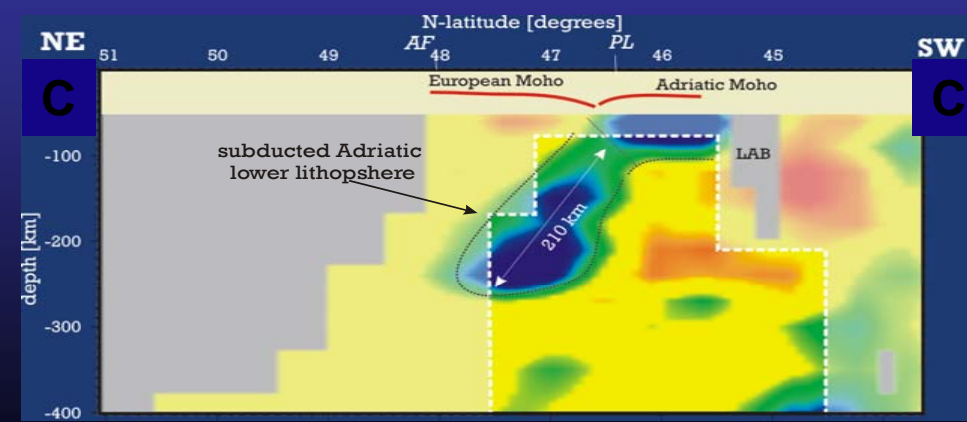
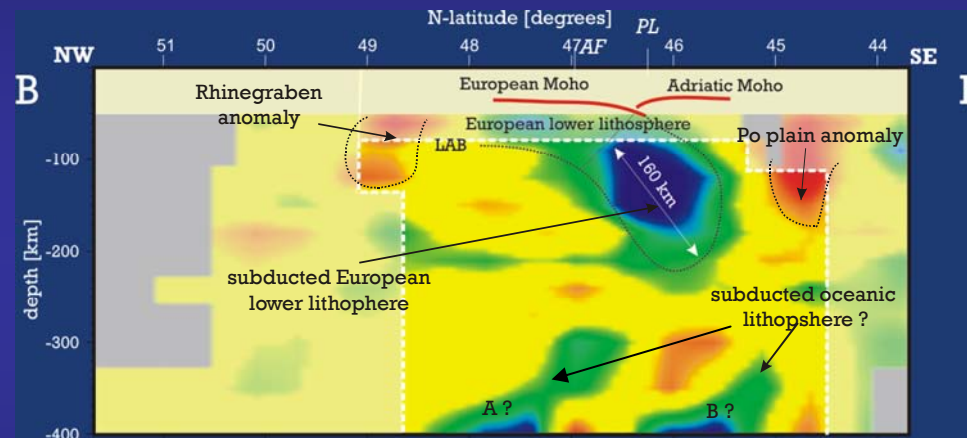
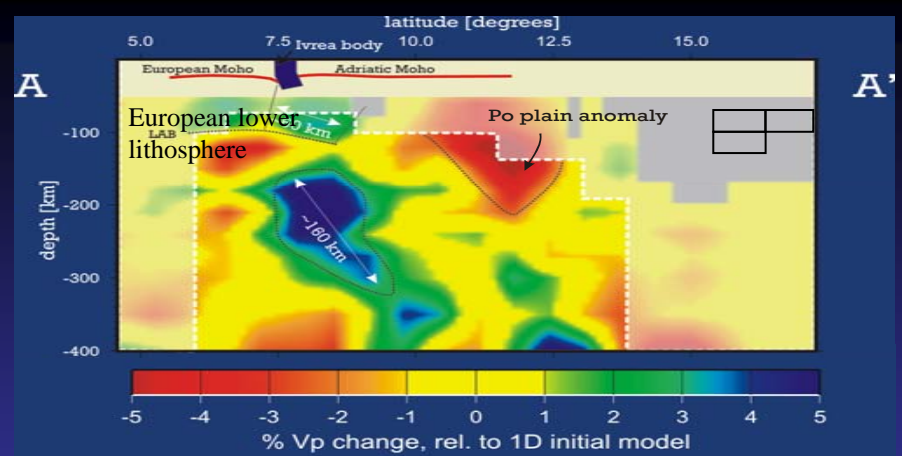
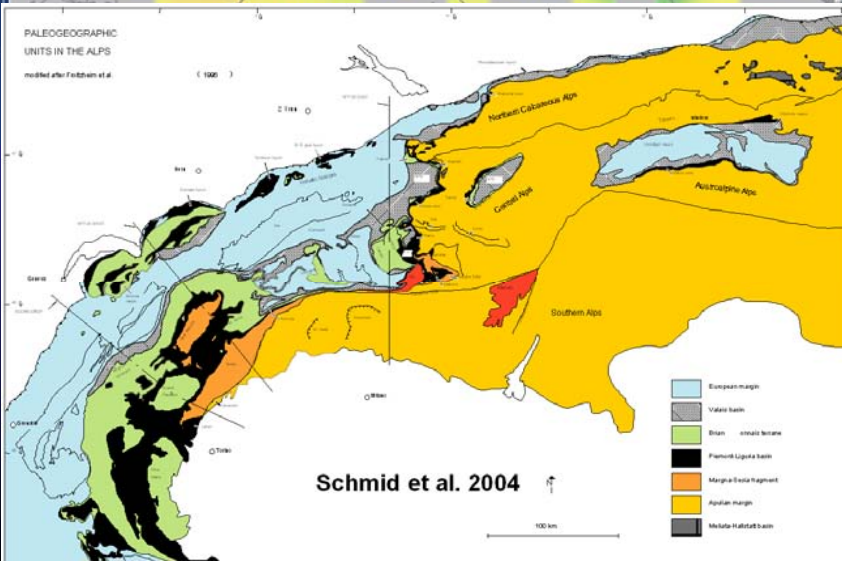
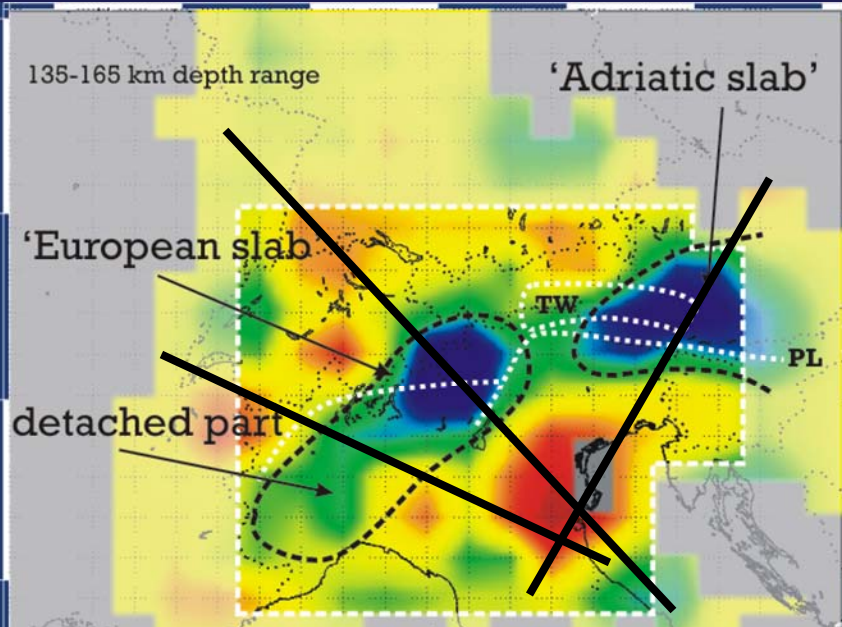


Slow Alpine Collision II: continental phase

*PhD thesis of Ph. Yamato;
Yamato et al., 2007*

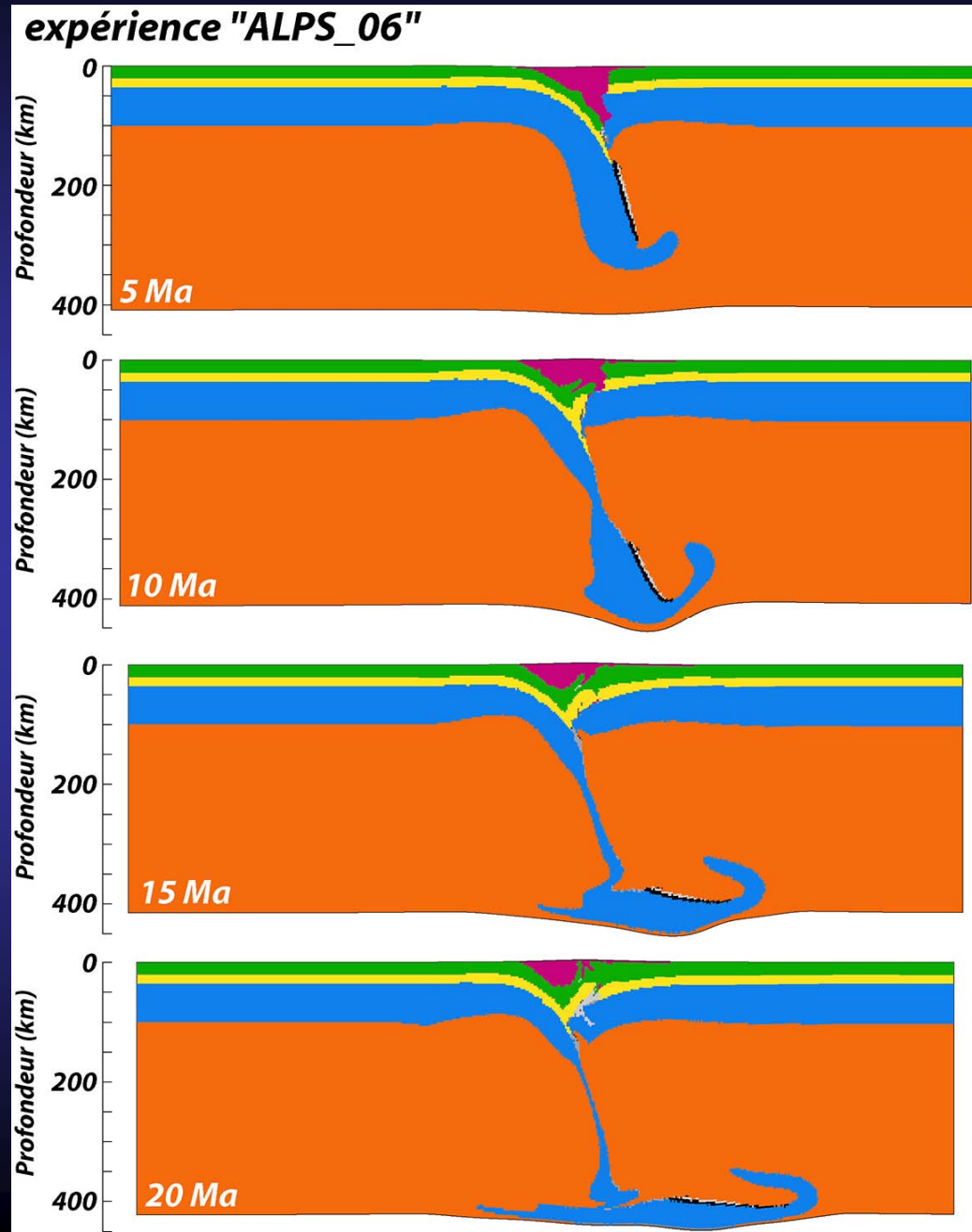
Alpine lithosphere-asthenosphere system

(Courtesy of E. Kissling)



Lippitsch et al. 2003, JGR

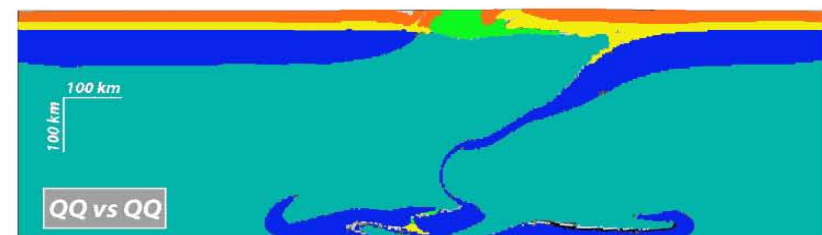
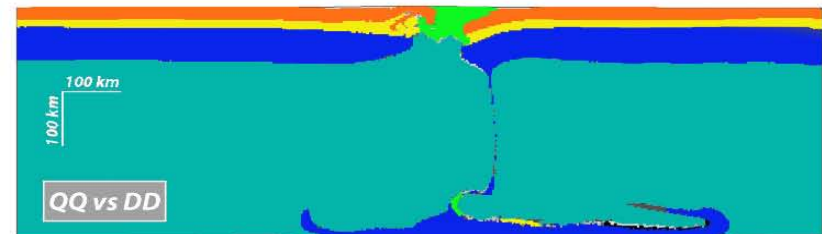
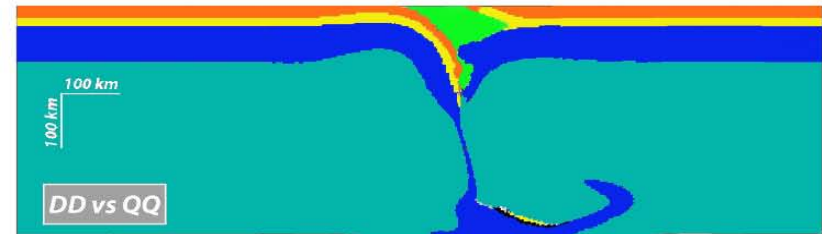
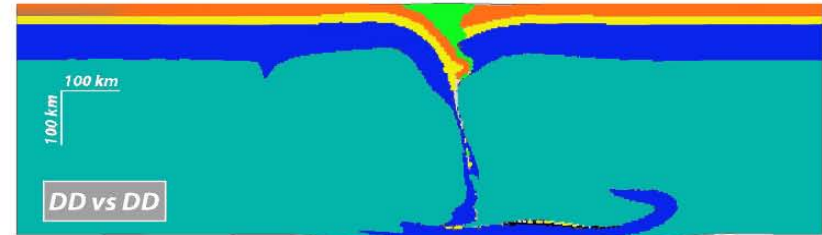
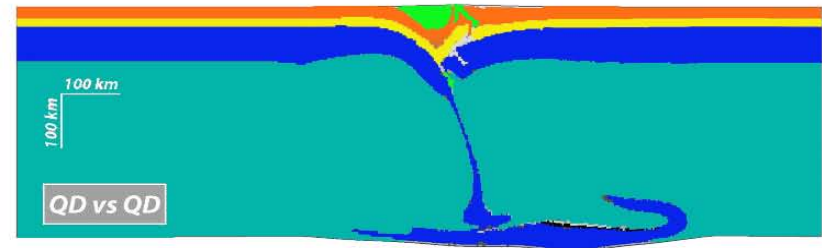
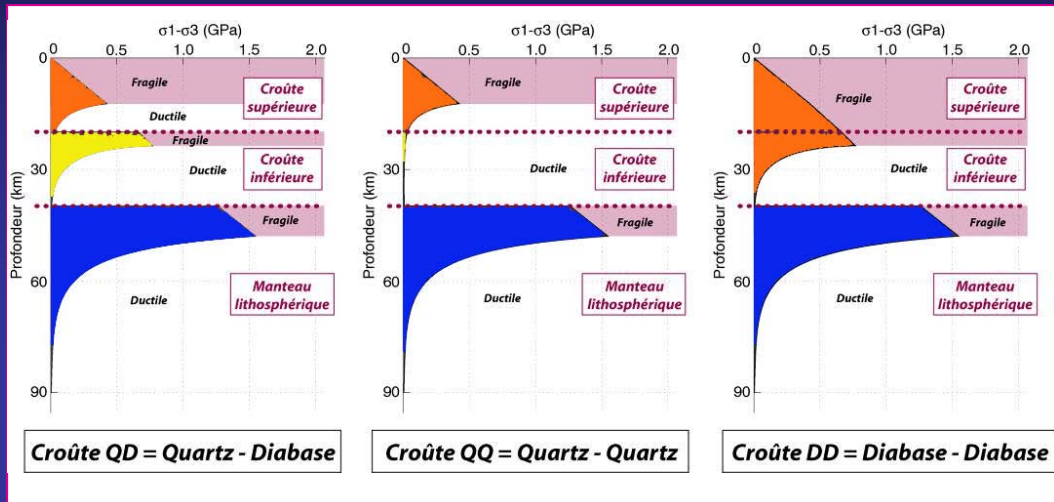
SLOW collision, WEAK ($T_e < 30$ km) lithosphere



$t = 20 \text{ Ma}$

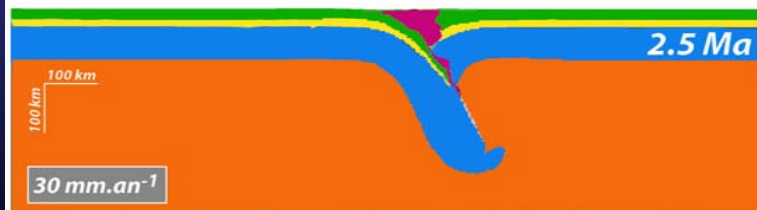
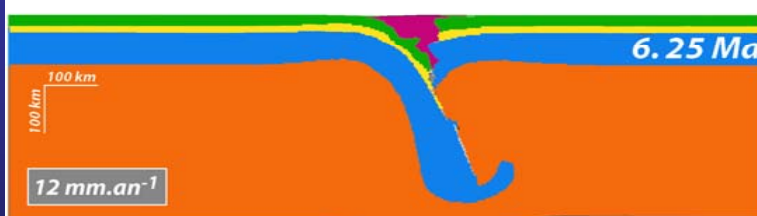
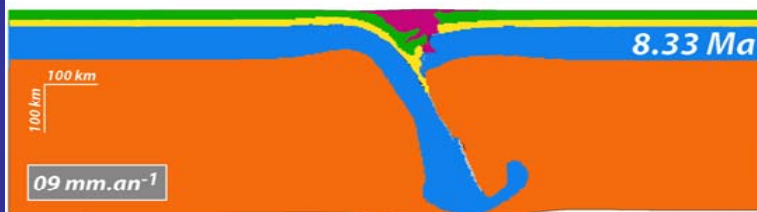
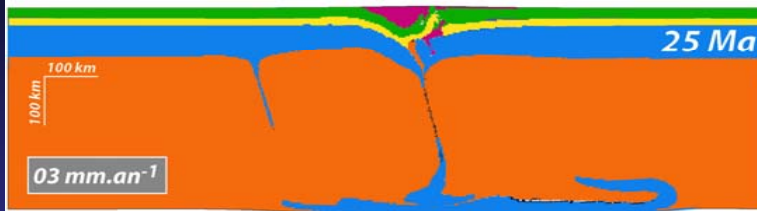
$\Delta x = 8\%$

Influence of the crustal rheology

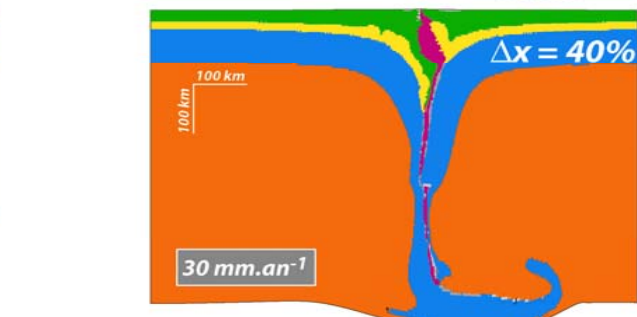
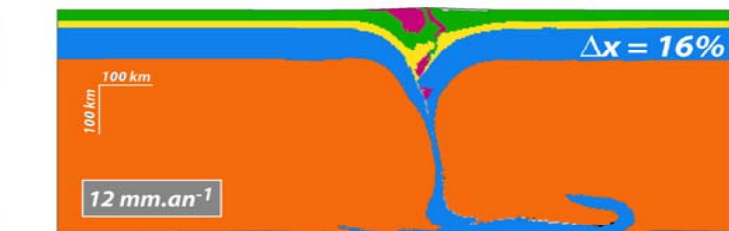
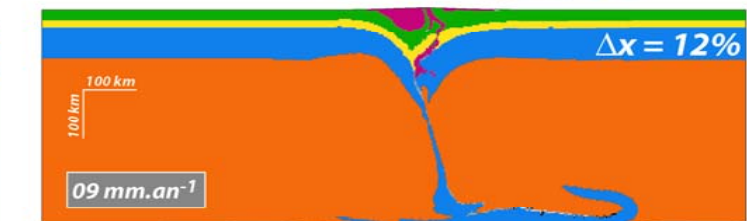
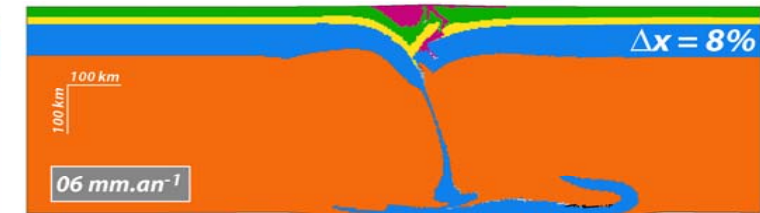
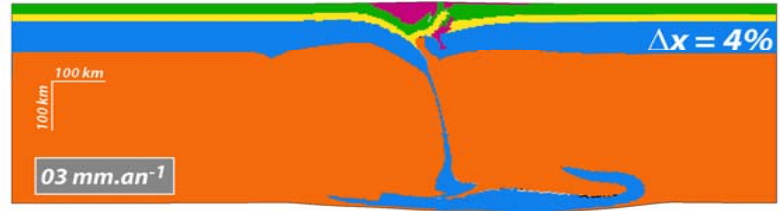


Influence of convergence rate at $\Delta x = 5\%$ at $t = 20 \text{ Myr}$

$\Delta x = 5\%$



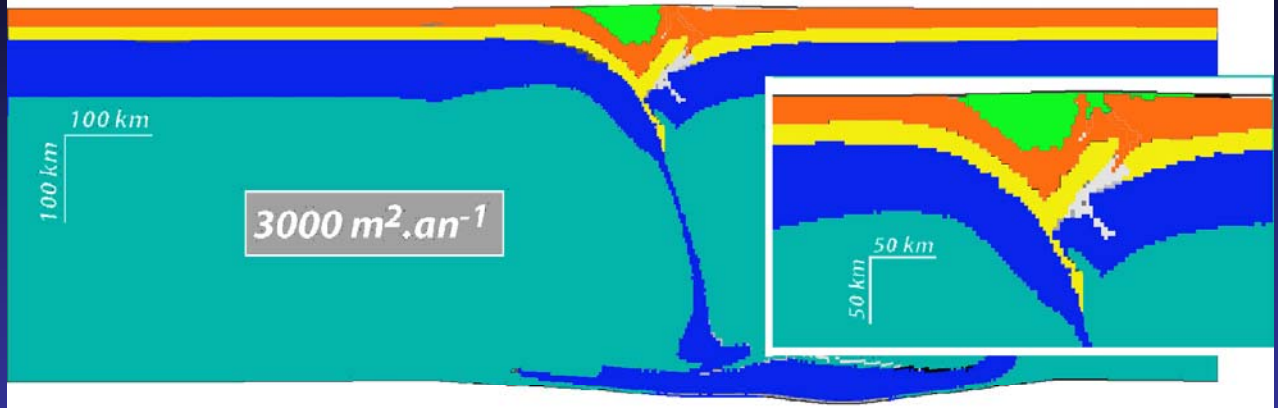
$t = 20 \text{ Ma}$



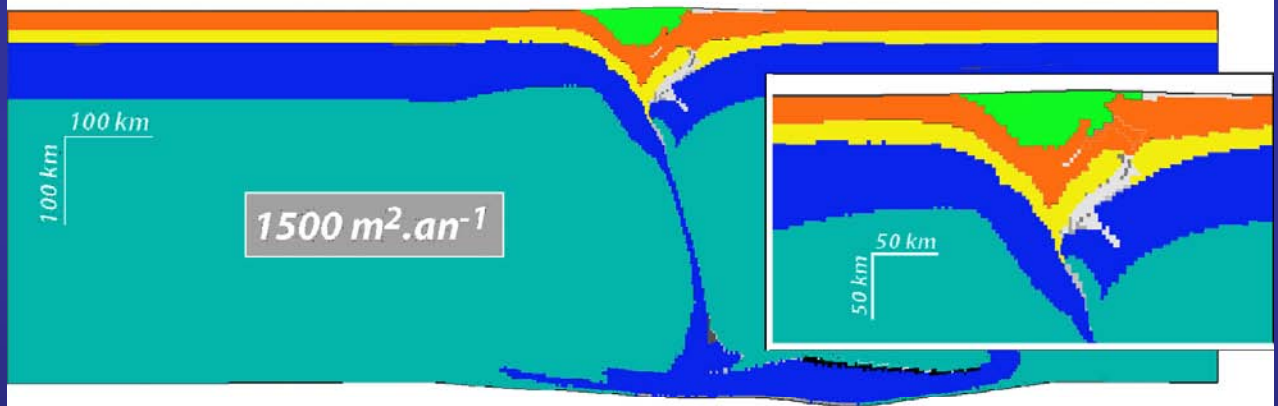
Influence of erosion (k) on collision mode

$t = 20 \text{ Ma}$, $\Delta x = 8\%$, $V_{\text{tot}} = 6 \text{ mm.an}^{-1}$

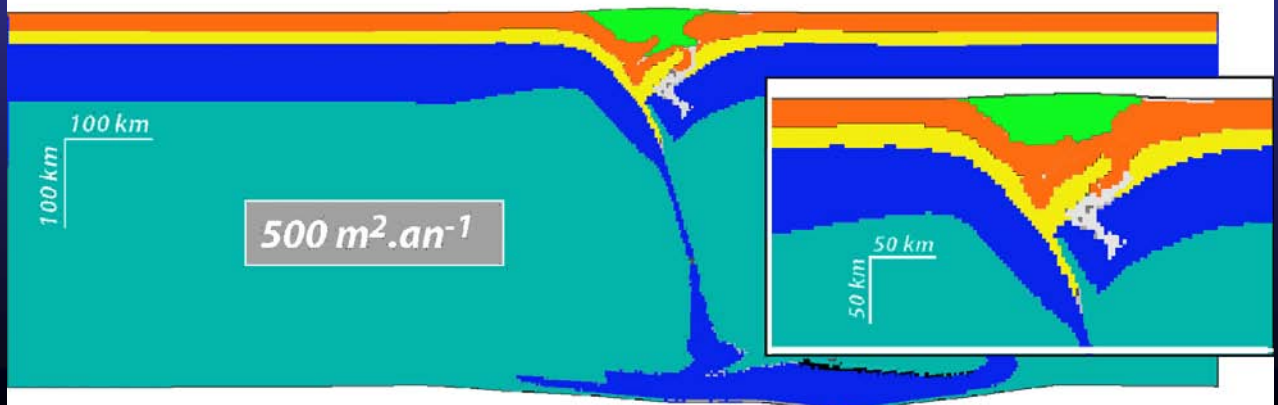
$k = 3000 \text{ m}^2 \text{ y}^{-1}$



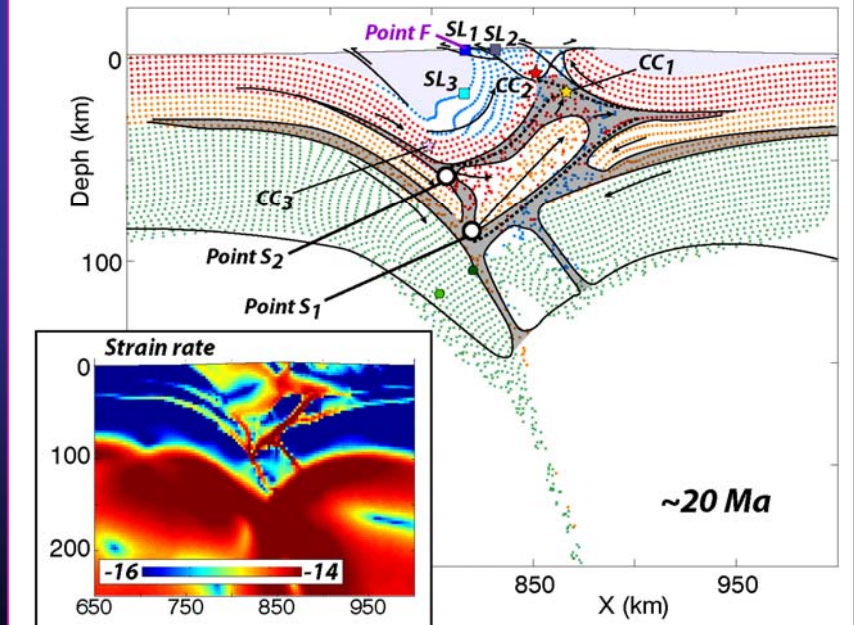
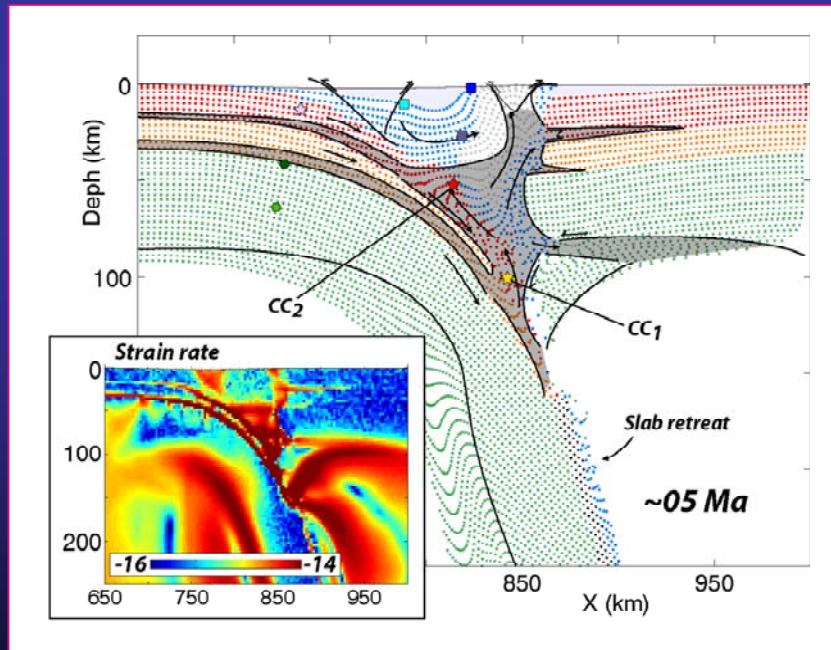
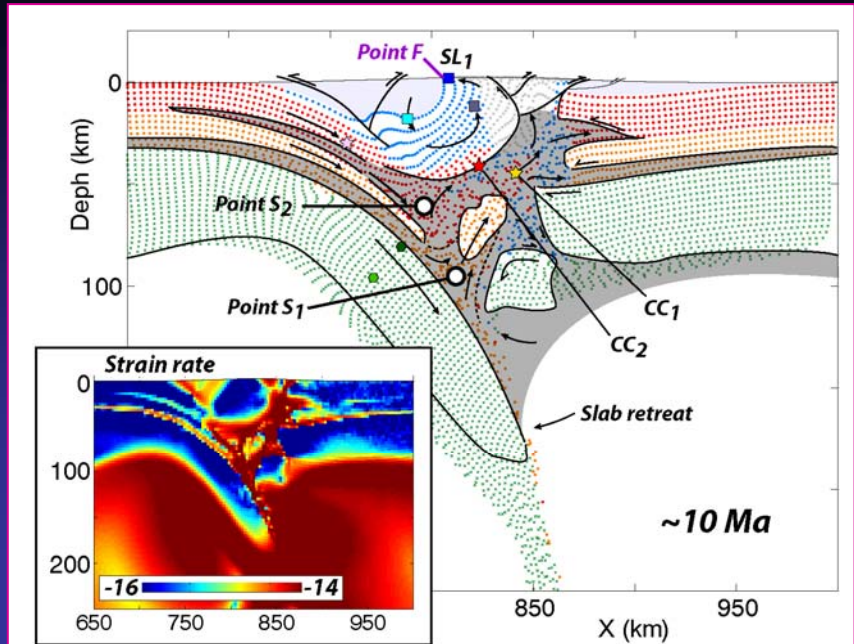
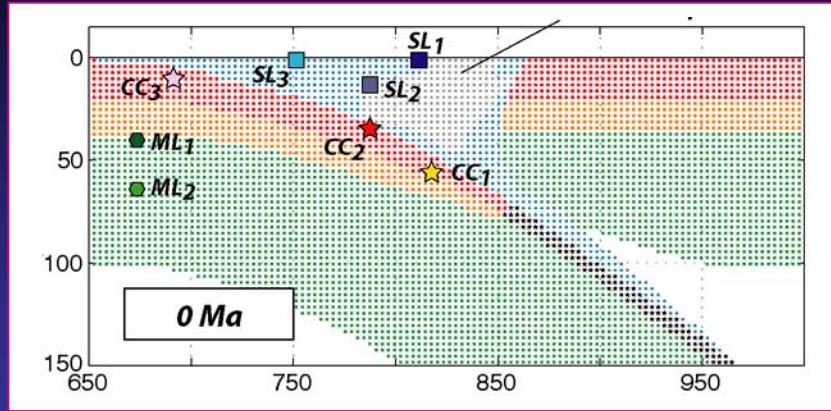
$k = 1500 \text{ m}^2 \text{ y}^{-1}$



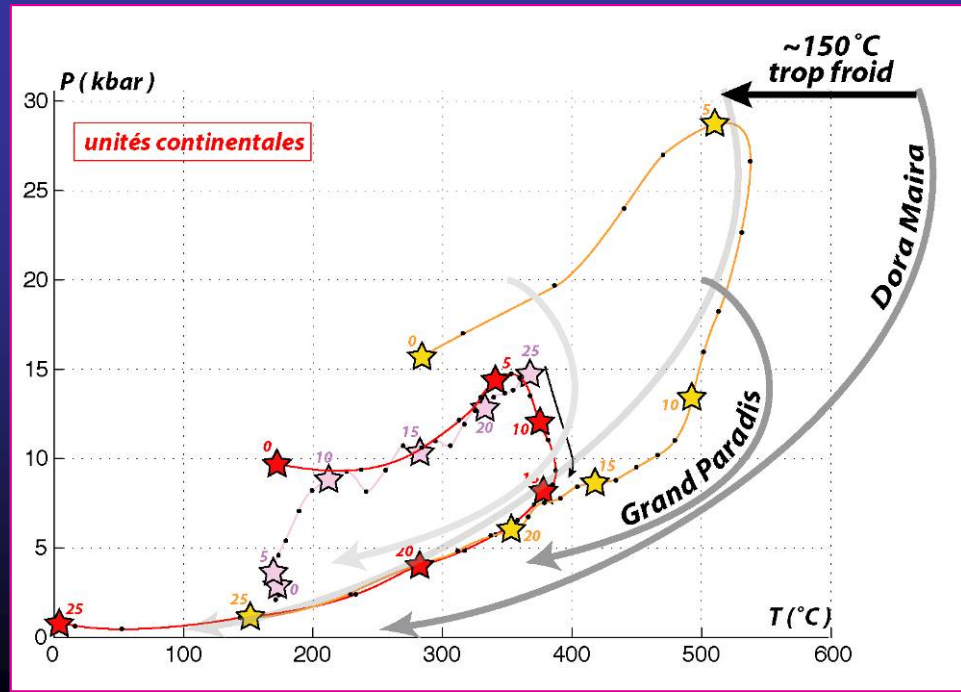
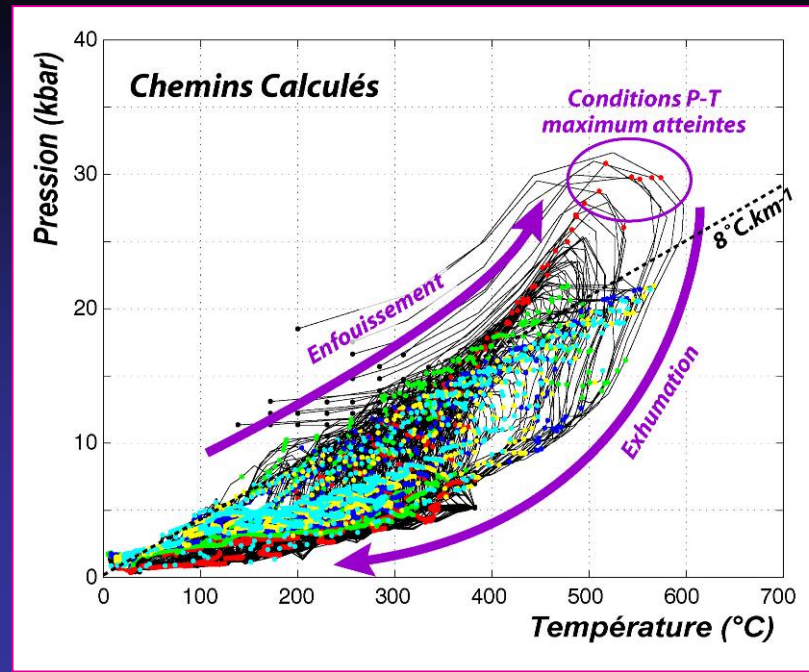
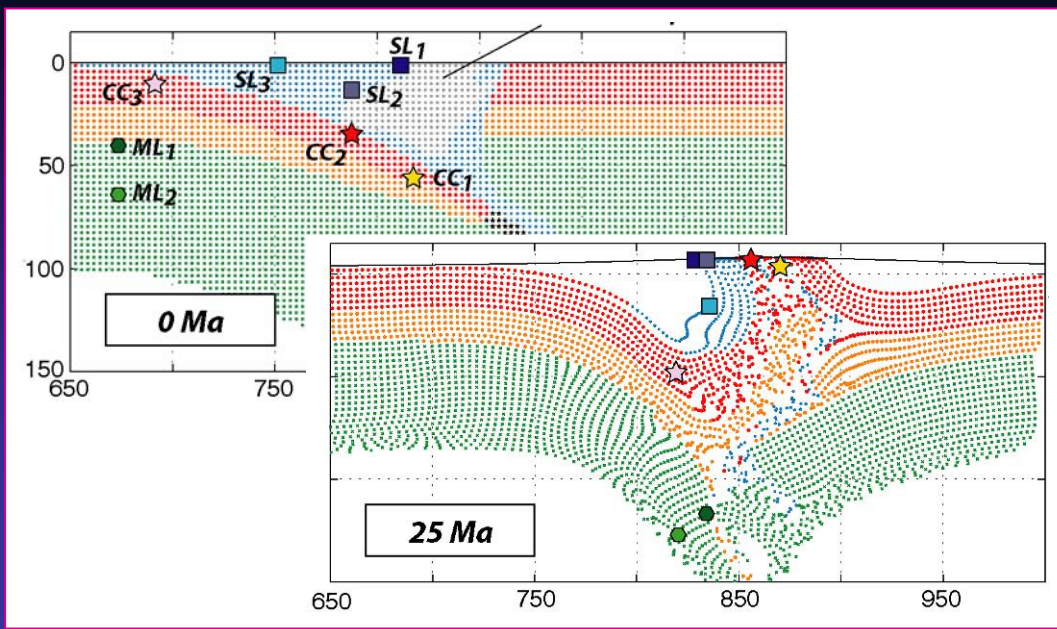
$k = 500 \text{ m}^2 \text{ y}^{-1}$



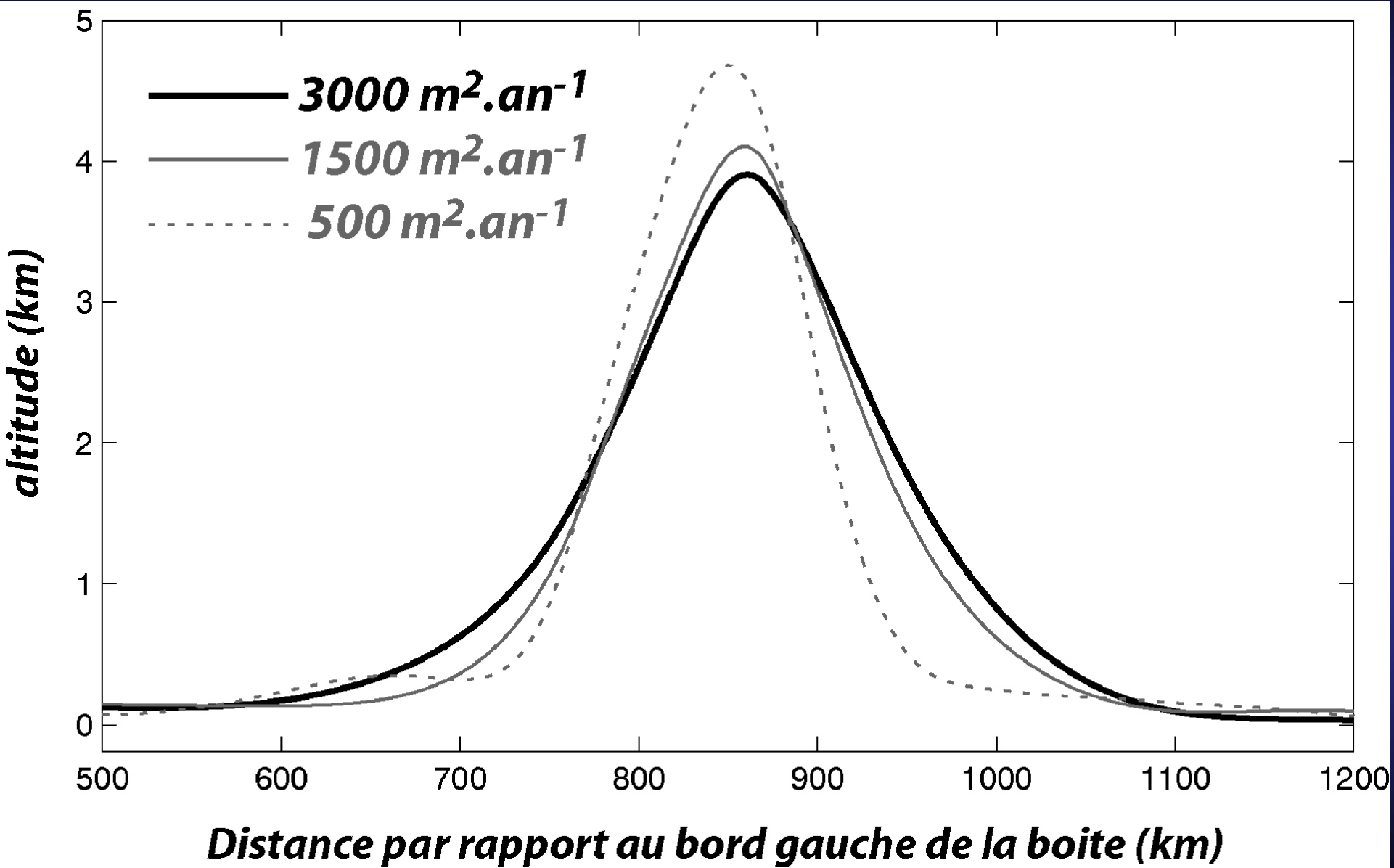
Reference case: evolution details



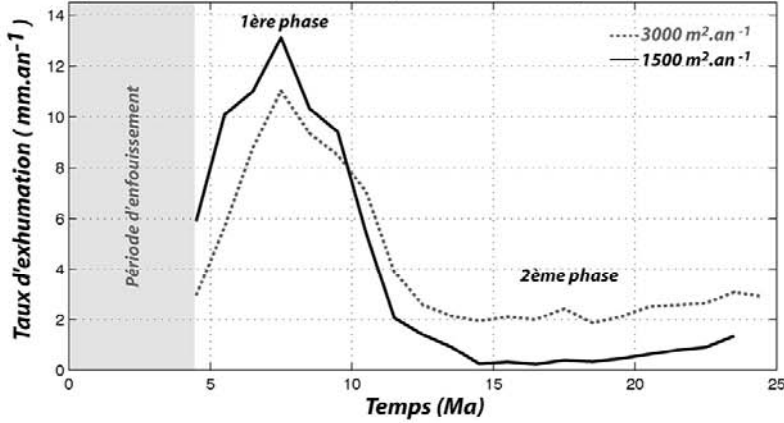
Reference case: predicted P-T-t paths



P-T-t Path



Moyenne des taux d'exhumation pour tous les marqueurs en exhumation

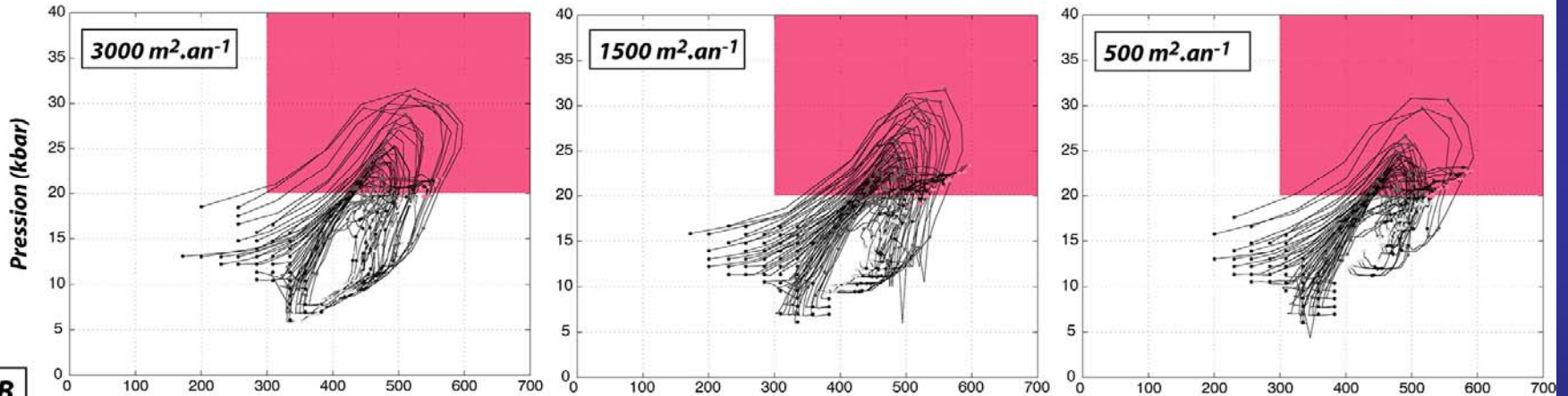


A

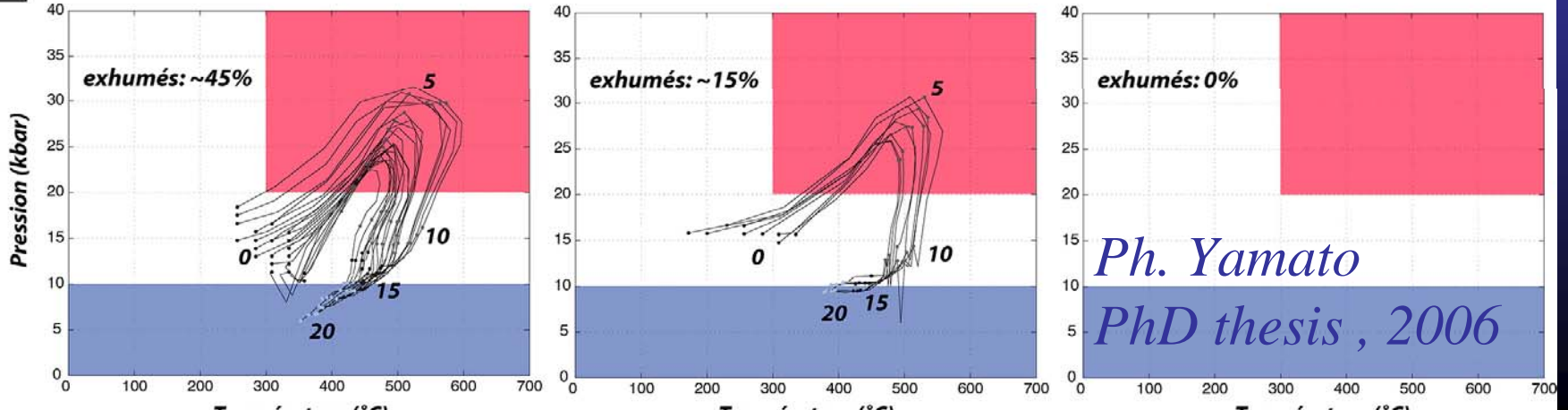
Exhumation rates as function of the erosion rate (first 20 Myr)

Top: markers that have achieved 20-40 kbar and 300-700°C

Bottom: markers that have achieved 10 kbar.



B



HP

LP

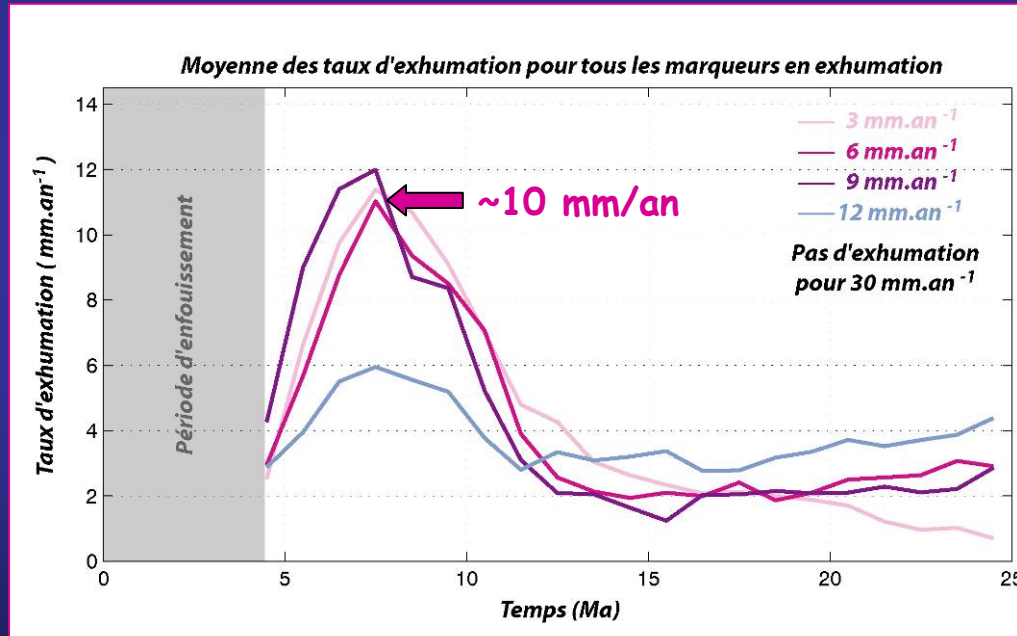
Ph. Yamato
PhD thesis, 2006

Summary of the parametric study of slow continental convergence

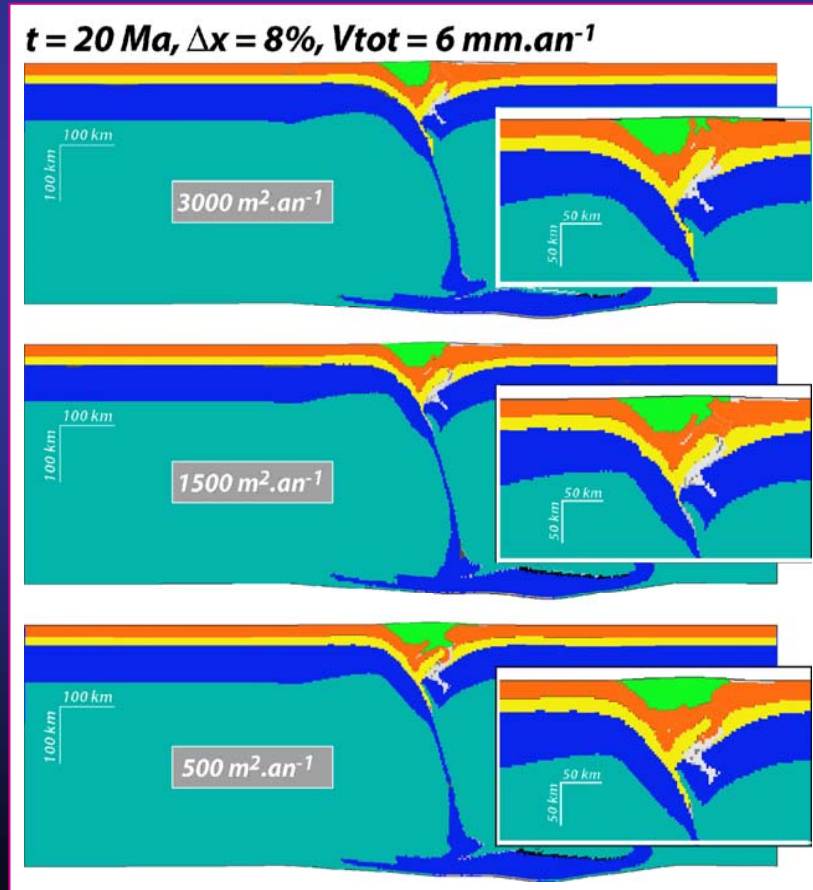
→ 3 major parameters

Convergence rate
Erosion
Rheology of the continental crust

Effect of the convergence rate



Effect of erosion

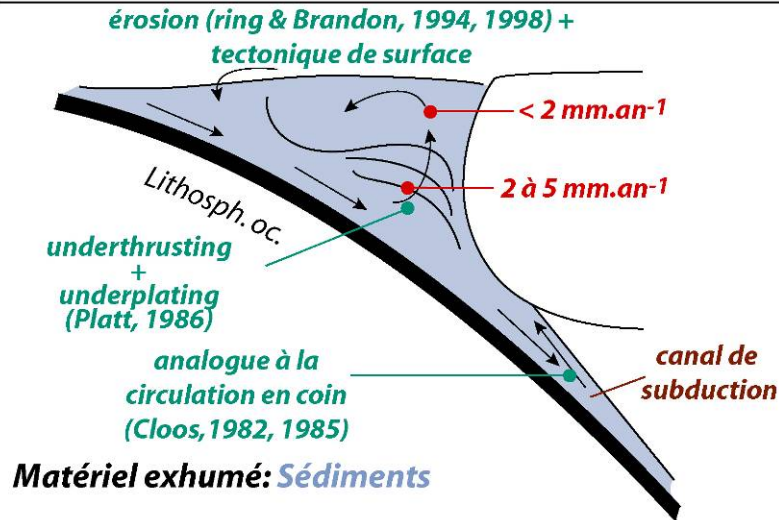


Yamato, 2007

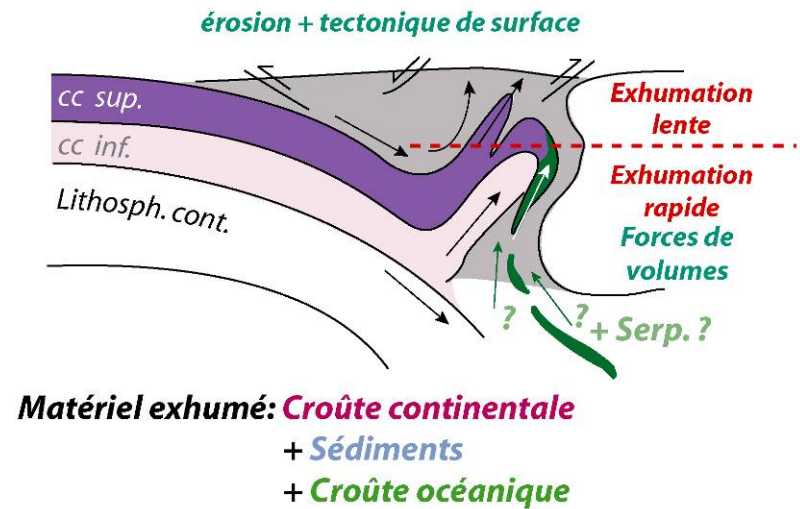
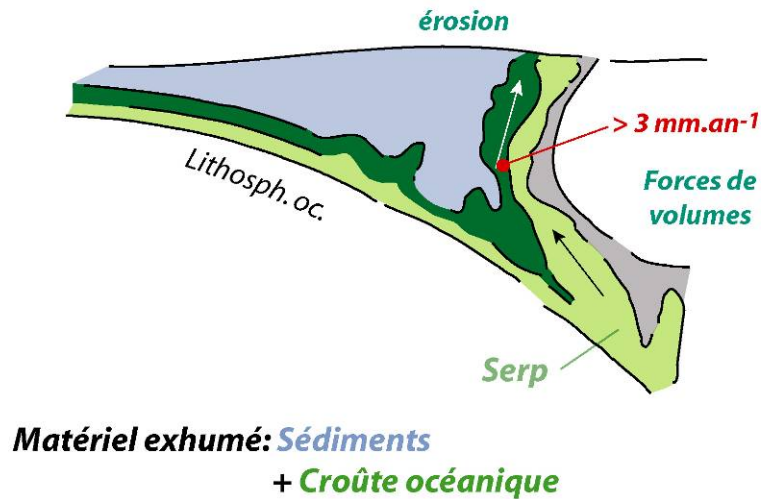
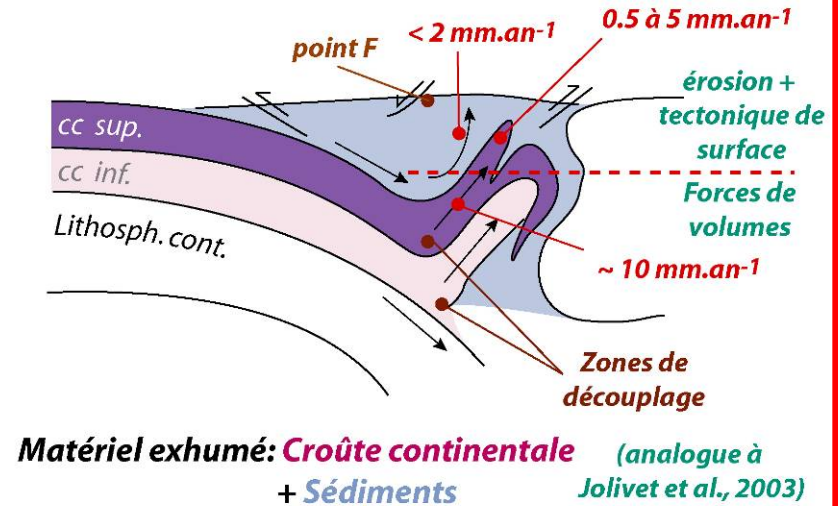
Burov and Yamato, 2007

Oceanic versus continental subduction

SUBDUCTION OCEANIQUE

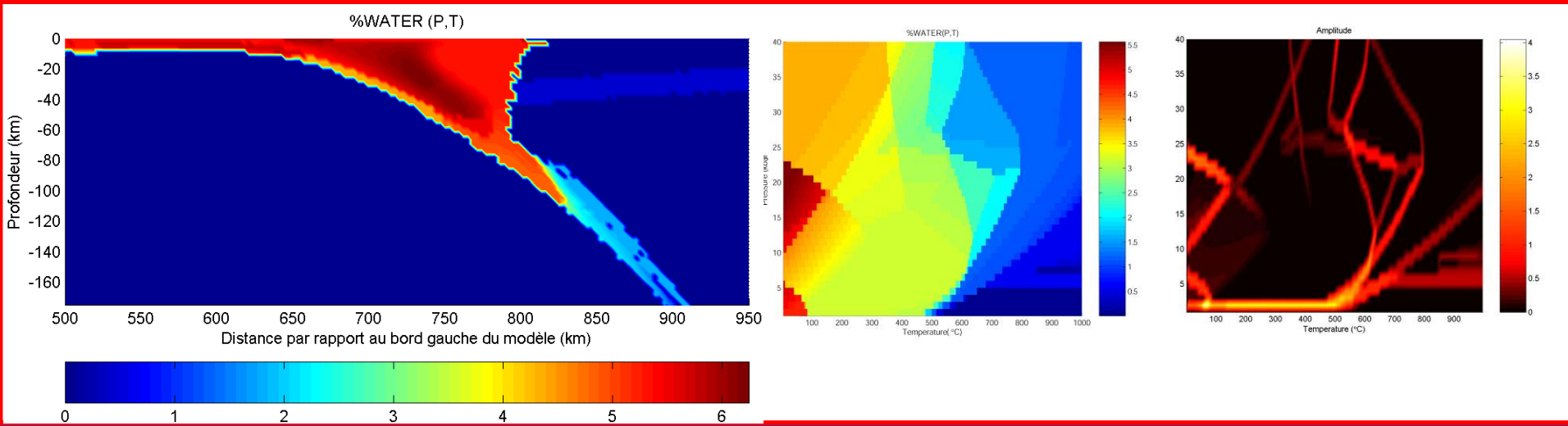


SUBDUCTION CONTINENTALE

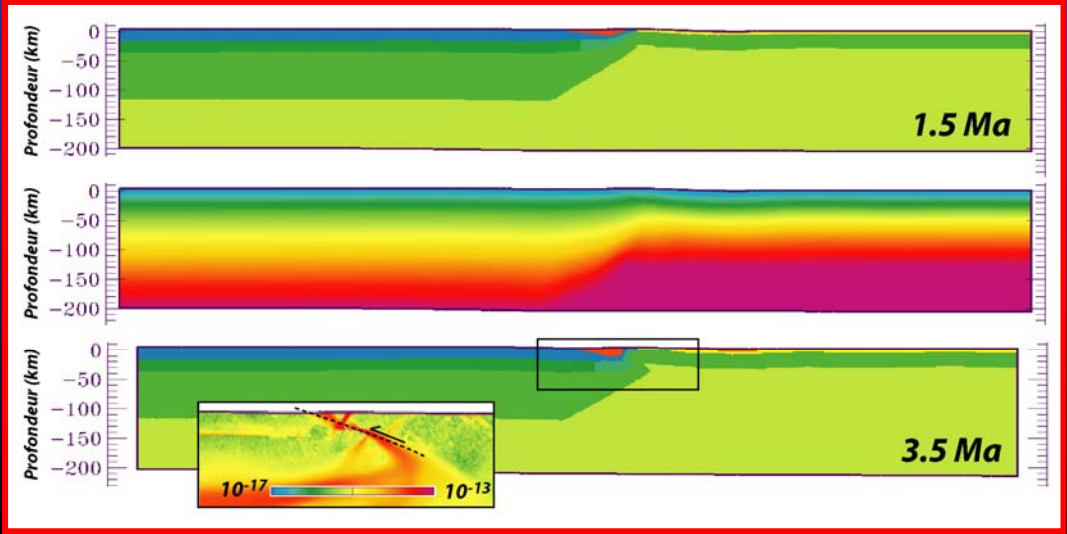


Some Perspectives

- Detailed study of impact of fluid circulation +
- P-T impact on rheology + melting + latent heat production.
- Parametrization of shear heating. Rheology of aggregates



- Some new problems: obduction



... and 'exhumation'!



SUMMARY

- Viscous-elastic-plastic rheology and rheological structure (not simply integrated strength) of both convergent plates is of crucial importance. Some commonly inferred (from rock mechanics) rheological profiles are mechanically prohibited (e.g., CB): possibility to constrain rheology from models !
- Models need to reproduce in sufficient detail a wealth of the observed features such as accretion prism and topography evolution, fault distribution, sedimentary mass balance, P-T-t paths for the exhumed rock, surface heat flow, present day seismic velocity structures etc. Structural and P-T-t data become VERY important constraints on the models.
- Convergence rates $< 1-2$ cm/y or > 10 cm/y are incompatible with subduction mechanisms. Continental subduction is a short-lived stage (1-5 My for the Alps, 15 My for India) of continental convergence. For oceanic subduction, fluids (serpentinization) condition stable asymmetric subduction.
- Topography, but also DEEP subsurface evolution strongly depend on dynamic interplays between subsurface and surface processes
- Need to account for deep mantle dynamic (and phase transitions) at list down to the depth of 650 km
- Phase transitions and evolution of the mechanical properties of rocks as function of P-T and fluid content need to be taken into account (next challenge !)

SUMMARY

- In difference from oceanic subduction, continental subduction requires far-field forcing and is strongly conditioned by rheological structure of the lithosphere. Strong mantle lithosphere and high initial convergence rate ($> 2 \times 1.5$ cm/y) are the primary conditions for continental subduction.
- Evolution of collision zones depends on the rheology and crustal thickness of both, the upper and the lower plate. Crust-mantle decoupling in the subducting plate may drive crustal thickening in the upper plate.
- Crustal material may be drawn to 100-150 km depths - the HP-UHP exhumation mechanisms are different for different convergence styles and rates - Structural and P-T-t data become important constraints on the models
- Fast convergence rates (e.g., 5 cm/y, Himalaya) favour polyphase evolution with *several episodes of crustal prism evolution and exhumation*.
- In real world, slow-down of the convergence rate during collision should play a primary role for exhumation and further evolution of collision
- Topography, but also DEEP subsurface evolution strongly depend on dynamic interplays between subsurface and surface processes